

S O K E N D A I

NII



# Safety under Statistical and Environmental Uncertainties

Challenges in Cyber-Physical Systems with  
Machine-Learning Components

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Research Director, ERATO MMSD



# Outline

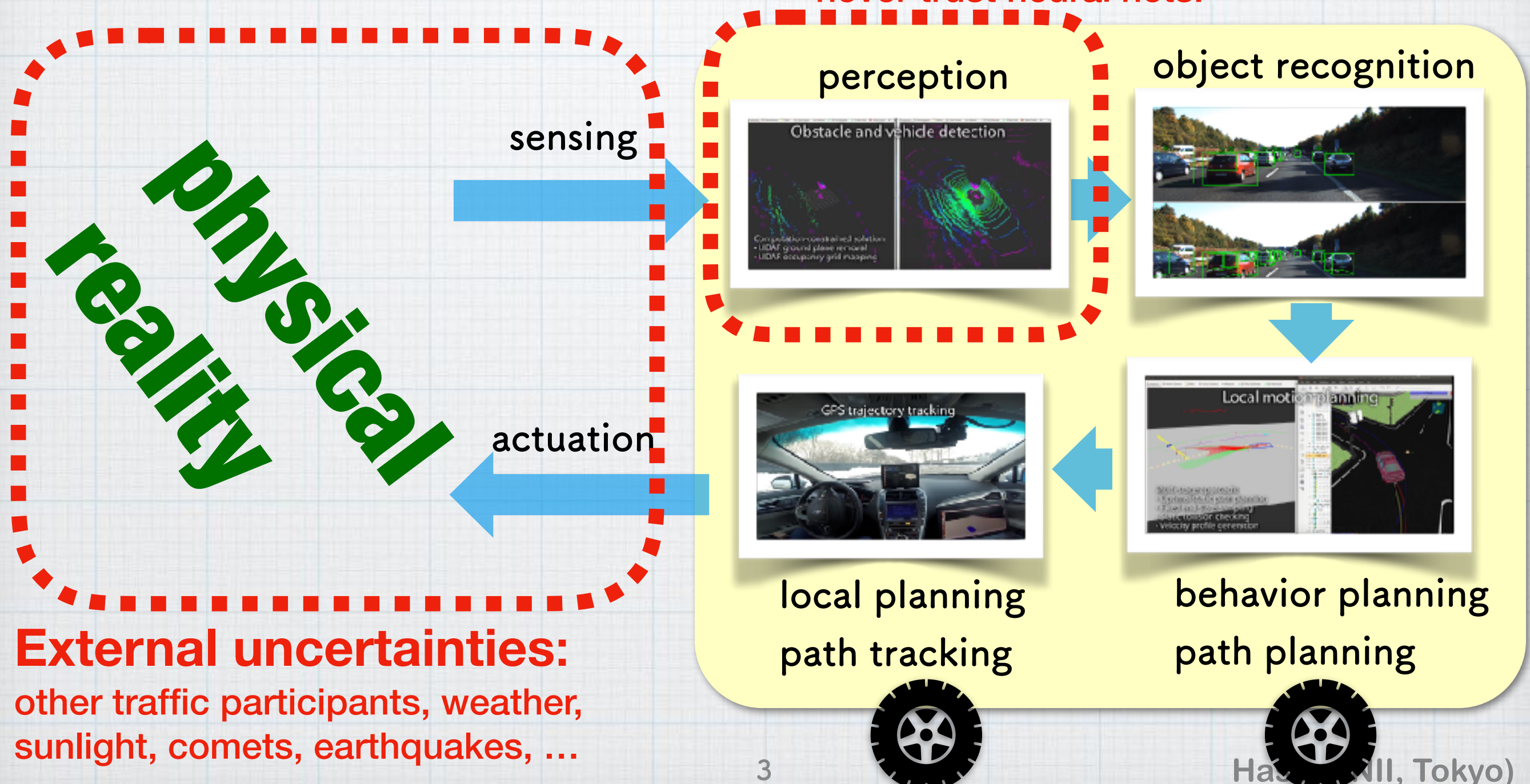
- \* Cyber-physical systems under uncertainties
- \* **Formal methods** and **testing** for CPS
- \* Hybrid system falsification
  - \* Logical connectives [CAV'19]
  - \* Causality in time [EMSOFT'18]
  - \* ... as demonstration of combining **logical** and **statistical**
- \* Other topics



# Uncertainties in Cyber-Physical Systems 2020

\* Take automated driving...

**Internal uncertainties:**  
never trust neural nets!



**External uncertainties:**  
other traffic participants, weather, sunlight, comets, earthquakes, ...

**You walk in the dark,  
guided by an apparatus**



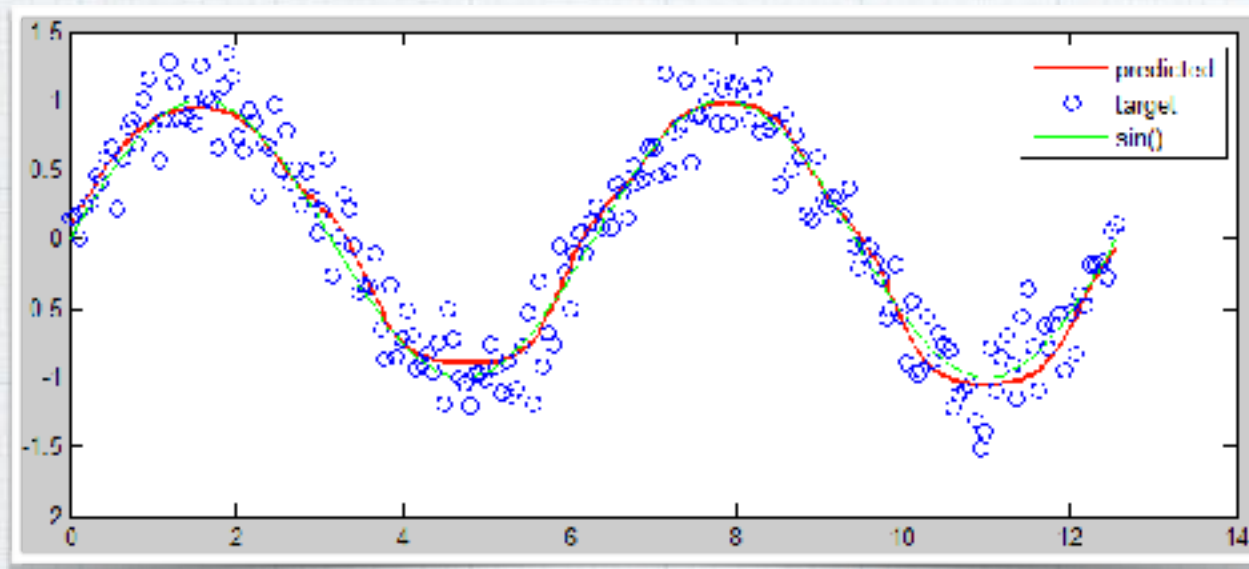


**... which itself is a black box!**

# Never Trust Statistical AI

- \* They approximate.  
You never know when they are completely precise

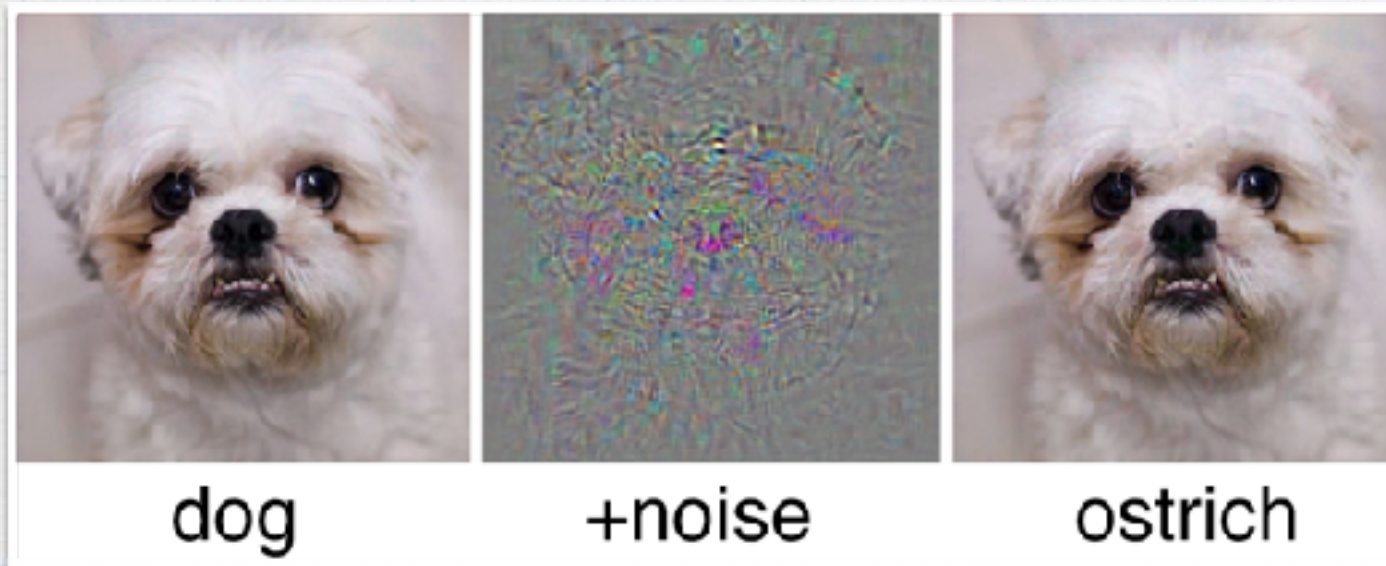
Ground truth  
→ noisy data  
→ approximation by regression



Approximating the sine curve by NN

<https://i.stack.imgur.com/l8qjP.png>

<https://stackoverflow.com/questions/1565115/unable-to-approximate-the-sine-function-using-a-neural-network>



Adversarial example

<https://i.stack.imgur.com/l8qjP.png>

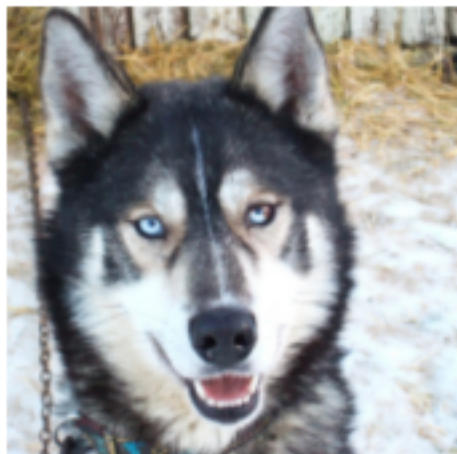
<https://stackoverflow.com/questions/1565115/unable-to-approximate-the-sine-function-using-a-neural-network>



# Never Trust Statistical AI

\* Question your “ground truth”

Ground truth  
→ noisy data  
→ approximation  
by regression



(a) Husky classified as wolf



(b) Explanation

Figure 11: Raw data and explanation of a bad model’s prediction in the “Husky vs Wolf” task.

	Before	After
Trusted the bad model	10 out of 27	3 out of 27
Snow as a potential feature	12 out of 27	25 out of 27

Table 2: “Husky vs Wolf” experiment results.

Husky vs Wolf? Snow vs No Snow?

<https://arxiv.org/pdf/1602.04938.pdf>



# ML Component as “Super-Sharp but Not-Totally-Reliable Colleague”



- \* **Often super sharp**  
“Wonderful idea! How did you get it?”
- \* **... for no clear reason**  
“It just came down to me...”
- \* **... and not always so**  
“How come you made this stupid mistake?”
- \* **Great to have one in a team;  
you don’t want all to be like that**



# ML Component in Safety-Critical Cyber-Physical Systems



- \* Take its opinion with a pinch of salt
- \* Suggestion, instead of decision
- Extreme example: proof check
- \* System-level assurance



# Statistical AI vs Formal Deduction



$$\frac{A \quad A \supset B}{B}$$

Statistical AI		Formal Deduction
Allow noisy data	Errors in input	Axioms are absolute
No guarantee	Correctness of concl.	Logical guarantee (mathematical proofs)
<p style="text-align: center;"><b>High</b></p> Automatic pattern discovery from data	Scalability	<p style="text-align: center;"><b>Low</b></p> Manual preparation of axioms
<p style="text-align: center;"><b>Low</b></p> Decision making by "weights"	Explainability	<p style="text-align: center;"><b>High</b></p> Explicit deduction processes as proofs



# Questions

- \* **Quality assurance of CPS**  
under **internal** (ML) and **external** (env.) **uncertainties?**
- \* **How to combine the two worlds?**

statistical  
continuous  
noisy  
data-based  
bottom-up

logical  
discrete  
rigorous  
rule-based  
top-down



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- \* Hybrid system falsification
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  - \* Causality in time [EMSOFT'18]
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- \* Other topics



# Formal Methods

- \* The general body of mathematical techniques, originally in **software science**
- \* Goals:

## Successes in software/ ICT

- \* IC design (Intel, ...)
- \* device drivers (Microsoft)
- \* light-weight FM (Facebook)
- \* ...

## Verification

- \* Input:
  - \* a system model  $\mathcal{M}$
  - \* a specification  $\varphi$
- \* Output: if  $\mathcal{M} \models \varphi$  or not
  - \* w/ a **proof**, if yes
  - \* w/ a **counterexample**,

## Synthesis

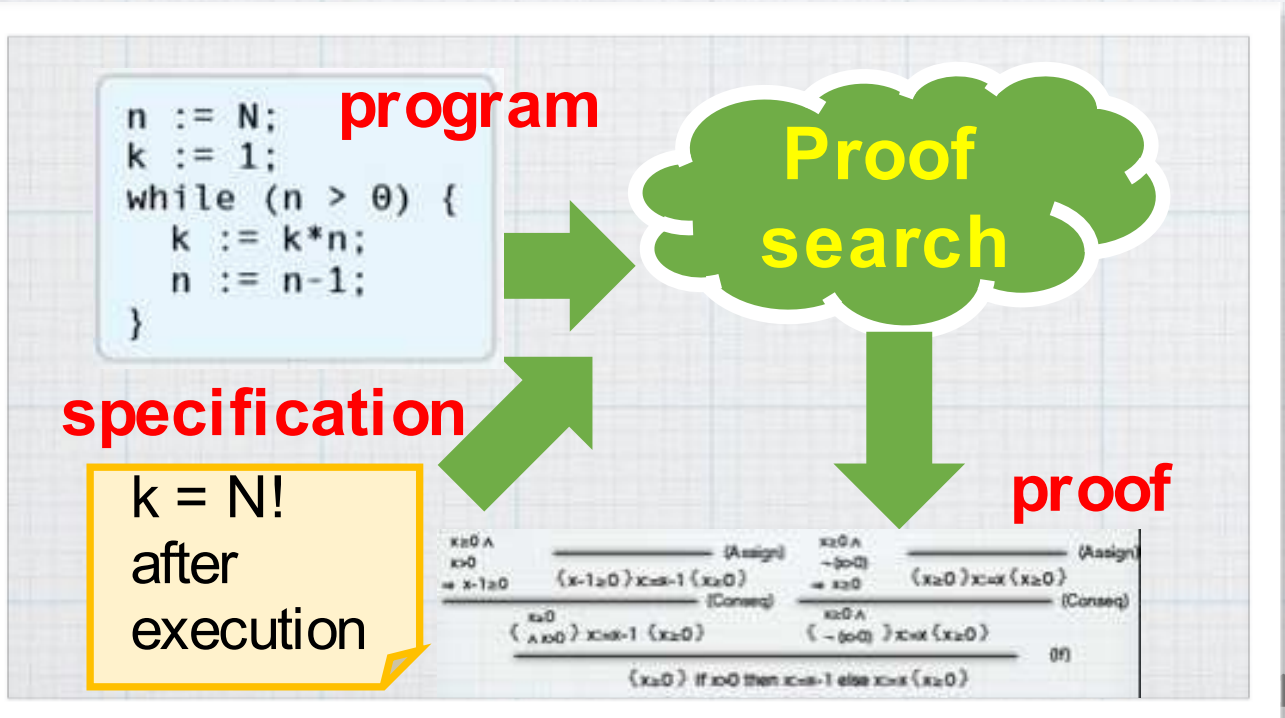
- \* Input:
  - \* a specification  $\varphi$
- \* Output: a system  $\mathcal{M}$  such that  $\mathcal{M} \models \varphi$ 
  - \* or: a parameter of a given (partial)

## Specification

- Expressing a property desired in a **formal language**
- \* machine-representable
  - \* basis for verif. & synthesis

# Verification by Theorem Proving

- \* Example: program verification by Hoare logic
  - \* Proof search can be automatic or interactive (proof assistants like Coq, Agda, PVS, Isabelle, ...)
  - \* A mathematical proof guarantees correctness
    - \* Unlike testing (empirical guarantee)
  - \* Can cover infinitely many inputs/environments (in principle)
    - \* Write “let  $i$  be the input” in the proof!



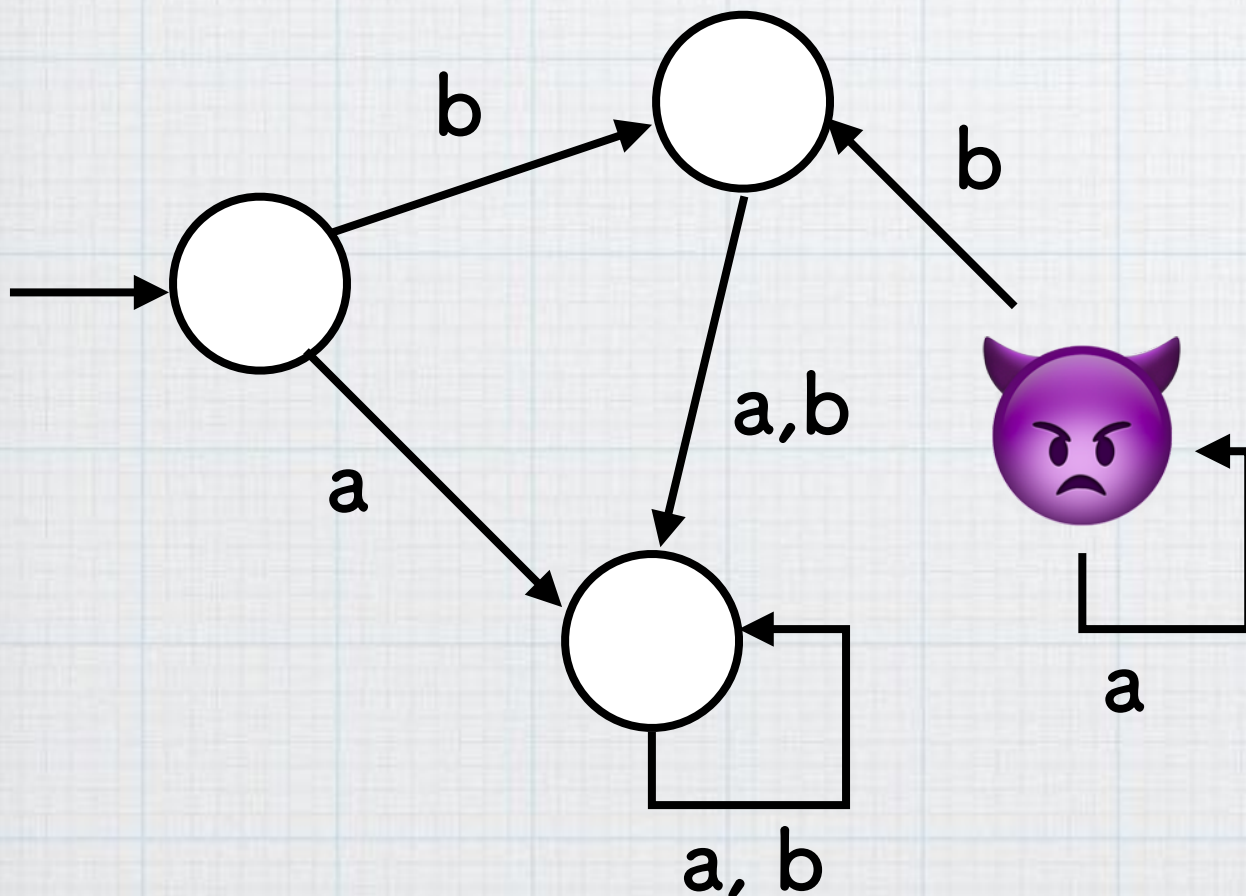
```
Theorem forall_exists : (forall P : Set->Prop,
  (forall x, ~(P x)) -> ~(exists x, P x)).
Proof.
  intros P.
  intros forall_x_not_Px.
  unfold not.
  intros exists_x_Px.
  destruct exists_x_Px as [ witness proof_of_Pwitness].
  pose (not_Pwitness := forall_x_not_Px witness).
  unfold not in not_Pwitness.
  pose (proof_of_False := not_Pwitness proof_of_Pwitness).
  case proof_of_False.
Qed.
```

**A Coq proof of  $\forall x. \neg P(x) \rightarrow \neg \exists x. P(x)$**



# Verification by Model Checking

- \* “Automated proof” by algorithms for automata
  - \* Proofs reduced to **graph reachability**
- \* An automaton is **finite** → “automated proofs” by enumeration
- \* Example: Check if we never reach 🍆 under any input word (\*)



- \* (**Wrong**)  
Check the spec (\*) for **all** input words  
(How many words? Infinite!!)
- \* (**Correct**)  
Compute the **reachable set**  
(graph exploration, saturates within finite time), and check if 🍆 is not there



# History of Formal Methods

Software gets bigger

network, distributed, concurrent

meet physical dynamics

rise of statistical ML

- \* **1970's** Initial studies on software quality assurance by formal methods (**software verification**).  
Theorem proving, model checking
- \* **1990's** **Software verification** put to use, realistic tools  
Theorem proving: Isabelle, Coq, PVS, ...  
model checking: SPIN, SMV/NuSMV, mCRL2, PRISM, Uppaal, ...
- \* **2006** **Cyber-physical systems** as a new application domain.  
Software verification + control theory
- \* **2016** **Machine learning systems** as a new application domain.  
Formal/logical deduction + statistical inference



# CPS Research, So Far (the V&V Aspect)



**CPS**  
(esp. hybrid systems)

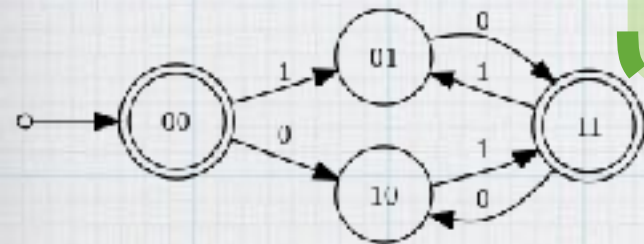
Analysis

Formal Methods

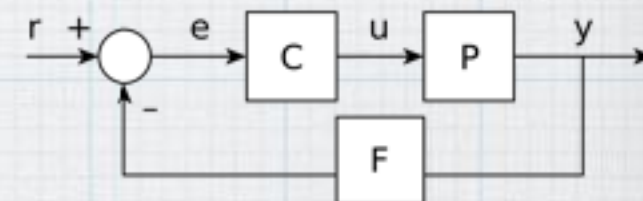
Control Theory

Collaboration

$$\square(p \Rightarrow \diamond q)$$



$$x' = f(x, u)$$



- \* US and Europe have had systematic efforts
  - \* US: **CPS Initiative** of NSF (2006-)
  - \* Europe: **Quantitative extension** of formal methods (probability, time, ...)
- \* Need to catch up...?
  - They haven't necessarily been so successful in **real-world applications**



# CPS Research, So Far (the V&V Aspect)



**CPS**  
(esp. hybrid systems)

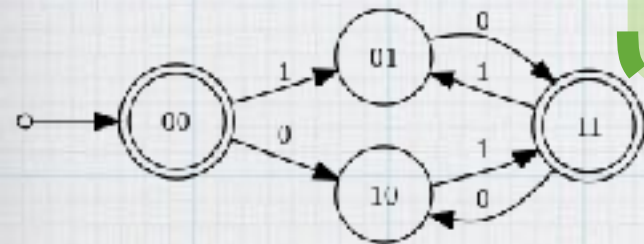
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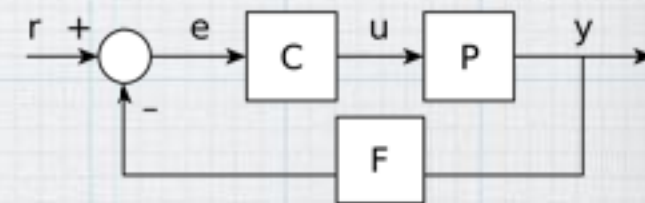
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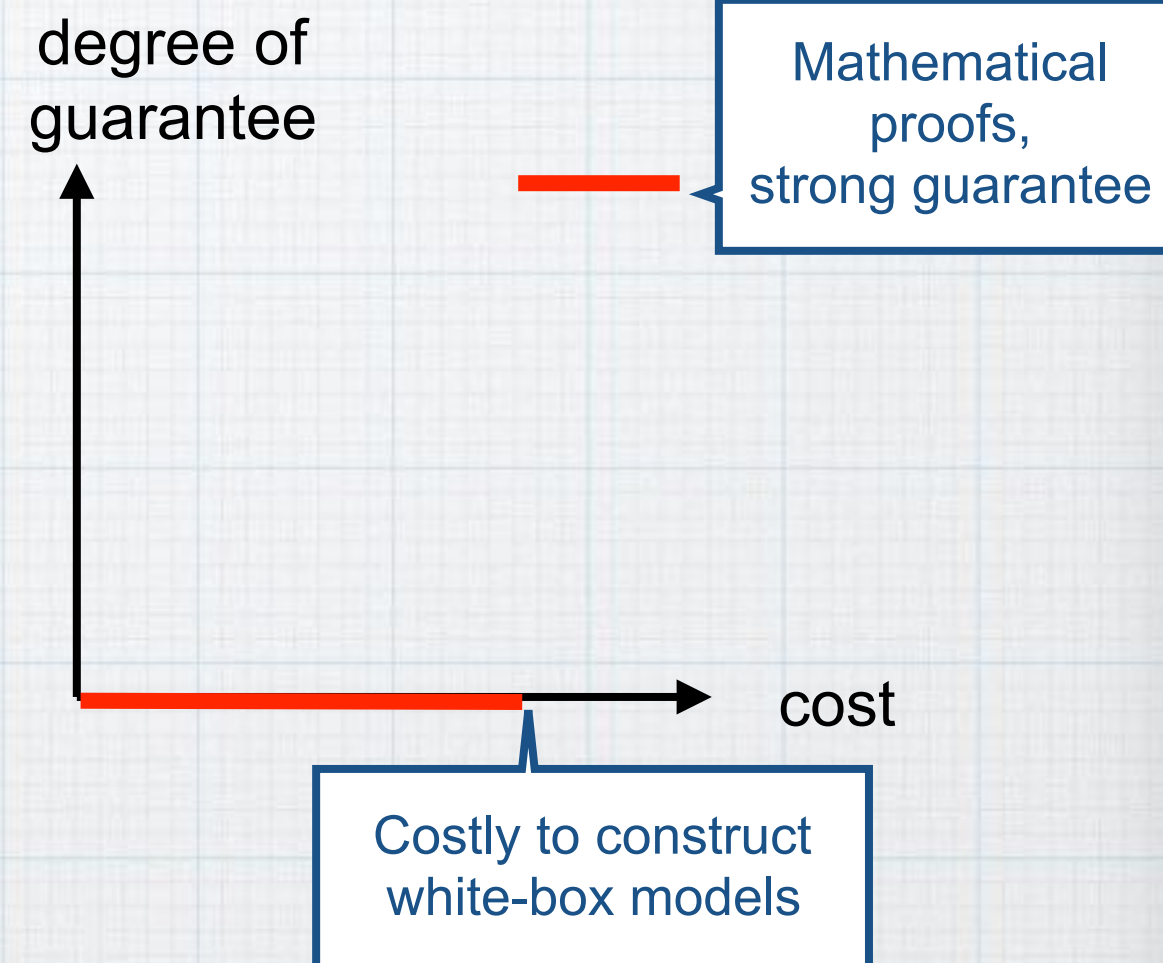


- \* Problem: **scalability**, esp. for real-world CPSs
  - \* Require **complete understanding** of a **white-box model**
  - \* Insist on being **absolutely sound** and **correct**
  - \* Little **tolerance to uncertainty and noise**
    - \* Big problem too in presence of statistical machine learning



# Towards Formal Methods That Are Down-Scalable

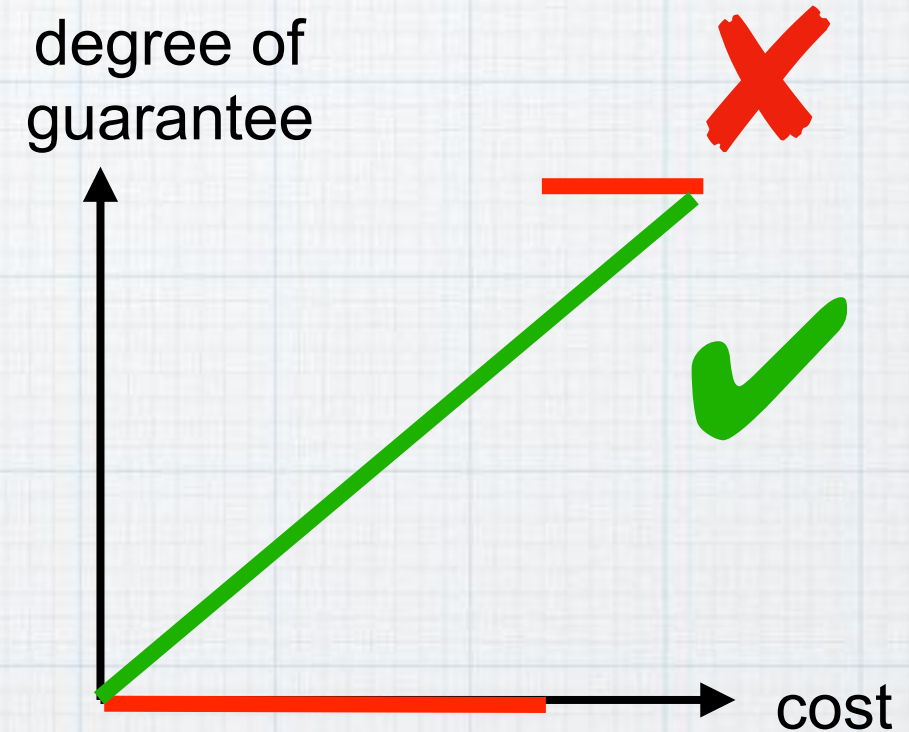
- \* Many FM methods (esp. for verification) are not **down-scalable**
  - \* They demand **white-box models**. Need formal models of all system components
  - \* They also require **totally new design processes**
  - \* → huge cost before getting non-zero benefit (quality assurance)
- \* Example applications to CPS: airplanes (Airbus), space (NASA), ...
  - \* Failure is so expensive → worth verification efforts
  - \* Still takes decades
  - \* Integrating continuous dynamics is hard → They focus on software





# Towards Formal Methods That Are Down-Scalable

- \* For real-world applications (esp. automotive domain), we need **down-scalability**
- \* Even if we can only afford **half the cost**,
- \* degree of guarantee does not become **zero**, but **half**

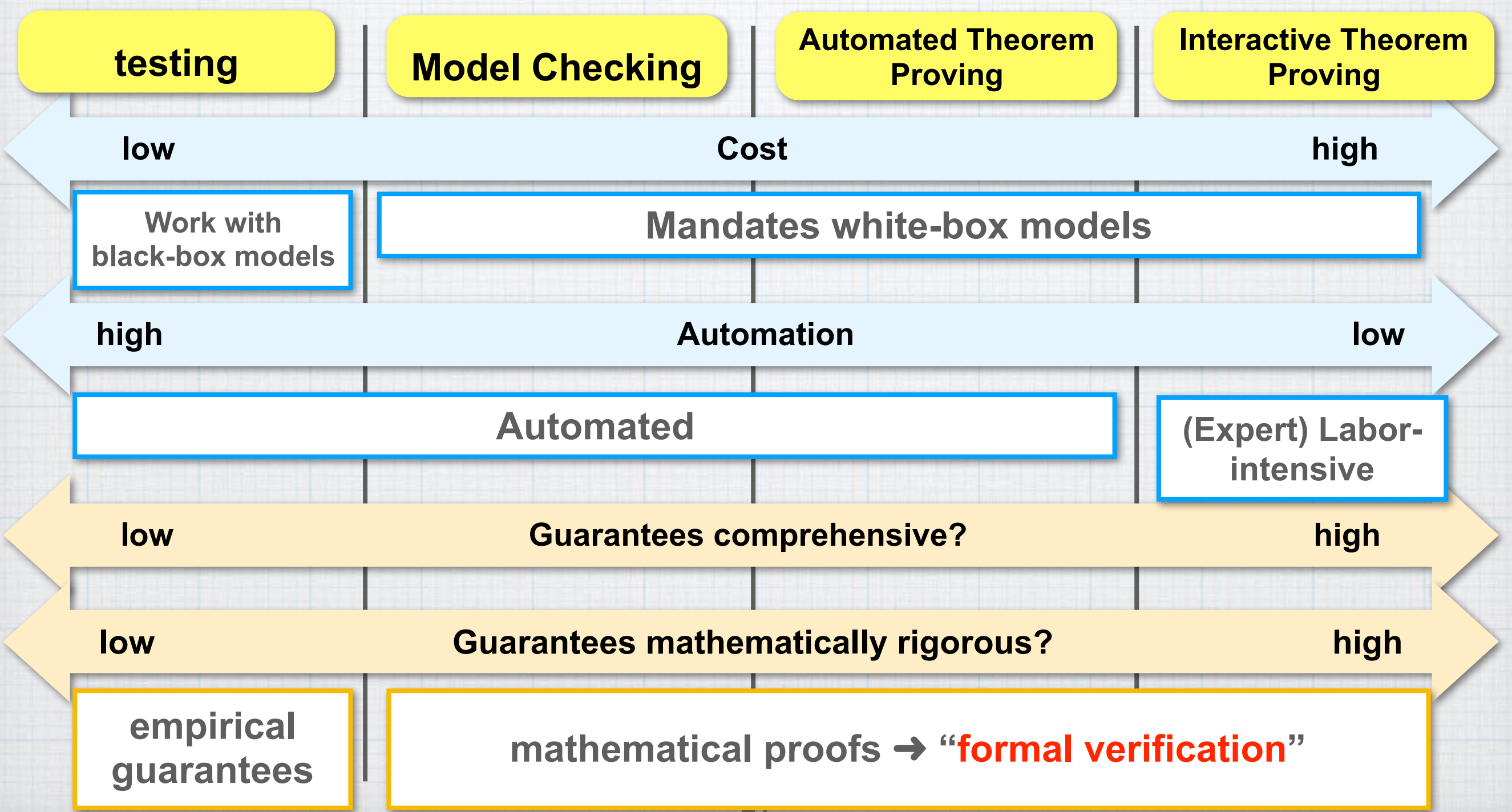






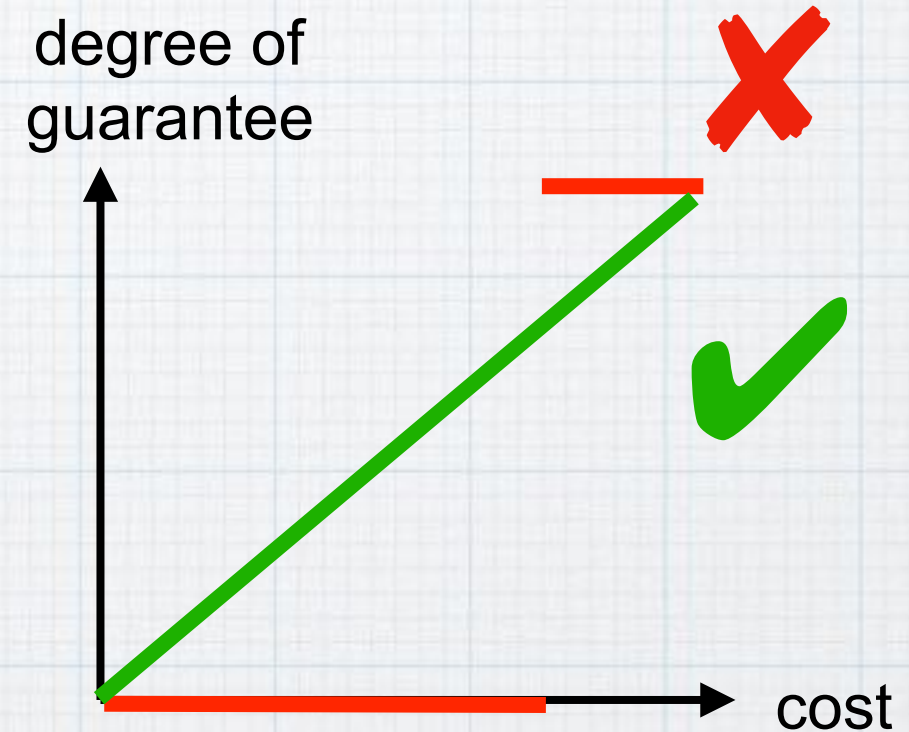
# Formal Methods: Spectrum

## Formal methods



# Towards Formal Methods That Are Down-Scalable

- \* Real-world applications (esp. automotive domain), need **down-scalability**
  - \* Even if we can only afford **half the cost**,
  - \* degree of guarantee does not become **zero**, but **half**
- \* Our efforts at ERATO MMSD
  - \* Combine **testing** and **formal verification**.
    - \* Search-based testing
    - \* monitoring
    - \* contract-based verification







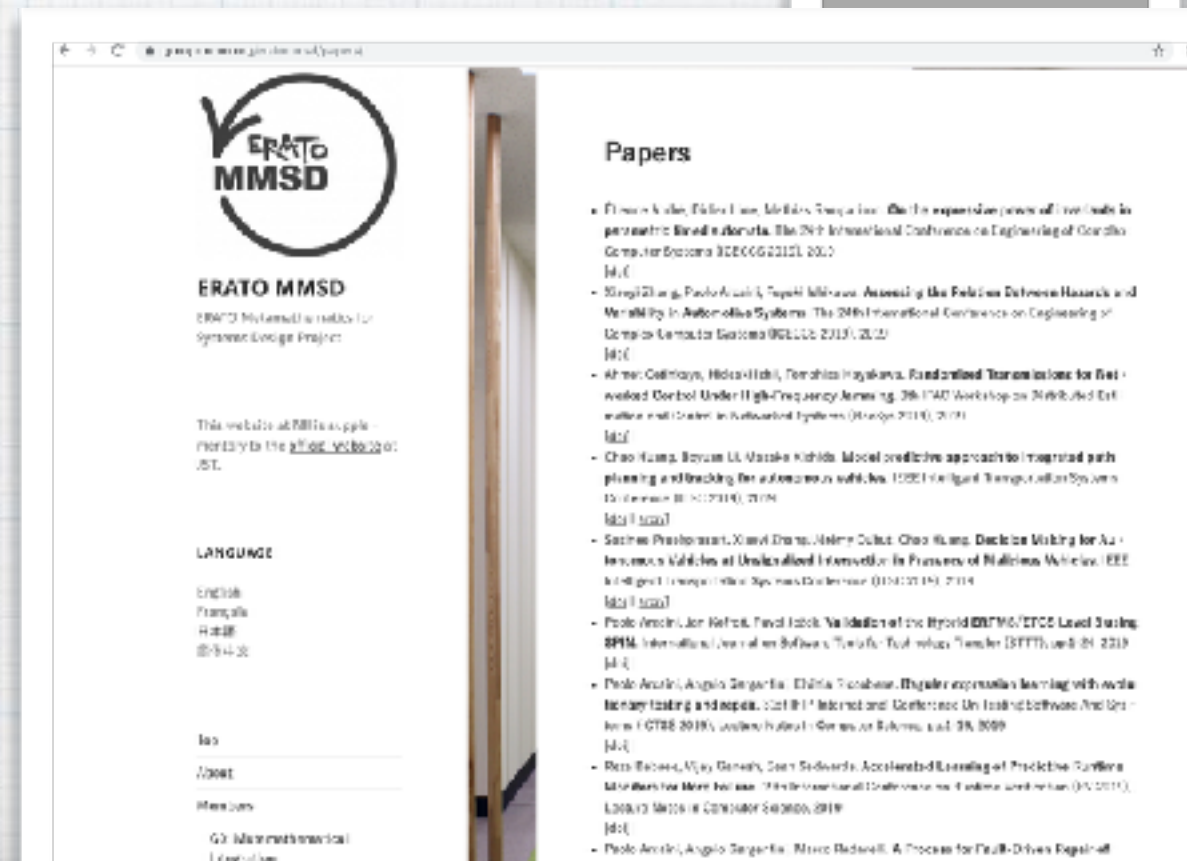
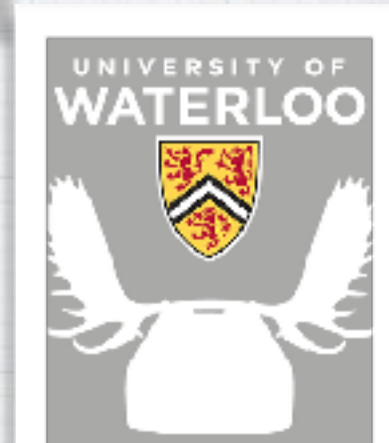
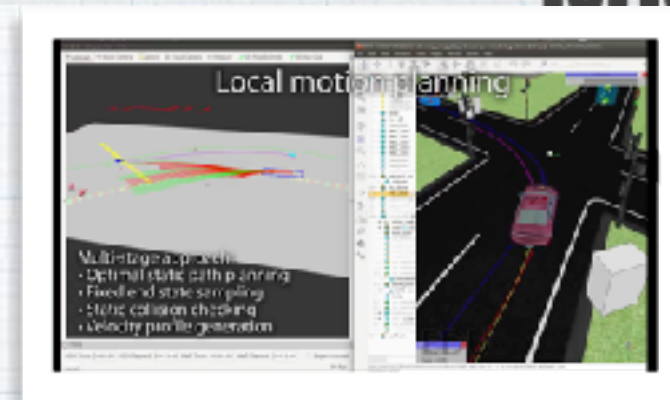
# On ERATO MMSD

\* JST ERATO Project, 2016/10-2022/03  
<https://group-mmm.org/eratommsd>

\* Our goal:  
 formal methods for **cyber-physical systems (CPS)**

- \* Extend **formal methods**, from software to CPS
- \* Safety, reliability, V&V (Verification & Validation).  
 “**Check if a system behaves as expected**”
- \* Emphasizing **industry collaboration**, also for scientific inspirations
- \* **Automated driving** as a strategic target domain.  
 Collaboration with U Waterloo:  
[www.autonomoose.net](http://www.autonomoose.net)

- \* Our team:
  - \* 28 researchers, > 20 students (as of 2019/09)
  - \* **International** and **scientifically diverse**





# Our Organization

International and multi-disciplinary. “creative chaos”



Kyoto U IS Site:  
**Advanced Deductive Verification**  
Leader:  
Kohei Suenaga

Kyoto U RIMS Site:  
**Categorical Infrastructure**  
Leader:  
Masahito Hasegawa

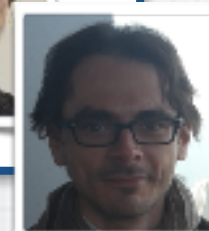
Group 0 @ NII:  
**Metatheoretical Integration**  
Leader: Shin-ya Katsumata

Topics:  
Programming Languages,  
Formal Semantics,  
Categorical Models,  
Mathematical Logic, ...



Group 3 @ NII:  
**Formal Methods and Intelligence**

Leader: Fuyuki Ishikawa  
Subleader: Paolo Arcaini  
Topics:  
Software Engineering,  
Formal Modeling,  
Testing, Safe & Explainable AI



Kyushu U Site:  
**Optimization for CPS V&V**  
Leader:  
Hayato Waki

Osaka U Site:  
**Control Theory for CPS**  
Leader:  
Toshimitsu Ushio

Group 1 @ NII:  
**Heterogeneous Formal Methods**

Leader: Ichiro Hasuo  
Subleader: Masako Kishida  
Topics:  
Automata Theory,  
Control Theory,  
Formal Verification,  
Proof Assistants,  
Automated Deduction,  
Runtime Verification



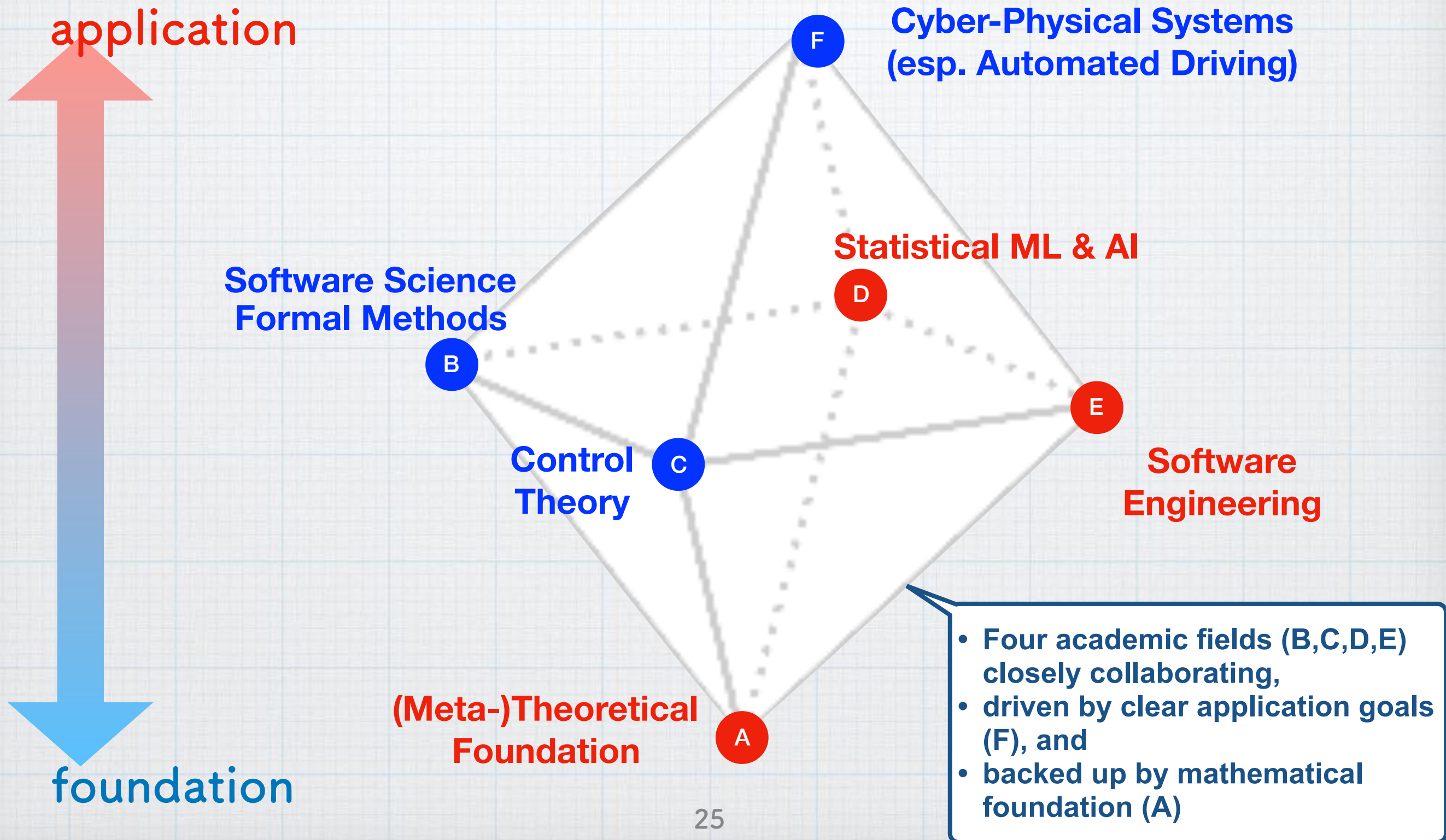
Group 2 @ U Waterloo:  
**Formal Methods in Industry**  
Leader: Krzysztof Czarnecki

Topics:  
Automated Driving, Software Engineering,  
Machine Learning





# Interdisciplinary Efforts towards CPS: Six Scientific Fields



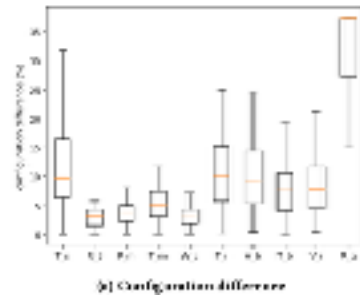


# Our Techniques in a Spectrum

testing

## Fault localization, stability analysis

- “Which part of the system is responsible for this failure?”
- [Zhang+, ICECCS’19] [Lee+, GECCO’19]



## Search-based testing

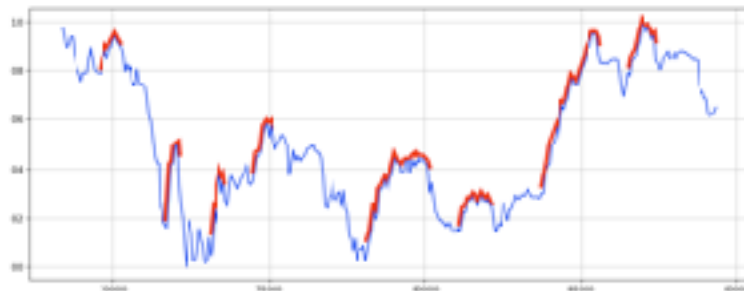
(aka hybrid system falsification)

- Active search for counterexamples
- Incompletely but efficiently, by **reinforcement learning**
- [Zhang+, CAV’19] [Zhang+, EMSOFT’18]



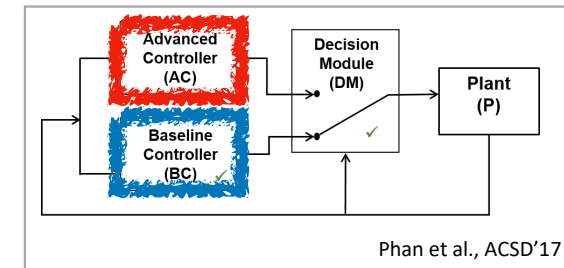
## Monitoring, runtime verification

- “Warn me when something is wrong”
- “Extract interesting parts out of this 10 GB log”
- Pattern matching via **timed automata**
- [Waga+, CAV’19] [Waga+, EMSOFT’19]



## Contract-based verification, safety architecture

- Formal verification in presence of black-box models
- Failover strategy + switching, monitoring
- Incremental modeling by Event-B, fuzzy logic, ...



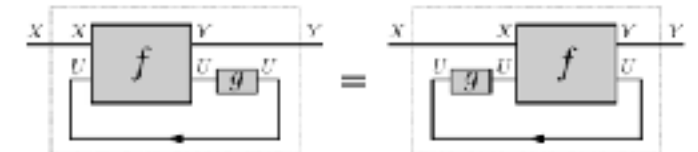
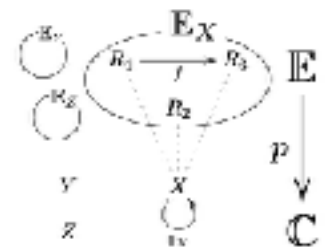
## Quantitative verification

- “Termination probability for this probabilistic program?” “How long will it take?”
- Automated analysis by **martingale synthesis**
- [Takisaka+, ATVA’18] [Kura+, TACAS’19]

$$V(x) = \max_{a \in \Gamma(x)} \{F(x, a) + \beta V(T(x, a))\}$$

## Categorical foundations

- “Uniform framework for bisimilarity and bisimulation distance?”
- “Structural justification of backpropagation for RNN?”
- [Komoroda+, LICS’19]
- [Sprunger+, LICS’19] ...



verification



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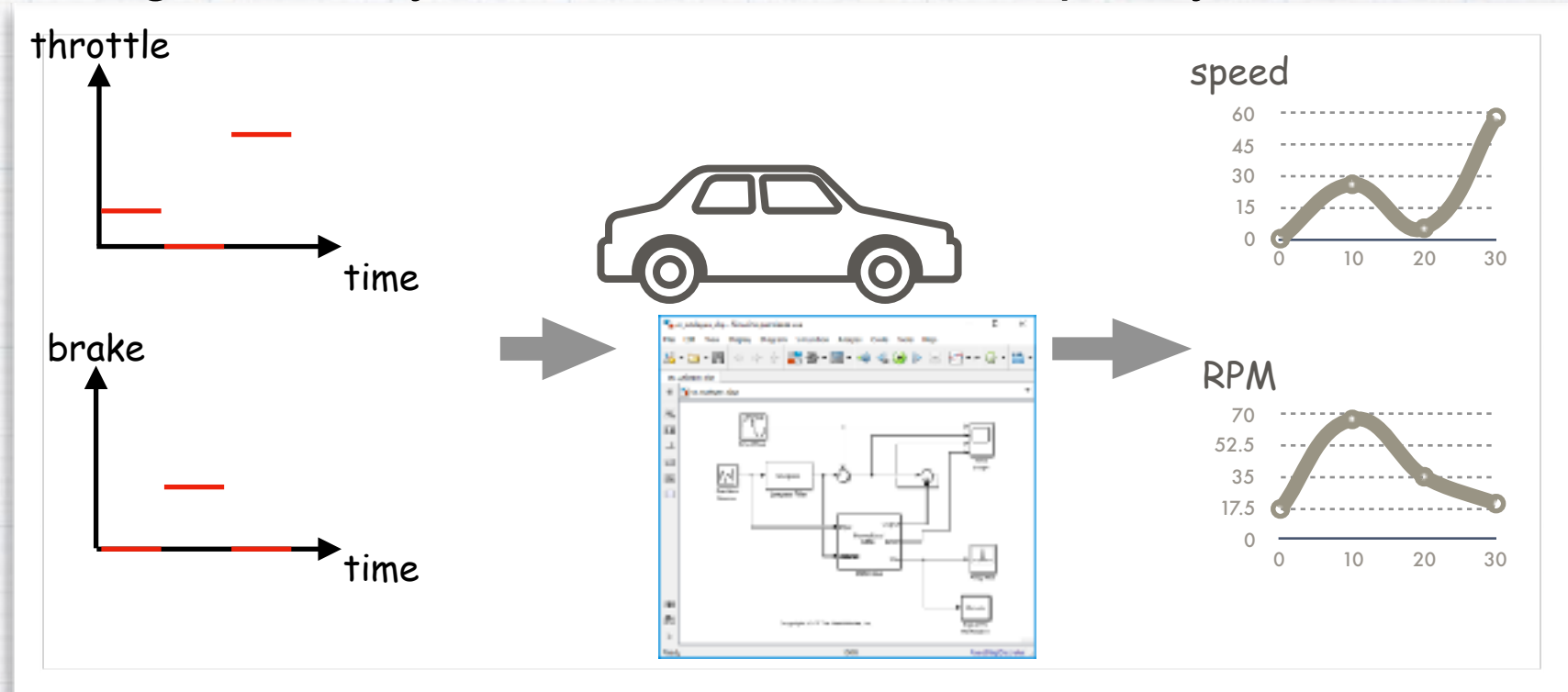


# Hybrid System Falsification

[Fainekos & Pappas, TCS'09]

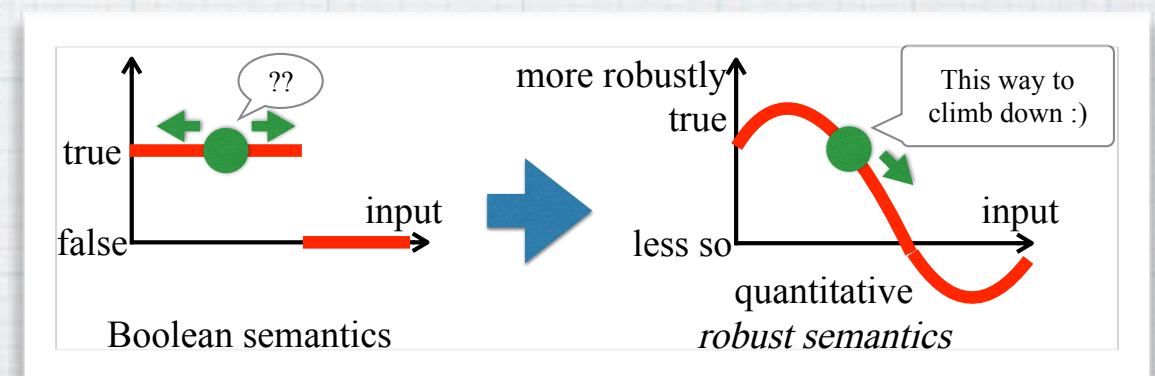
\* **Black-box**, search-based testing. Actively search for erroneous input by:

- \* Try an input signal
- \* Observe the system's behavior
- \* Choose the next input that is likely to be erroneous



\* [Fainekos & Pappas, TCS'09]  
 A **reinforcement learning problem**,  
 by moving

- \* from the **Boolean** semantics (erroneous or not)
- \* to **quantitative** “robust semantics” (how far from being erroneous)





# Discrete Structures in Continuous Learning & Optimization

- \* In hybrid system falsification (and statistical machine learning in general), efficiency comes mainly from **gradient descent (which is continuous)**
- \* **Question:** can we also exploit **discrete structures** for efficiency and explainability?
- \* Example: hierarchical optimization scheme [Zhang+, CAV'19]

**Search-based testing (aka hybrid system falsification)**

- Active search for counterexamples
- Incompletely but efficiently, by **reinforcement learning**
- [Zhang+, CAV'19] [Zhang+, EMSOFT'18]



- \* Given: a black-box model  $M$  and a specification  $\square_I(\varphi_1 \vee \varphi_2)$
- \* Goal: input  $i$  s.t.  $M(i)$  violates the spec

**Multi-armed bandit** over subformulas  $\varphi_1$  and  $\varphi_2$

“made this much progress for  $\varphi_i$ ”

Feed search results back

Discrete Optim.

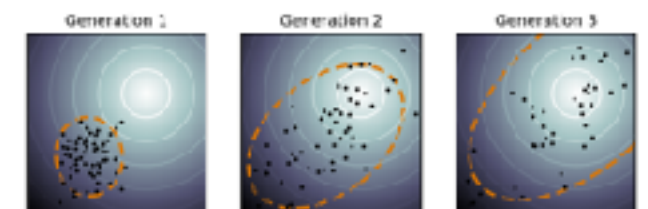
Restrict search domain

Continuous Optim.

Which formula ( $\varphi_1$  or  $\varphi_2$ ) to try to falsify

Stochastic gradient descent (such as CMA-ES)

for input that violates  $\varphi_i$





# Multi-armed Bandits for Boolean Connectives in Hybrid System Falsification

Zhenya Zhang, Ichiro Hasuo, Paolo Arcaini

National Institute of Informatics, Tokyo, Japan

The Graduate University for Advanced Studies (SOKENDAI), Hayama, Japan

31st International Conference on Computer-Aided Verification

July 16, 2019



# Falsification

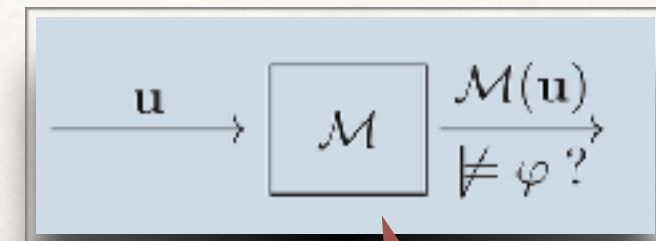
- Falsification problem:

$\mathcal{M}$  : black-box model

$\mathbf{u}$  : input signal (piecewise constant)

$\mathcal{M}(\mathbf{u})$  : output signal

$\varphi$  : specification in Temporal Logic



hybrid system

- Goal: find an input signal  $\mathbf{u}$  s.t.  $\mathcal{M}(\mathbf{u}) \not\models \varphi$

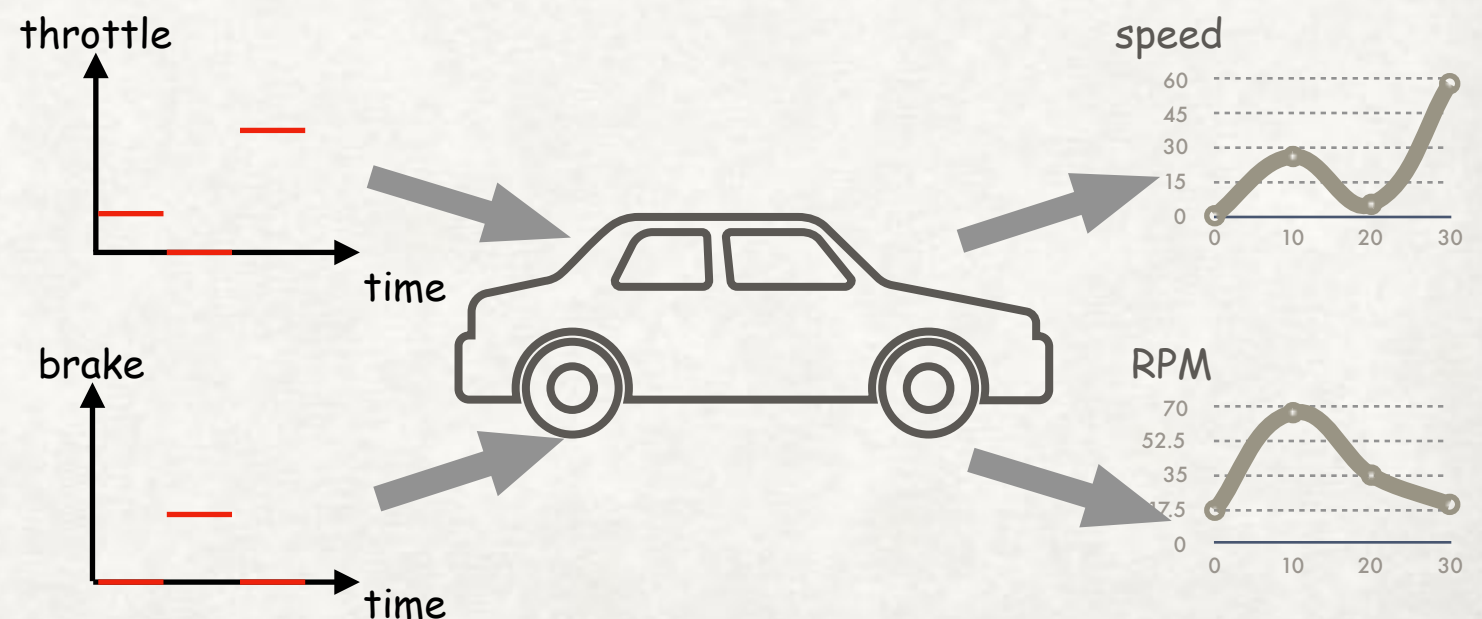
## Example:

$\square_{[0,30]} (speed < 120)$

Always

Bounded-time

Proposition

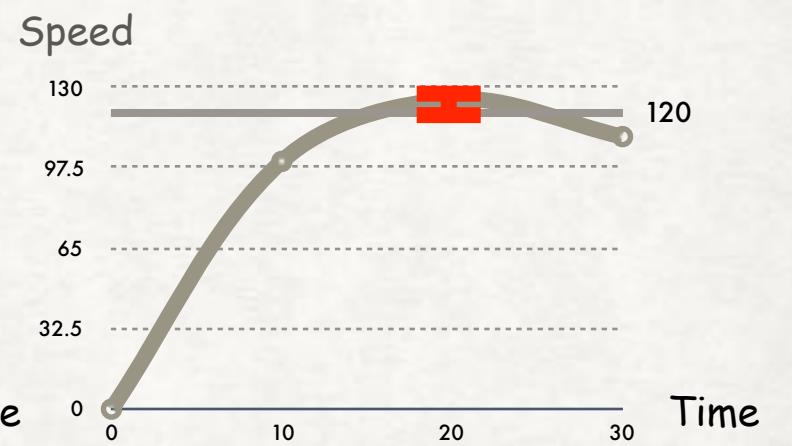
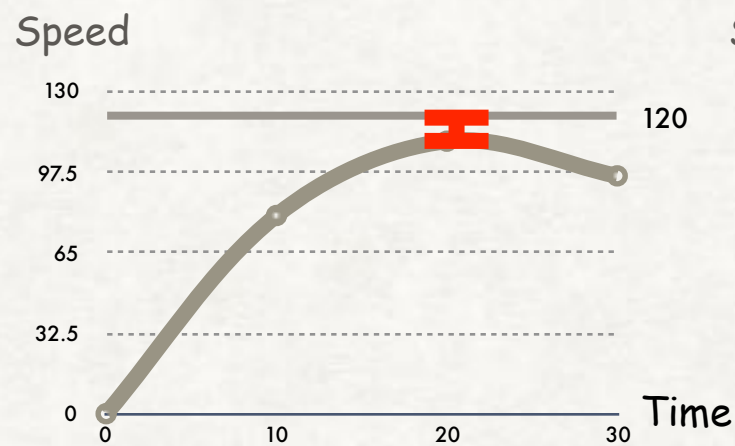
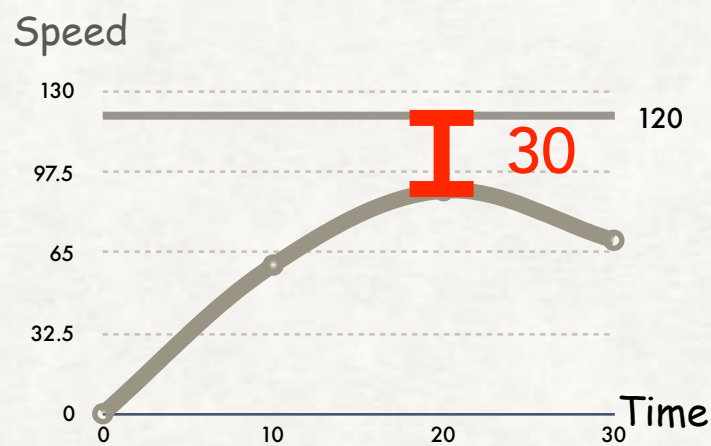


# STL robustness

- Quantitative robustness semantics of STL [Donze, Maler FORMATS'10]

e.g.,  $\varphi = \square_{[0,30]}(speed < 120)$

Output  
Signals



Boolean  
Satisfaction

True

Boolean

False

Quantitative  
Robustness

30

Real number

10

-5



# Hill-climbing optimization

- falsification => **optimization**

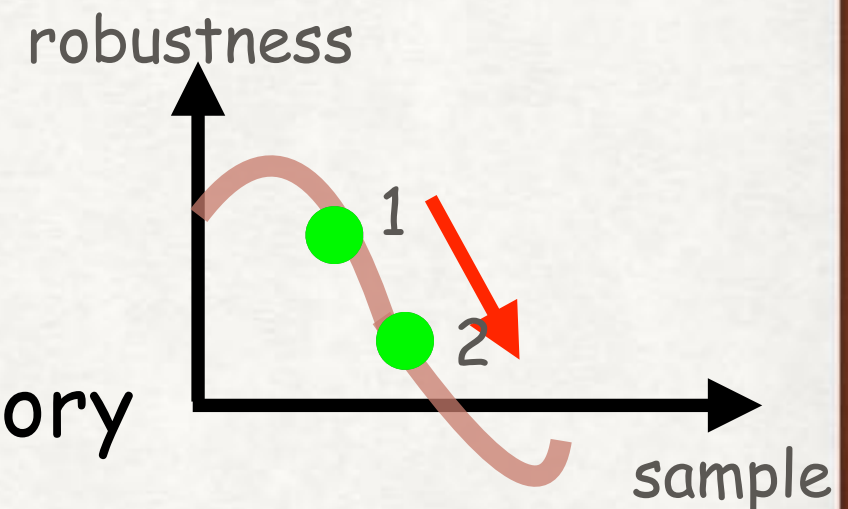
robustness

- Objective function:  $[\mathcal{M}(\mathbf{u}), \varphi]$
- Goal:  $\min [\mathcal{M}(\mathbf{u}), \varphi]$
- $[\mathcal{M}(\mathbf{u}), \varphi] < 0 \rightarrow$  done!

- “Hill-climbing” optimization algorithms

- Decide the next sample based on history
- More intelligent than random sampling
- Tools: Breach [Donze CAV'10] (CMA-ES, NM, etc.)

S-TaLiRo [Annapureddy et al. TACAS'11] (SA etc.)



# Motivating example

- Scale problem

- e.g.,  $\phi \equiv \square_{[0,30]}(\text{gear} = 3 \rightarrow \text{speed} > 20)$



- $\phi \equiv \square_I(\varphi_1 \vee \varphi_2)$  where  $\varphi_1 \equiv \neg(\text{gear} = 3)$  and  $\varphi_2 \equiv (\text{speed} > 20)$

- STL robustness semantics [Donze, Maler FORMATS'10]

$$\llbracket \mathbf{w}, f(x_1, \dots, x_n) > 0 \rrbracket := f(\mathbf{w}(0)(x_1), \dots, \mathbf{w}(0)(x_n))$$

$$\llbracket \mathbf{w}, \perp \rrbracket := -\infty \quad \llbracket \mathbf{w}, \neg\varphi \rrbracket := -\llbracket \mathbf{w}, \varphi \rrbracket$$

$$\llbracket \mathbf{w}, \varphi_1 \wedge \varphi_2 \rrbracket := \llbracket \mathbf{w}, \varphi_1 \rrbracket \cap \llbracket \mathbf{w}, \varphi_2 \rrbracket \quad \llbracket \mathbf{w}, \varphi_1 \vee \varphi_2 \rrbracket := \llbracket \mathbf{w}, \varphi_1 \rrbracket \sqcup \llbracket \mathbf{w}, \varphi_2 \rrbracket$$

$$\llbracket \mathbf{w}, \varphi_1 \mathcal{U}_I \varphi_2 \rrbracket := \bigsqcup_{t \in I \cap [0, T]} (\llbracket \mathbf{w}^t, \varphi_2 \rrbracket \cap \prod_{t' \in [0, t)} \llbracket \mathbf{w}^{t'}, \varphi_1 \rrbracket)$$

$\text{gear} \in \{1, 2, 3, 4\}$

$\text{speed} \in [0, 150]$

$\llbracket \mathcal{M}(\mathbf{u}), \varphi_1 \rrbracket \stackrel{?}{\sqcup} \llbracket \mathcal{M}(\mathbf{u}), \varphi_2 \rrbracket$



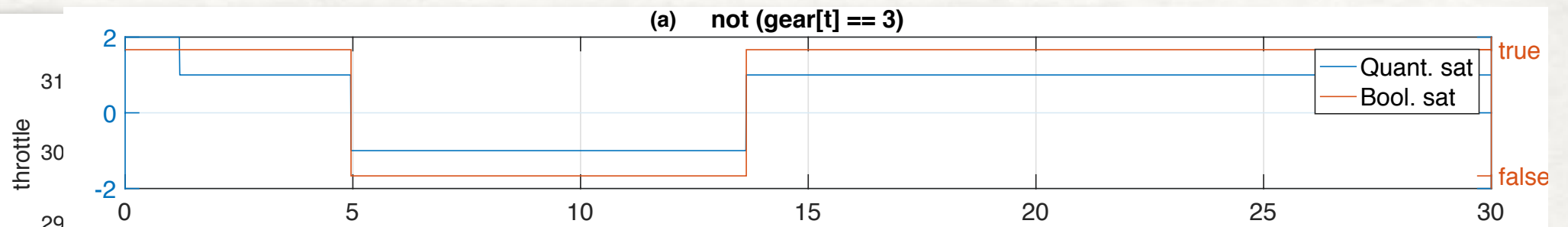
# Motivating example

$$\phi \equiv \square_{[0,30]} (gear = 3 \rightarrow speed > 20)$$

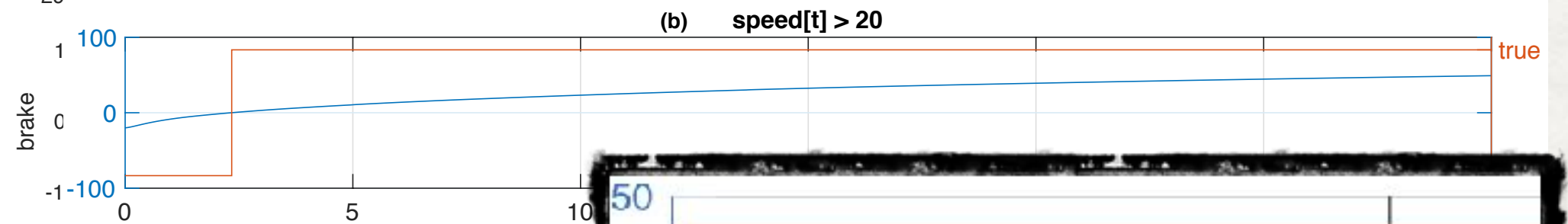


$$\phi \equiv \square_I (\varphi_1 \vee \varphi_2) \quad \varphi_1 \equiv \neg (gear = 3) \\ \varphi_2 \equiv (speed > 20)$$

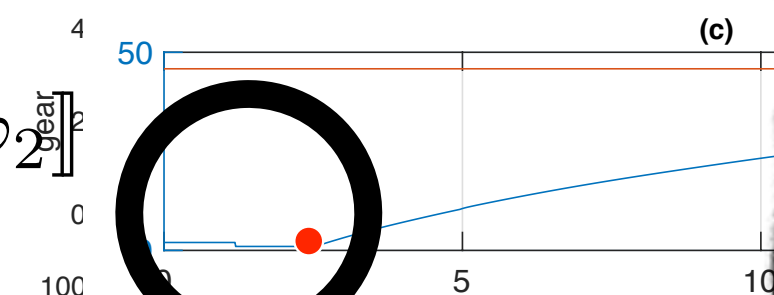
$$[\mathcal{M}(\mathbf{u}), \varphi_1]$$



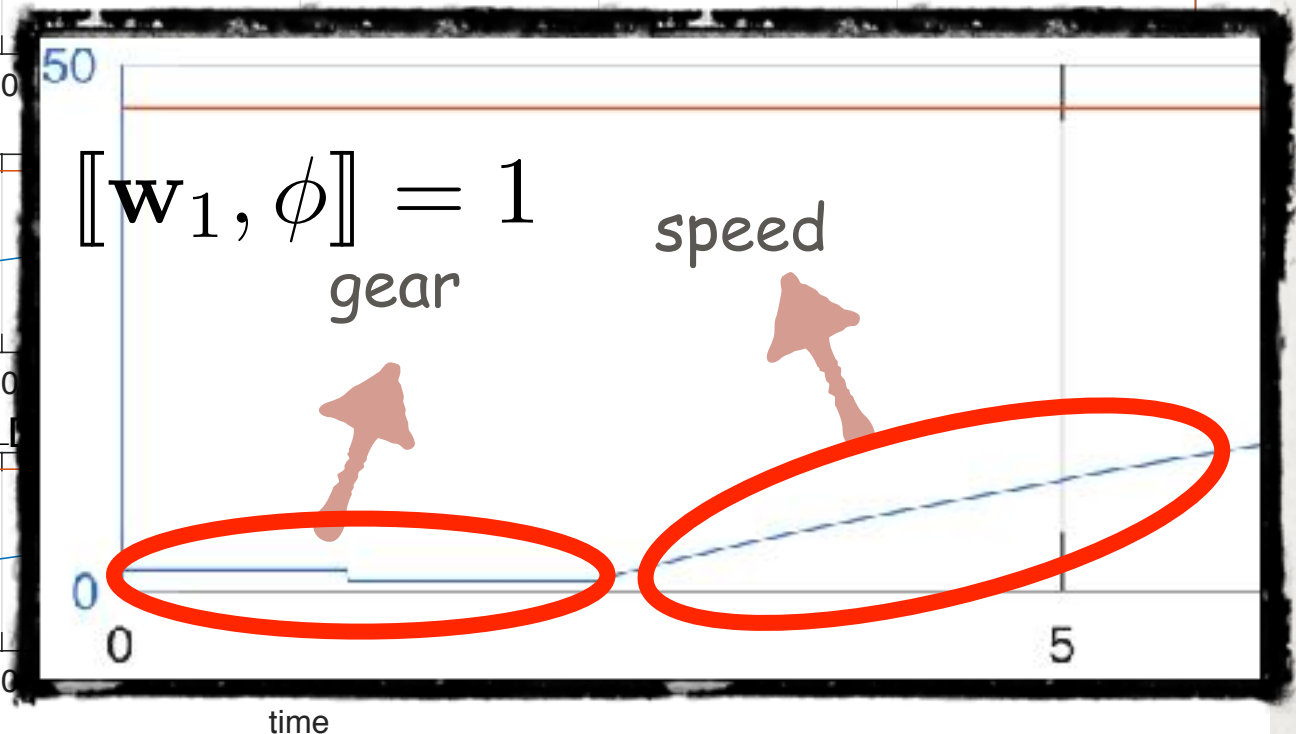
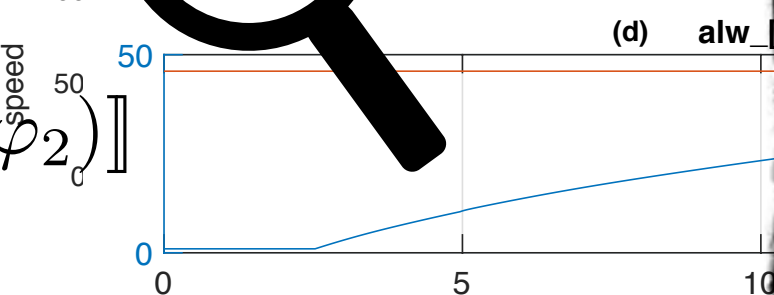
$$[\mathcal{M}(\mathbf{u}), \varphi_2]$$



$$[\mathcal{M}(\mathbf{u}), \varphi_1 \vee \varphi_2]$$



$$[\mathcal{M}(\mathbf{u}), \square_I (\varphi_1 \vee \varphi_2)]$$



# Motivating example

$$\phi \equiv \square_{[0,30]}(\text{gear} = 3 \rightarrow \text{speed} > 20)$$



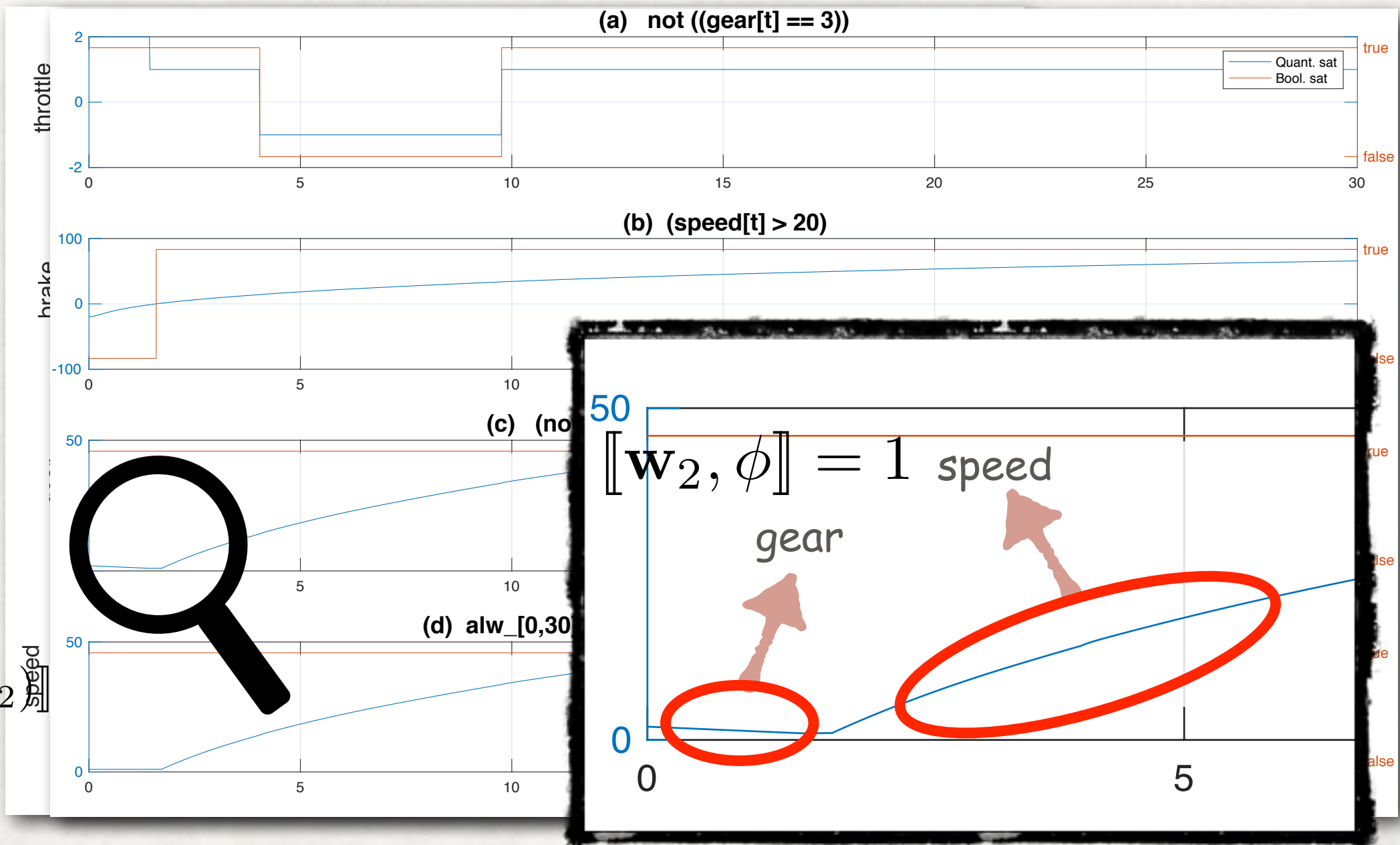
$$\phi \equiv \square_I(\varphi_1 \vee \varphi_2) \quad \varphi_1 \equiv \neg(\text{gear} = 3) \\ \varphi_2 \equiv (\text{speed} > 20)$$

$$[\mathcal{M}(\mathbf{u}), \varphi_1]$$

$$[\mathcal{M}(\mathbf{u}), \varphi_2]$$

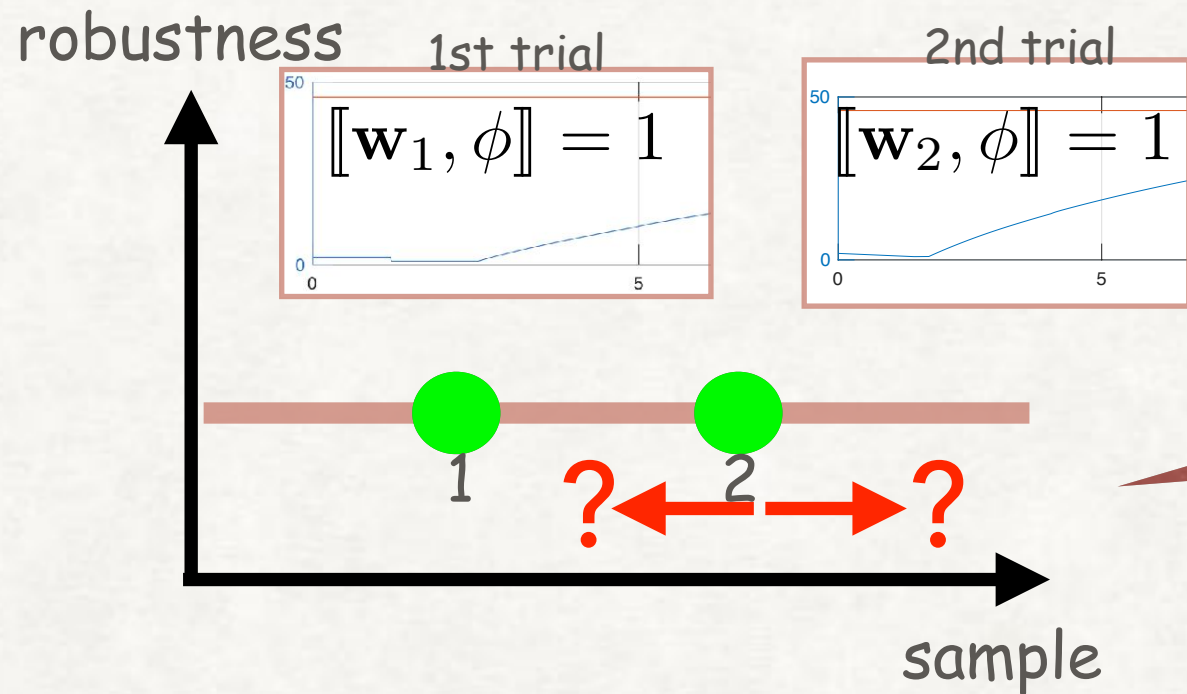
$$[\mathcal{M}(\mathbf{u}), \varphi_1 \vee \varphi_2]$$

$$[\mathcal{M}(\mathbf{u}), \square_I(\varphi_1 \vee \varphi_2)]$$





# Problem



Hill-climbing algorithm gets lost!

- Falsification of safety properties with boolean connectives
  - $\square_I(\varphi_1 \wedge \varphi_2)$ , conjunctive
  - $\square_I(\varphi_1 \vee \varphi_2)$ , disjunctive

# Multi-armed bandit

- Multi-armed Bandit problem
  - Gambler vs a row of slot machines
  - Goal: maximize the reward
  - exploitation: focus on a "good" one
  - exploration: also consider others

- Algorithms based on "Reward"
  - n machines, k is index of rounds
  - $\epsilon$ -greedy: relies on a scalar  $\epsilon$

$$j_{\text{emp-opt}} \leftarrow \arg \max_{j \in [1, n]} R(j, k-1)$$

Sample  $i_k \in [1, n]$  from the distribution

$$\left[ \begin{array}{l} j_{\text{emp-opt}} \longrightarrow (1 - \epsilon) + \frac{\epsilon}{n} \\ j \longrightarrow \frac{\epsilon}{n} \quad \text{for each } j \in [1, n] \setminus \{j_{\text{emp-opt}}\} \end{array} \right]$$

High probability

Low probability

- UCB1: balance of exploration and exploitation

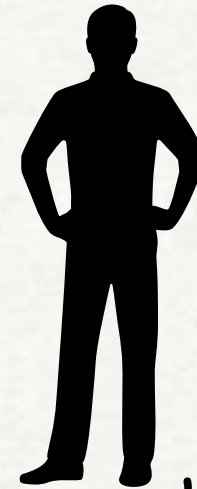
$$i_k \leftarrow \arg \max_{j \in [1, n]} \left( R(j, k-1) + c \sqrt{\frac{2 \ln(k-1)}{N(j, k-1)}} \right)$$

The number of times  
visiting j



# Case 1. $\square_I(\varphi_1 \wedge \varphi_2)$

- Intuition: it suffices that either  $[\mathcal{M}(\mathbf{u}), \varphi_1] < 0$  or  $[\mathcal{M}(\mathbf{u}), \varphi_2] < 0$



- Run hill-climbing optimization on two machines
- Schedule them with MAB solvers
  - $\epsilon$ -greedy, UCB1, etc.
- Reward: hill-climbing gain

$k$ : rounds played

$$\mathcal{R}(\varphi_i) = \begin{cases} \frac{\text{max-rb}(i, k-1) - \text{last-rb}(i, k-1)}{\text{max-rb}(i, k-1)} & \text{if } \varphi_i \text{ has been played before} \\ 0 & \text{otherwise} \end{cases}$$

Intuition: the more robustness decrease, the more promising it is

## Case 2. $\Box_I(\varphi_1 \vee \varphi_2)$

- Not as straightforward as Case 1
- Assumption: it is trivial to falsify only  $\varphi_1$  or  $\varphi_2$
- Robustness restricted to  $S$  :  $\llbracket \mathcal{M}(\mathbf{u}), \varphi \rrbracket_S \quad S \subseteq [0, T]$

- Key insight:

$$\text{Let } S = \{t \subseteq [0, T] \mid \llbracket \mathcal{M}(\mathbf{u})^t, \varphi_1 \rrbracket < 0\}$$

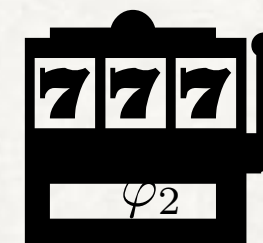
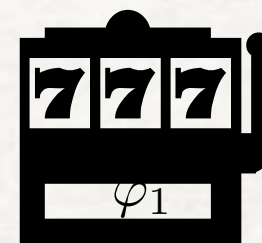
$$\llbracket \mathcal{M}(\mathbf{u}), \varphi_2 \rrbracket_S < 0 \text{ implies } \llbracket \mathcal{M}(\mathbf{u}), \Box_I(\varphi_1 \vee \varphi_2) \rrbracket < 0$$

- Intuition: it suffices that

$$\text{either } \llbracket \mathcal{M}(\mathbf{u}), \varphi_1 \rrbracket_{S_1} < 0$$

$$\text{or } \llbracket \mathcal{M}(\mathbf{u}), \varphi_2 \rrbracket_{S_2} < 0$$

$$S_i = \{t \in [0, T] \mid \llbracket \mathcal{M}(\mathbf{u}^t), \varphi_{\bar{i}} \rrbracket < 0\}$$



when  $i = 1, \bar{i} = 2$

when  $i = 2, \bar{i} = 1$



# Experimental evaluation

- Benchmark set 1: efficacy and efficiency
- Simulink models & specifications:
  - Automatic transmission [Hoxha et al. ARCH'15]
  - Abstract fuel control [Jin et al. HSCC'14]
  - NARMA-L2 neurocontroller [Beale et al. '92]

General boolean connectives, not necessarily with scale problem

- Algorithms:
  - Breach (with CMA-ES)
  - MAB- $\epsilon$ -greedy
  - MAB-UCB

- Misc:
  - 30 trials for each
  - Timeout: 600s
  - HC: CMA-ES

(a) Bbench (here  $\delta_{t'}(w)$  represents  $w^t(t') - w^t(0)$ ).

Bench	Specification	Parameter
ID	Formula	
AT	AT1 $\square_{[0,30]}((gear = 3) \rightarrow (speed > \rho))$	$\rho \in \{20.6, 20.4, 20.2, 20, 19.8\}$
	AT2 $\square_{[0,30]}((gear = 4) \rightarrow (speed > \rho))$	$\rho \in \{43, 41, 39, 37, 35\}$
	AT3 $\square_{[0,30]}((gear = 4) \rightarrow (rpm > \rho))$	$\rho \in \{700, 800, 900, 1000, 1100\}$
	AT4 $\square_{[0,30-\tau]}((\delta_{10}(rpm) > 2000) \rightarrow (\delta_{\tau}(gear) > 0))$	$\tau \in \{15, 16, 17, 18, 19\}$
	AT5 $\square_{[0,30]}((speed < \rho) \wedge (RPM < 4780))$	$\rho \in \{130, 131, 132, 133, 134, 135, 136, 137\}$
	AT6 $\square_{[0,26]}((\delta_4(speed) > \rho) \rightarrow (\delta_4(gear) > 0))$	$\rho \in \{20, 25, 30, 35, 40\}$
	AT7 $\square_{[0,30-\tau]}((\delta_{\tau}(speed) > 30) \rightarrow (\delta_{\tau}(gear) > 0))$	$\tau \in \{2, 3, 4, 5, 6, 7, 8\}$
AFC	AFC1 $\square_{[11,50]}((controller\_mode = 0) \rightarrow (mu < \rho))$	$\rho \in \{0.16, 0.17, 0.18, 0.19, 0.2\}$
	AFC2 $\square_{[11,50]}((controller\_mode = 1) \rightarrow (mu < \rho))$	$\rho \in \{0.222, 0.224, 0.226, 0.228, 0.23\}$
	$close \equiv  Pos - Ref  \leq \rho + \alpha *  Ref $	
	$reach \equiv \diamond_{[0,2]}(\square_{[0,1]}(close))$	
NN	NN1 $\square_{[0,18]}(\neg close \rightarrow reach), \alpha = 0.04$	$\rho \in \{0.001, 0.002, 0.003, 0.004, 0.005\}$
	NN1 $\square_{[0,18]}(\neg close \rightarrow reach), \alpha = 0.03$	$\rho \in \{0.001, 0.002, 0.003, 0.004, 0.005\}$

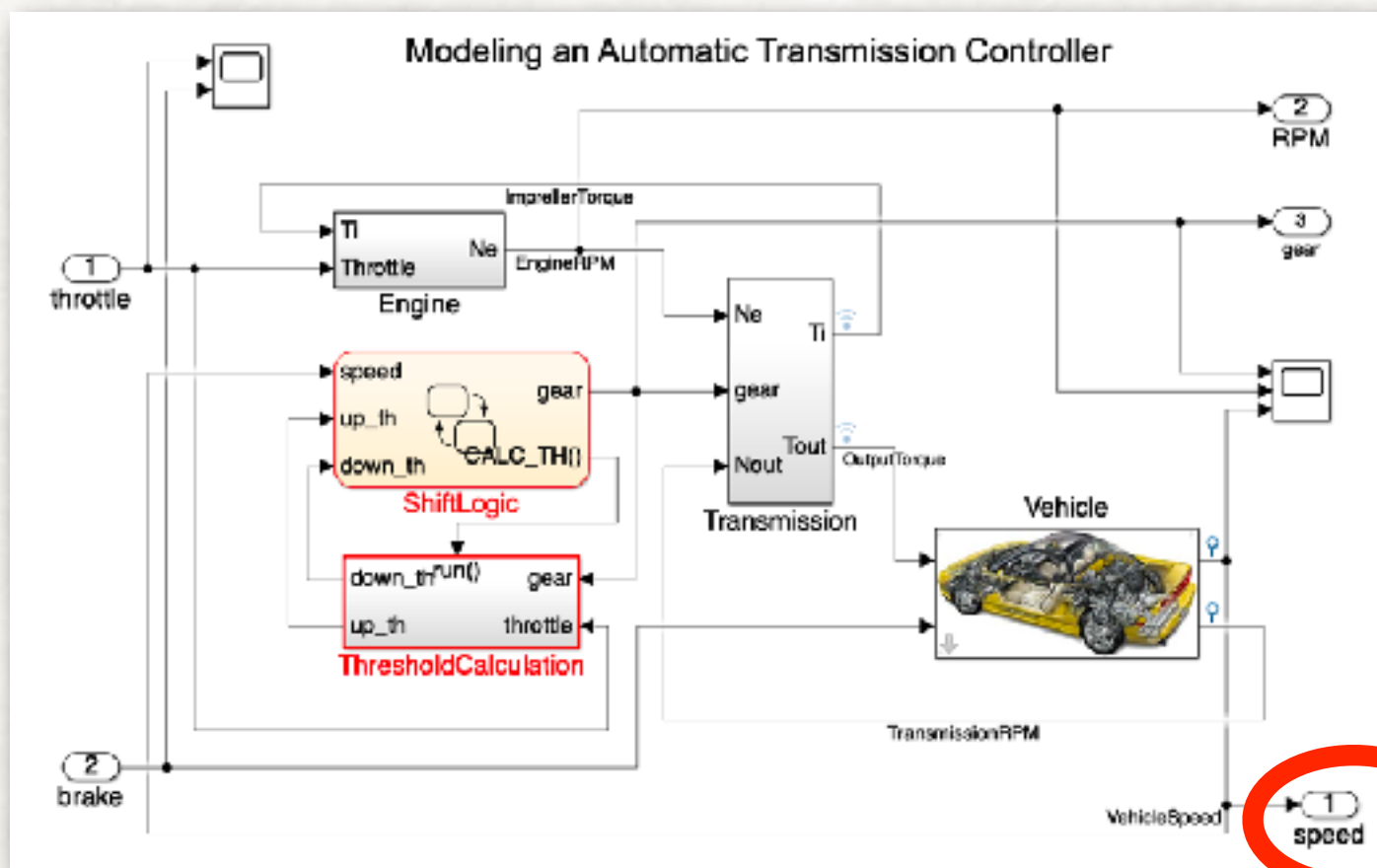
Spec. ID	Breach						MAB- $\epsilon$ -greedy						MAB-UCB									
	SR (#)			time (sec.)			SR			time			SR (#/30)			time (sec.)						
	success rate	M	Avg	success rate	$\Delta$	Avg	success rate	$\Delta$	M	Avg	$\Delta$	success rate	$\Delta$	M	Avg	$\Delta$						
AT1	14	25	20.2	125	361.2	223.1	24	30	28.6	35.7	62.7	213.4	106.4	-73.4	28	30	29.2	37.8	45.1	146.8	77.4	-97.1
AT2	11	30	20.2	14	390.6	209.8	30	30	30	43.9	11.9	126.3	54.5	-96.9	27	30	29.4	42.2	17.7	92.5	36.8	-112.1
AT3	29	30	29.4	2.3	22.2	14.2	30	30	30	2	2.5	7	3.5	-82.9	30	30	30	2	2.5	3.6	3	-88.6
AT4	18	30	25.8	19.5	265.3	109.6	29	30	29.8	16	7.8	45.1	24.4	-105	30	30	30	16.6	6.2	36.2	22.2	-113.5
AT5	6	23	14.1	203.1	525.9	366.2	26	30	28.5	72.1	35.2	149	93.7	-120.6	26	30	28.2	71.4	37.7	154.1	99.2	-116.8
AT6	5	29	22.8	30.1	509.5	157	21	30	27	28	2.3	300	95.1	-98.3	22	30	27	27.7	2.9	247.3	86.1	-99.4
AT7	15	30	26.6	12.2	314	81.5	20	30	28.6	8.4	2.9	283.9	49.9	-92	23	30	29	10.3	5.5	223.3	42.9	-88.3
AFC1	6	30	14.4	124.8	565.6	413.5	4	28	12	-28.4	171	568.4	446	10.8	5	30	16.4	9.7	98.7	559.8	389.9	-9.3
AFC2	2	30	18	80.7	582.3	343.4	5	30	20	23.8	43.2	547.8	301.9	-23.8	5	30	20	22.9	59.4	568.4	320.5	-11.1
NN1	17	25	20.8	212.9	384.7	292.9	14	27	20.2	-4.5	189.5	422.8	320.3	6.2	17	28	22.6	7.3	148.2	403.3	272.3	-11.8
NN2	27	28	27.2	55.5	93.4	73.1	30	30	30	9.8	11	39.3	26.3	-97.8	30	30	30	9.8	14.6	38.2	27.4	-92.3
AT1 <sup>-2</sup>	30	30	30	42.5	97.4	56.9	28	30	29	-3.4	75.6	178.3	118.7	68.7	28	30	29.4	-2.1	54.3	136.3	80.3	33.3
AT1 <sup>0</sup>	14	25	20.2	125	361.2	223.1	24	30	28.6	35.7	62.7	213.4	106.4	-73.4	28	30	29.2	37.8	45.1	146.8	77.4	-97.1
AT1 <sup>1</sup>	4	21	15.4	204.5	527.6	310.2	25	30	29	68.4	49	234.7	102.1	-108	27	29	28.2	64.5	77.5	128.7	105.1	-93
AT1 <sup>3</sup>	8	24	19.8	164	471.7	240.1	29	30	29.8	44.6	67.5	170.6	101.9	-77.3	29	30	29.4	43.4	55.4	104.8	80.6	-93.6
AT5 <sup>-2</sup>	29	30	29.6	61.1	163.7	102	25	30	27.8	-6.4	76.9	139.5	111.9	12.6	28	30	29.4	-0.7	48.5	131.9	85.7	-17
AT5 <sup>0</sup>	6	18	11.2	291.1	525.9	423.1	28	30	28.4	90.5	80.2	151.3	107.4	-117.7	26	30	28	89.4	68.3	154.1	114.9	-114.5
AT5 <sup>1</sup>	0	2	0.4	566.4	600	593.3	27	30	28.4	194.8	70.7	184.5	110.3	-138.5	25	30	27.6	194.1	83.1	150	123.7	-131.2
AT5 <sup>3</sup>	0	1	0.2	586.4	600	597.3	27	30	28.6	197.2	66.8	163.3	102.5	-142.3	27	29	28	197.2	80.4	160.9	111.9	-137.4
AFC1 <sup>0</sup>	6	30	14.4	124.8	565.6	413.5	4	29	16.4	8.5	115.1	559.9	411.1	-2.8	5	30	16.4	9.7	98.7	559.8	389.9	-9.3
AFC1 <sup>1</sup>	7	30	16.6	99	548.2	393.3	3	29	10.8	-60.9	198.1	587.6	465.8	24.6	7	29	17.8	10.3	105.7	527.3	354.3	-10.3
AFC1 <sup>2</sup>	0	12	5.2	434.4	600	535.8	3	28	11.6	96.2	180.8	577.6	463	-20.7	4	30	17	127	73.7	556.3	374.5	-47.3
AFC1 <sup>3</sup>	1	12	4.8	425.7	587.4	532.6	3	30	14.4	109	138	585.5	436.5	-28	7	30	15	113	77.1	553.4	403.7	-39.9

- RQ1: Which is the best MAB algorithm for our purpose?
  - MAB-UCB
- RQ2: How is the performance of the proposed process
  - Generally more effective and efficient compared to Breach
  - Works very well even on examples free of scale problem



# Experimental evaluation

- Benchmark set 2: scale problem
- Experiment setting
- e.g., Automatic transmission [Hoxha, ARCH'15]

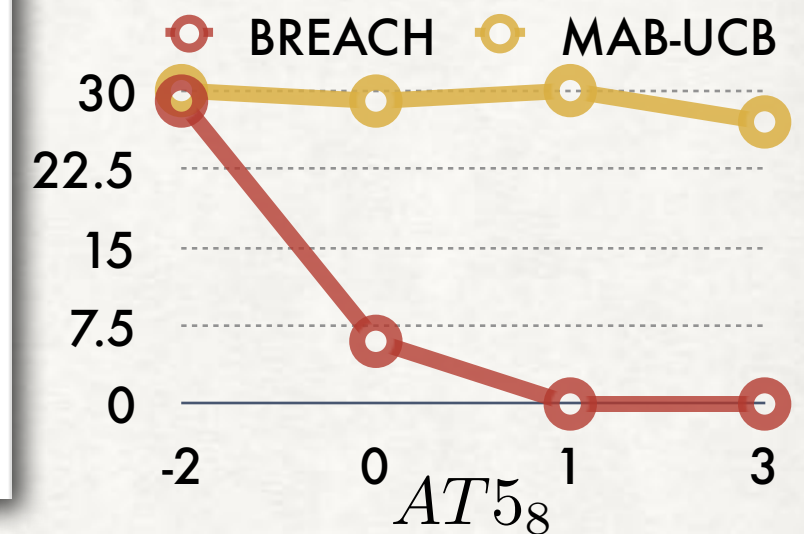
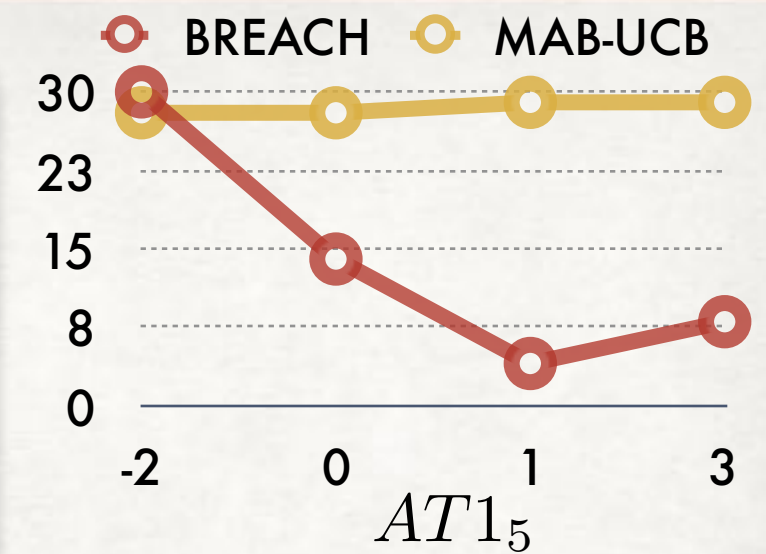


Spec ID	scaled output	factor $10^k$
AT1 <sub>1</sub>		
AT1 <sub>2</sub>		
AT1 <sub>3</sub>	<i>speed</i>	$k \in \{-2,0,1,3\}$
AT1 <sub>4</sub>		
AT1 <sub>5</sub>		
AT5 <sub>4</sub>		
AT5 <sub>5</sub>		
AT5 <sub>6</sub>	<i>speed</i>	$k \in \{-2,0,1,3\}$
AT5 <sub>7</sub>		
AT5 <sub>8</sub>		
AFC1 <sub>1</sub>		
AFC1 <sub>2</sub>		
AFC1 <sub>3</sub>	<i>mu</i>	$k \in \{0,1,2,3\}$
AFC1 <sub>4</sub>		
AFC1 <sub>5</sub>		

e.g., when scaling speed and  $k = 3$ ,  
 $\square_{[0,30]} (gear = 3 \rightarrow speed > 20000)$

$speed * 10^k$

Spec. ID	Breach		MAB-UCB		Spec. ID	Breach		MAB-UCB		Spec. ID	Breach		MAB-UCB	
	SR (/30)	time (sec.)	SR (/30)	time (sec.)		SR (/30)	time (sec.)	SR (/30)	time (sec.)		SR (/30)	time (sec.)	SR (/30)	time (sec.)
AT1 <sup>-2</sup>	30	51.3	30	54.3	AT5 <sup>-2</sup>	30	61.1	30	48.5	AFC1 <sup>0</sup>	30	124.8	30	98.7
AT1 <sup>0</sup>	25	125	29	75	AT5 <sup>0</sup>	18	291.1	28	94.5	AFC1 <sup>1</sup>	30	99	29	105.7
AT1 <sup>1</sup>	20	221.1	28	107.9	AT5 <sup>1</sup>	2	566.4	25	150	AFC1 <sup>2</sup>	12	434.4	30	73.7
AT1 <sup>2</sup>	23	170	29	55.4	AT5 <sup>2</sup>	1	586.4	28	96.2	AFC1 <sup>3</sup>	12	425.7	30	77.1
AT1 <sup>3</sup>	30	49	29	67.5	AT5 <sup>3</sup>	30	71.3	29	67.8	AFC1 <sup>4</sup>	16	421.5	23	346.8
AT1 <sup>4</sup>	22	187.5	30	45.1	AT5 <sup>4</sup>	15	369.1	27	114	AFC1 <sup>5</sup>	25	345.9	27	227.9
AT1 <sup>5</sup>	21	204.5	29	77.5	AT5 <sup>5</sup>	0	600	29	83.1	AFC1 <sup>6</sup>	8	497.2	25	320.5
AT1 <sup>6</sup>	24	164	30	61	AT5 <sup>6</sup>	0	600	27	113.8	AFC1 <sup>7</sup>	5	518.1	21	364
AT1 <sup>7</sup>	30	42.5	30	62.4	AT5 <sup>7</sup>	29	110.2	28	103.3	AFC1 <sup>8</sup>	11	457.7	15	442
AT1 <sup>8</sup>	19	239.5	29	62.5	AT5 <sup>8</sup>	10	438.2	30	68.3	AFC1 <sup>9</sup>	13	479.2	14	455.5
AT1 <sup>9</sup>	16	296.2	27	128.7	AT5 <sup>9</sup>	0	600	27	126.7	AFC1 <sup>10</sup>	2	590.7	15	453.2
AT1 <sup>10</sup>	21	209.8	30	93.4	AT5 <sup>10</sup>	0	600	29	80.4	AFC1 <sup>11</sup>	5	545.6	8	510.6
AT1 <sup>11</sup>	30	44.5	30	80.8	AT5 <sup>11</sup>	30	103.6	30	77.3	AFC1 <sup>12</sup>	9	498.2	9	502.1
AT1 <sup>12</sup>	21	202.2	30	57.4	AT5 <sup>12</sup>	7	491.4	26	154.1	AFC1 <sup>13</sup>	8	494	12	455
AT1 <sup>13</sup>	16	301.7	28	119.5	AT5 <sup>13</sup>	0	600	27	134.3	AFC1 <sup>14</sup>	4	556.8	11	468.7
AT1 <sup>14</sup>	23	185.1	29	88.3	AT5 <sup>14</sup>	0	600	29	108	AFC1 <sup>15</sup>	1	587.4	9	513.4
AT1 <sup>15</sup>	30	97.4	28	136.3	AT5 <sup>15</sup>	29	163.7	30	131.9	AFC1 <sup>16</sup>	6	565.6	5	559.8
AT1 <sup>16</sup>	14	361.2	28	146.8	AT5 <sup>16</sup>	6	525.9	29	143.6	AFC1 <sup>17</sup>	7	548.2	7	527.3
AT1 <sup>17</sup>	4	527.6	29	91.9	AT5 <sup>17</sup>	0	600	30	124.2	AFC1 <sup>18</sup>	0	600	4	556.3
AT1 <sup>18</sup>	8	471.7	29	104.8	AT5 <sup>18</sup>	0	600	27	160.9	AFC1 <sup>19</sup>	1	586	7	553.4



- RQ3: Does the proposed approach effectively solve the scale problem?
  - — yes, ours is not subject to the change of the scale.
- RQ4: Is the proposed approach more effective than normalization?
  - — yes, e.g.,  $AT5_5^1$  is normalized to the same scale, but Breach performs badly



# Conclusion and future work

- Conclusion

- We propose an approach for solving the scale problem
- Multi-armed bandit solver + hill-climbing gain reward
- Experiments show the effectiveness and efficiency

- Future work

- Extension to a more general class of STL formula
- Extension to robustness semantics other than the spatial one

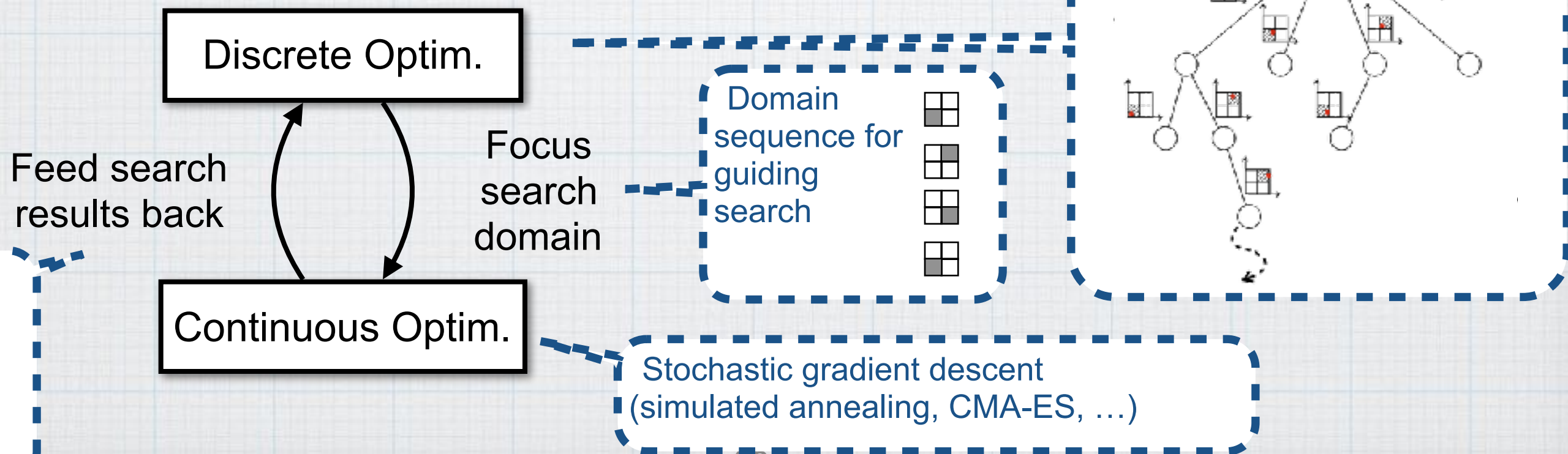
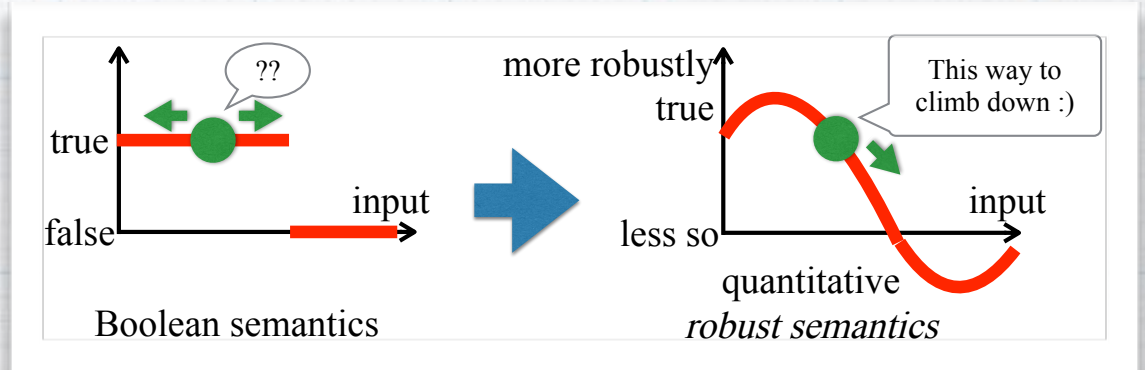


Thanks!

# Hierarchical Optimization in Hybrid System Falsification

[Zhang, Ernst, Sedwards, Arcaini & Hasuo, EMSOFT'18]  
 [Zhang, Hasuo & Arcaini, CAV'19] ...

- \* Another example [EMSOFT'18]
  - \* utilizing time-causal structures
  - \* for search capabilities,
  - \* but also for coverage and exploration





# Problem

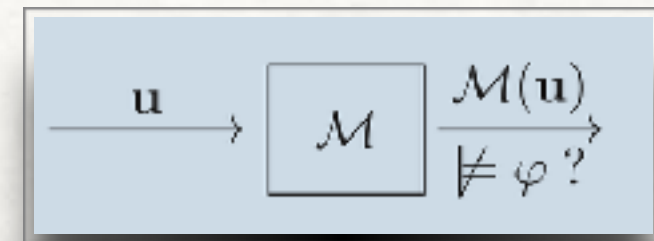
- Falsification problem:

$\mathcal{M}$  : black-box model

$\mathbf{u}$  : input signal (piecewise constant)

$\mathcal{M}(\mathbf{u})$  : output signal

$\varphi$  : specification in Temporal Logic



- Goal: to find a  $\mathbf{u}$  s.t.  $\mathcal{M}(\mathbf{u}) \neq \varphi$

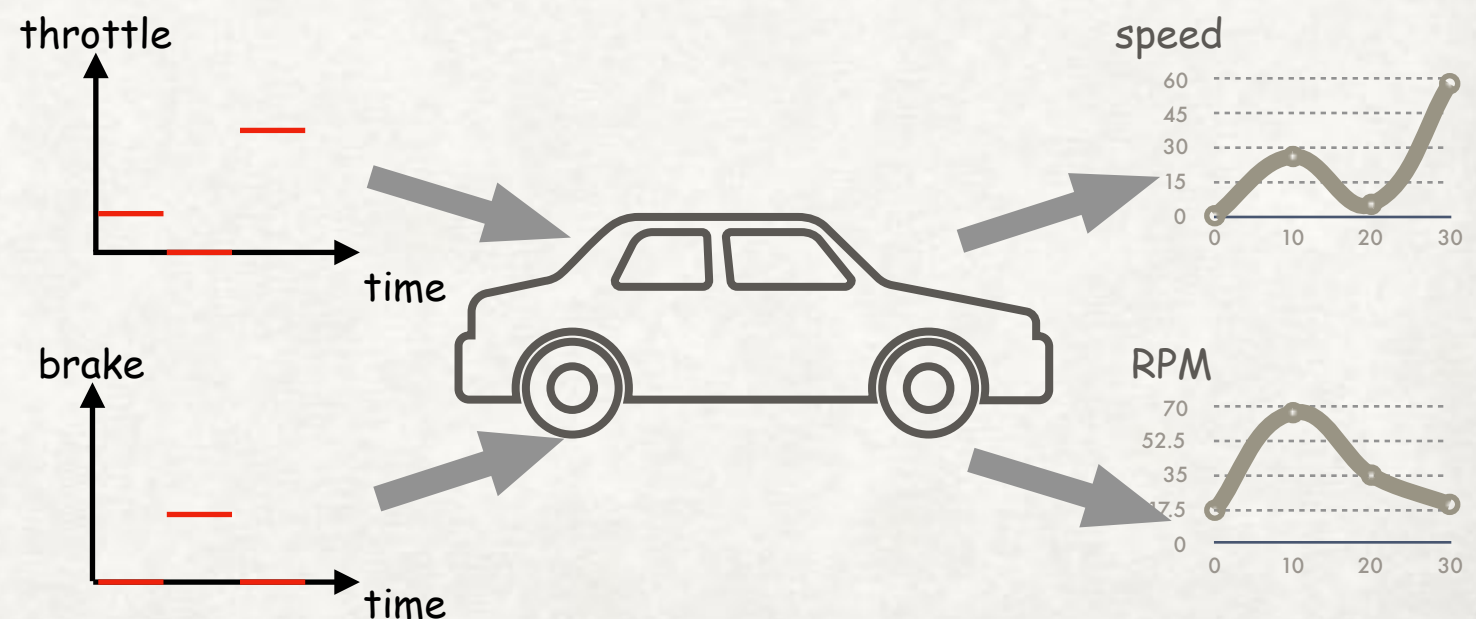
Example:

$\square_{[0,30]} (speed < 120)$

Always

Bounded  
-time

Proposition

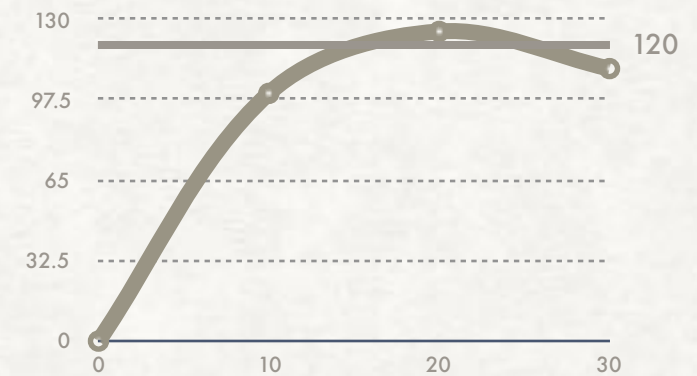
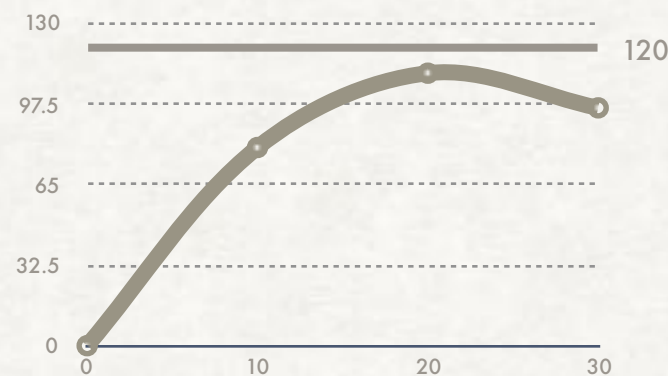
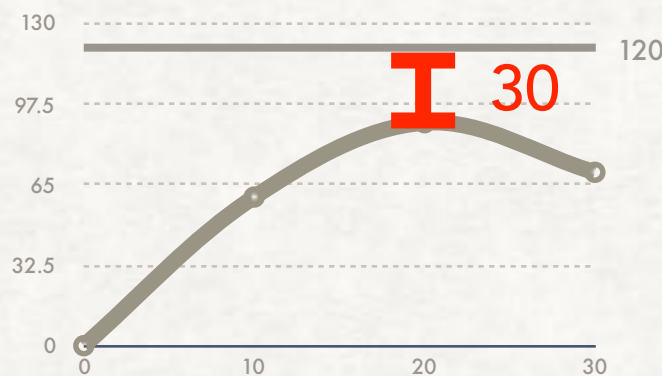


# Existing solutions

- Quantitative robustness semantics of STL [Donze, Maler FORMATS'10]

e.g.,  $\varphi = \square_{[0,30]}(speed < 120)$

Output  
Signals



Boolean  
Satisfaction

True

**Boolean**

False

Quantitative  
Robustness

30

**Real number**

-5



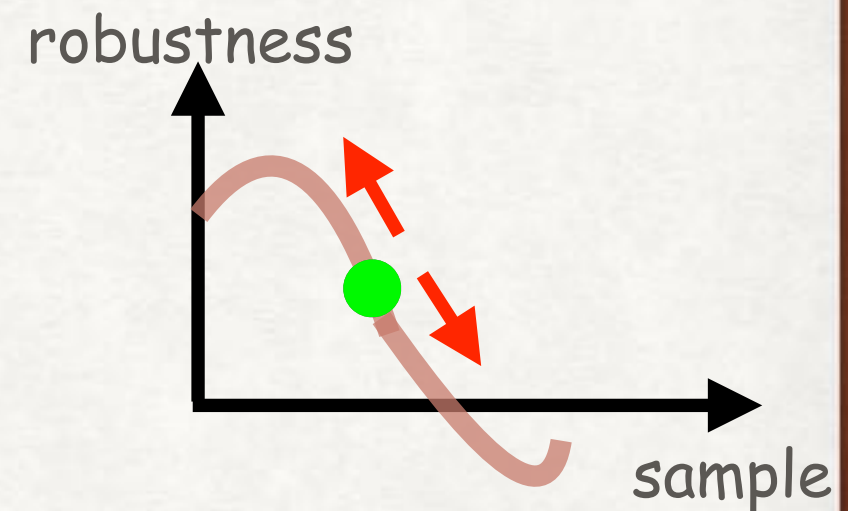


# Existing solutions

- falsification => **optimization**
- Objective function:  $[[\mathcal{M}, \mathbf{u}]]$
- Goal:  $\min ([[ \mathcal{M}, \mathbf{u} ]])$  to see if it can be negative

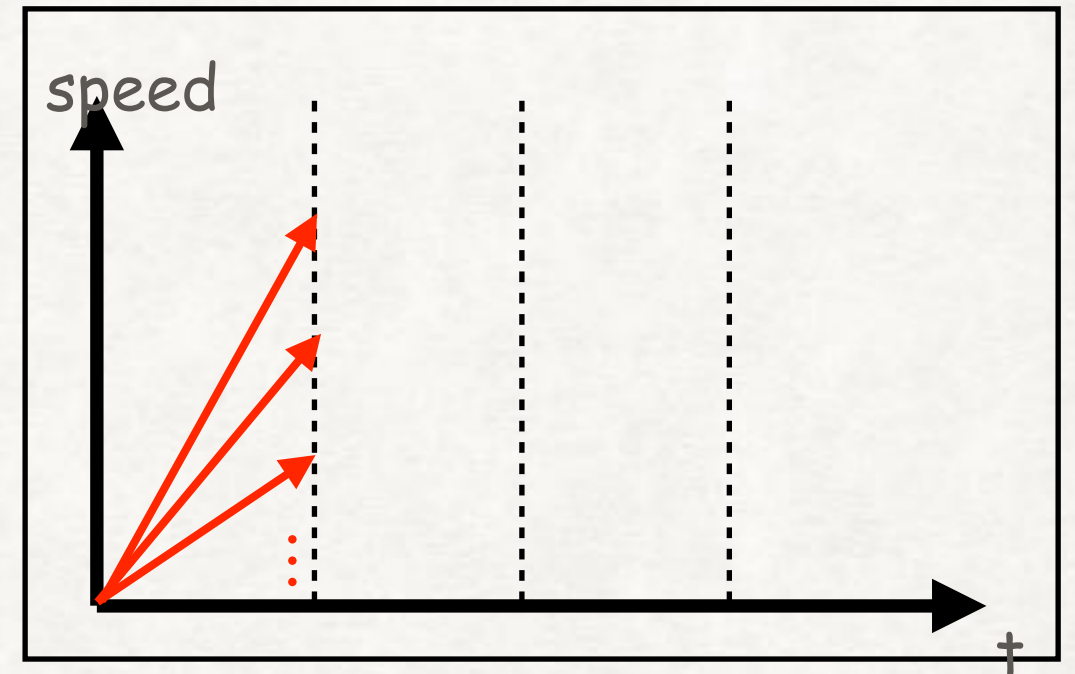
robustness

- “Hill-climbing” optimization algorithms
  - Decide next sample based on history
  - More intelligent than random sampling
  - Tools: Breach [Donze CAV'10] (CMA-ES, NM, etc.)  
S-TALIRO [Annapureddy et al. TACAS'11] (SA etc.)



# Existing solutions

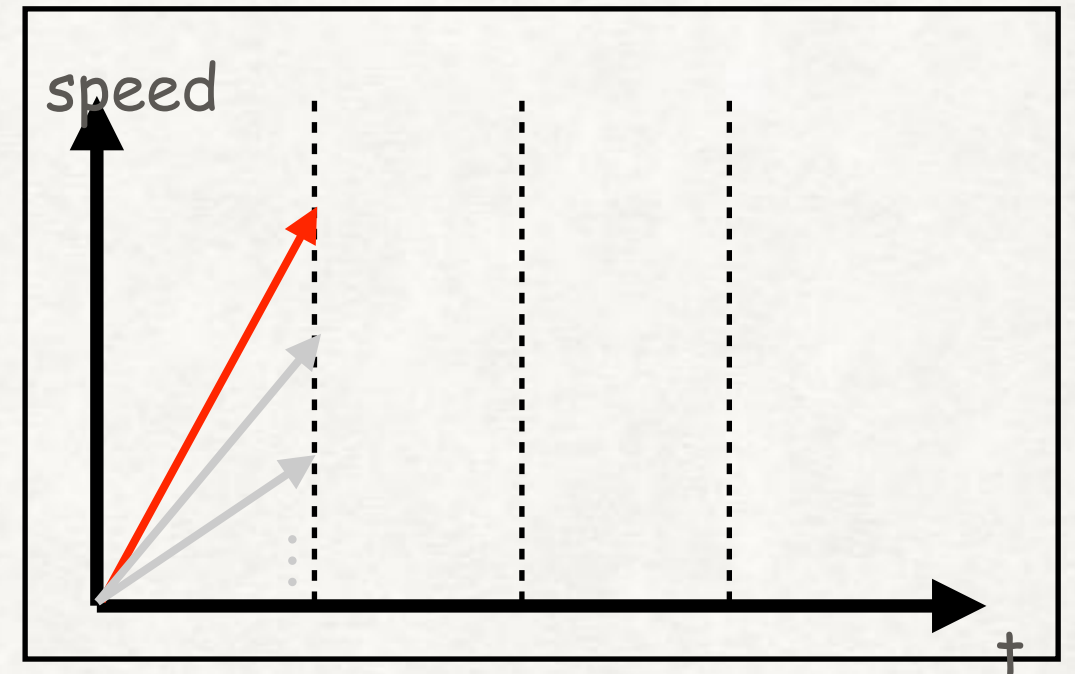
- Time-staging heuristics [Ernst+SNR'18]
  - Divide time into many intervals
  - Take local optimum of each stage
  - Combine them as whole input





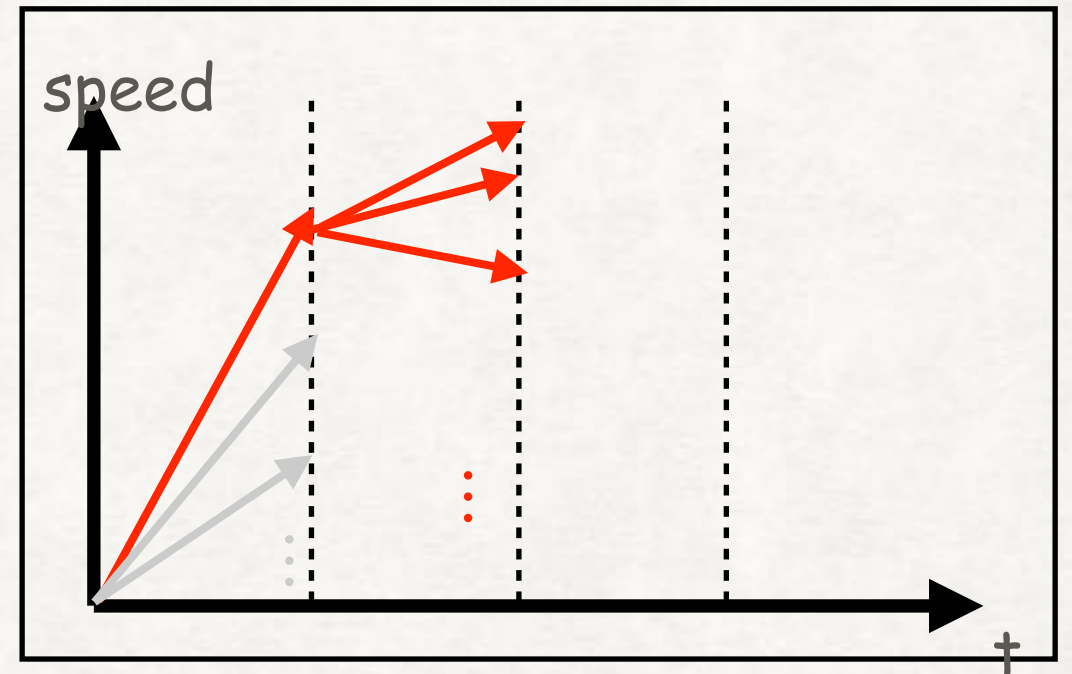
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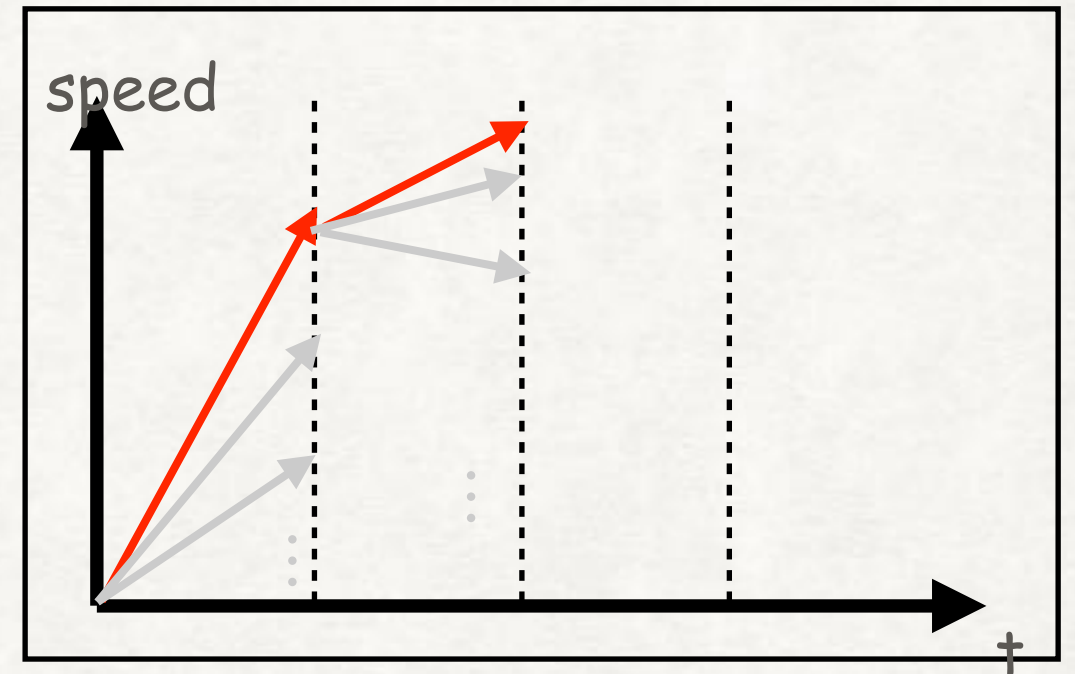
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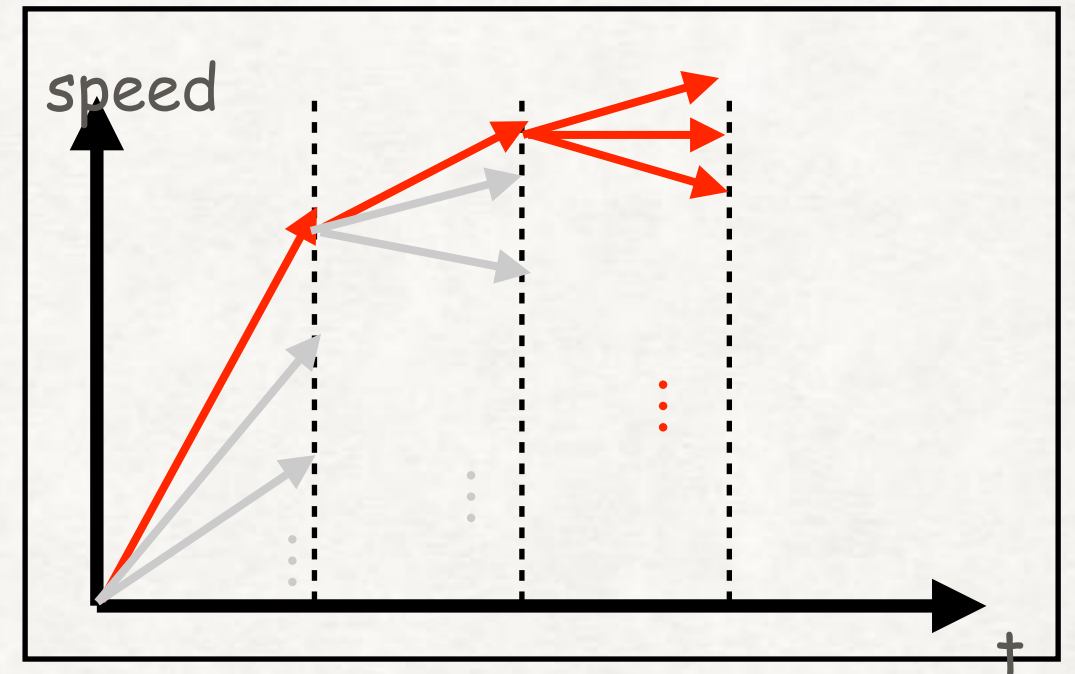
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# Existing solutions

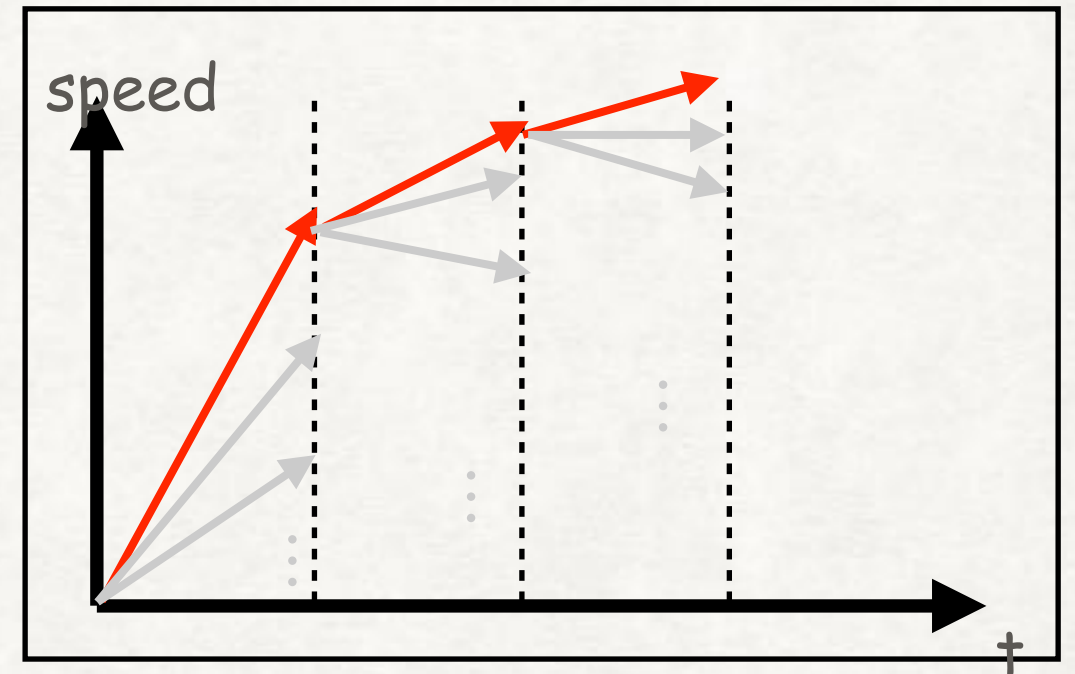
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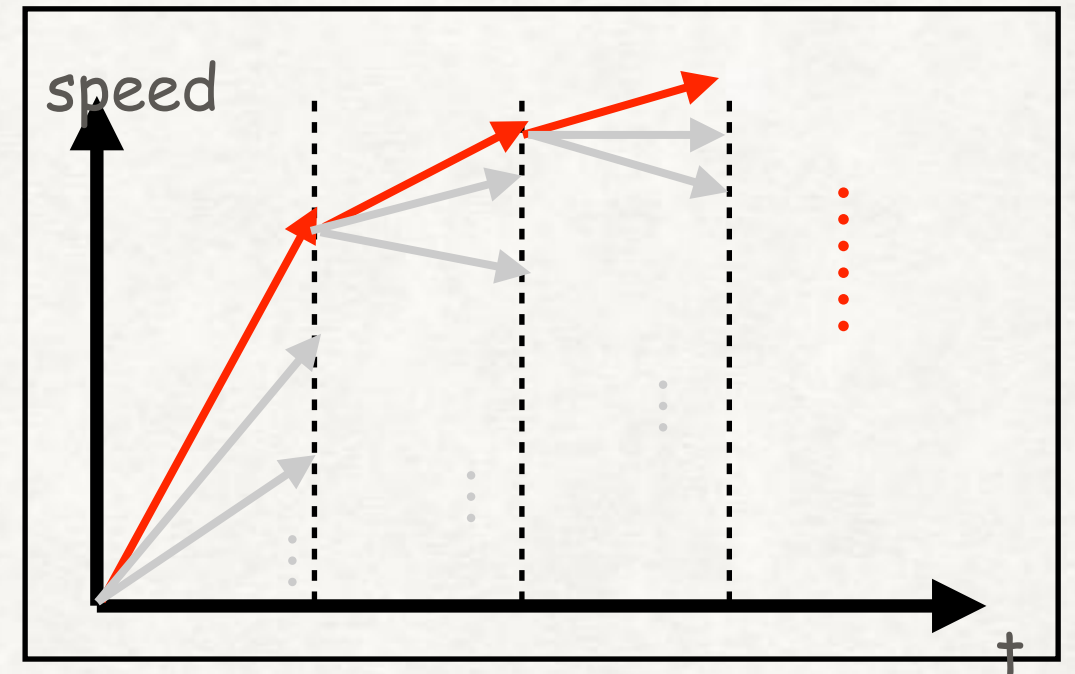
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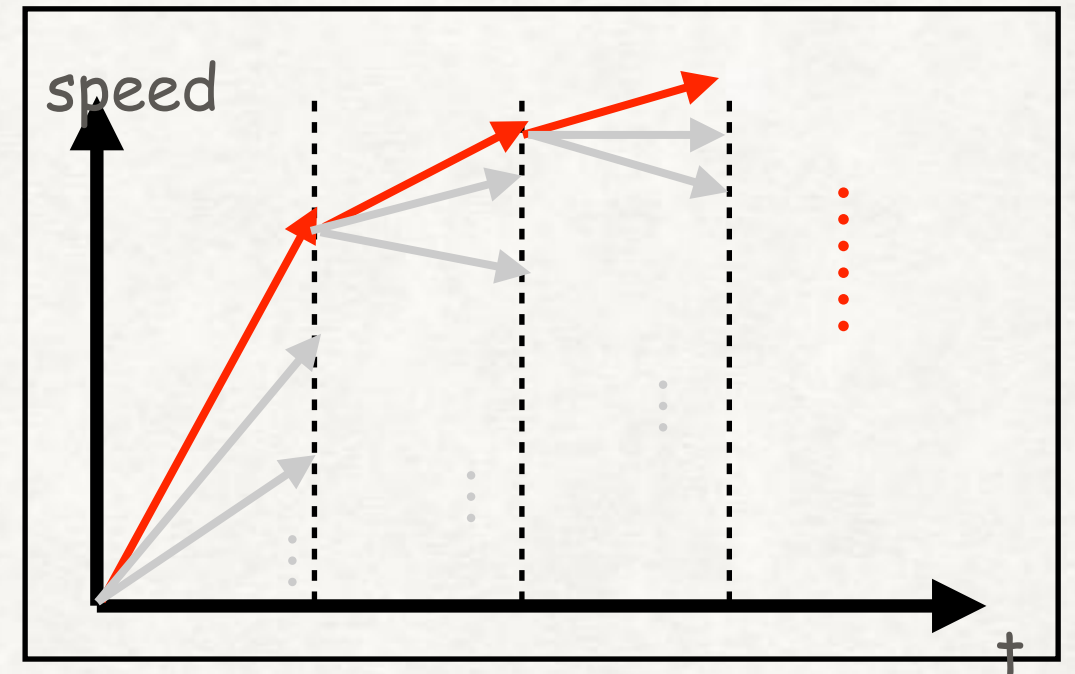
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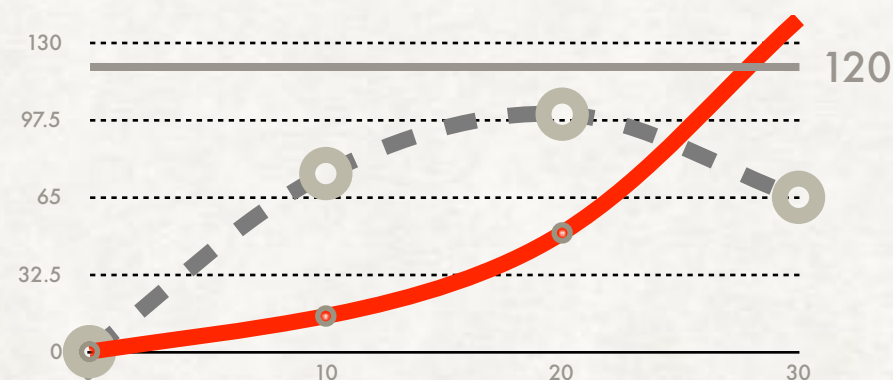


# Existing solutions

- Time-staging heuristics [Ernst+SNR'18]
  - Divide time into many intervals
  - Take local optimum of each stage
  - Combine them as whole input



Weakness: How about this situation?

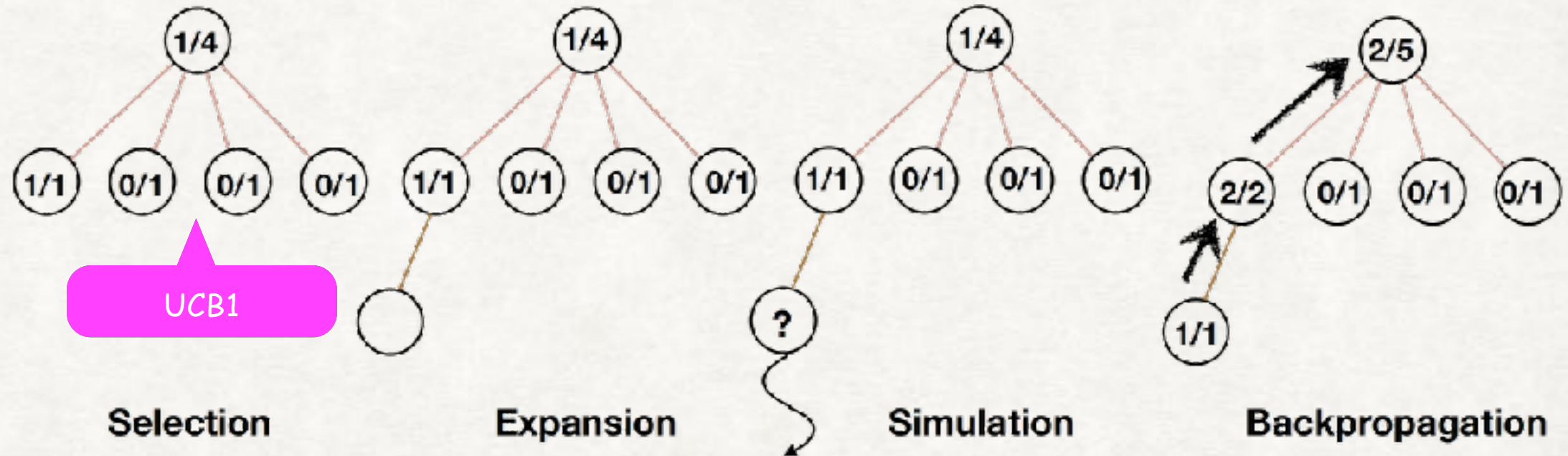
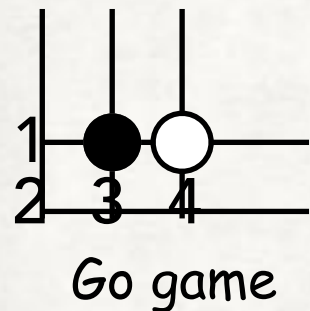


We need trackback mechanism,  
we need a tree-search structure...

- But...
- Our search space is infinite...



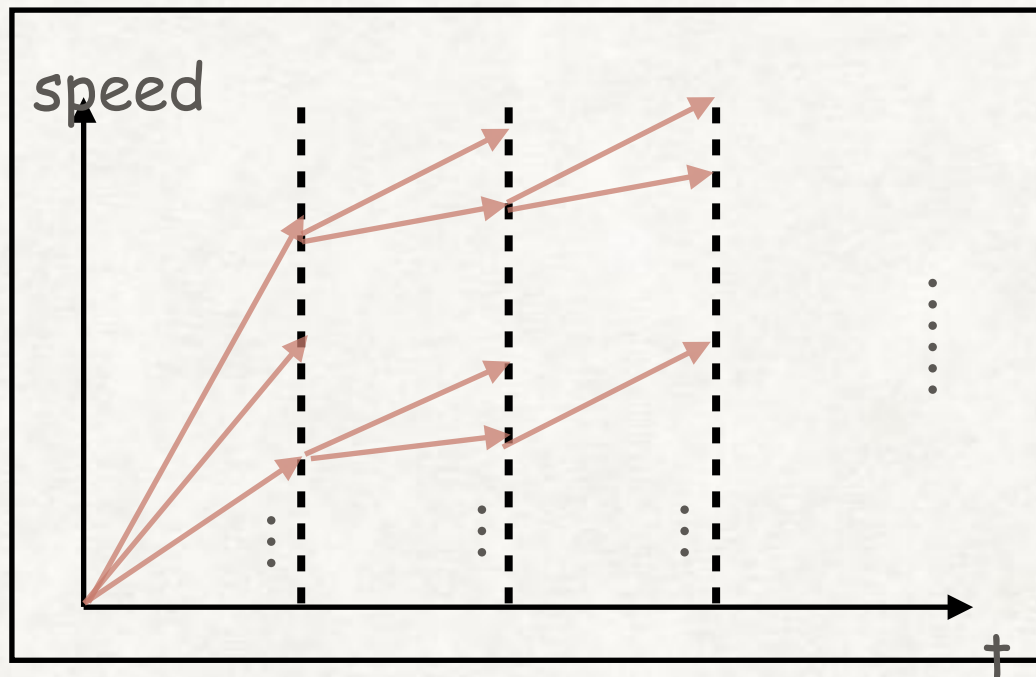
# Monte Carlo Tree Search



- Pay much attention on "promising" branches
- Playout (simulation) to give each node a reward
- UCB1 [Kocsis+ECML'06] for exploration and exploitation

# Application of MCTS

- Naive idea of applying MCTS to falsification



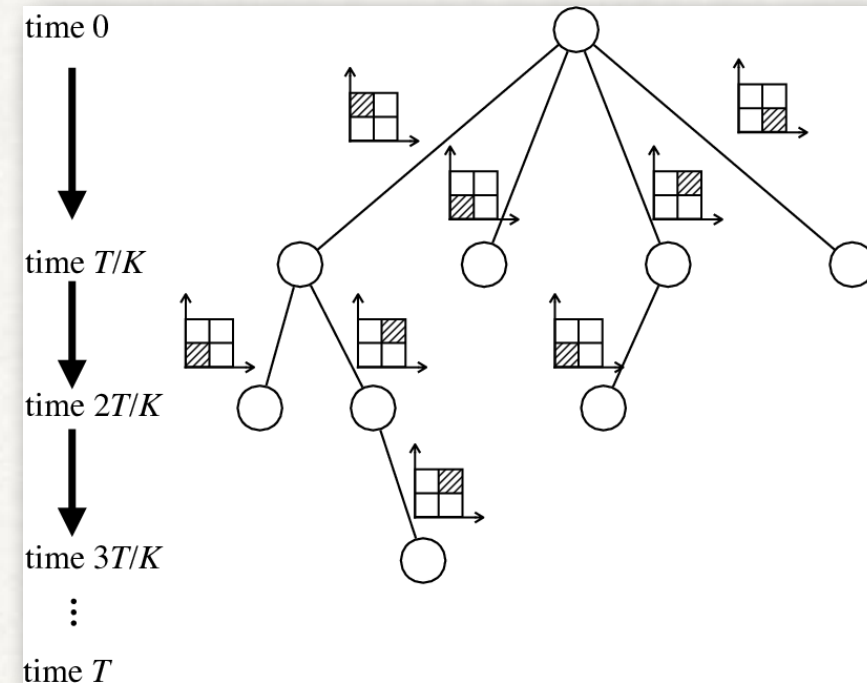
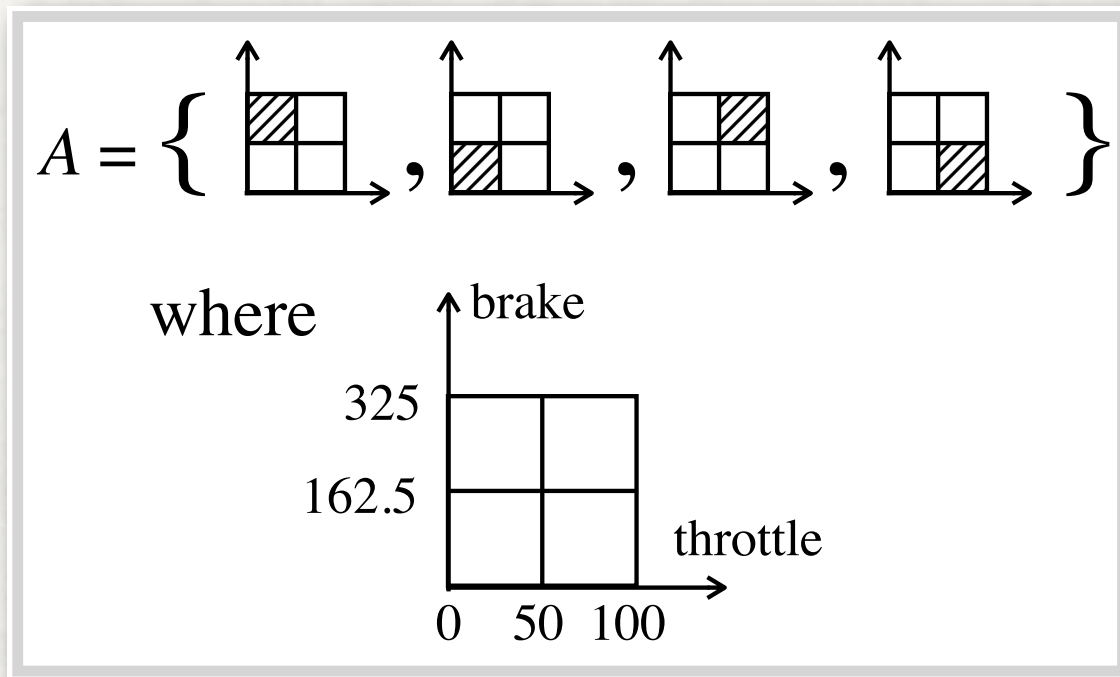
1. Divide time
2. Take a value as child
3. Randomly pick child to do playout ...

- Challenges

- Q1: How to select children from infinite input space
- Q2: How to define reward
- Q3: How does playout work



# Q1: Infinite input space



- Partition input space at each stage
- Treat each sub-region as a child
- Reward evaluates each sub-region

# Q2: reward

- Original MCTS:

```
function BESTCHILD( $v, c$ )
  return arg max $v' \in \text{children of } v$   $\frac{Q(v')}{N(v')} + c \sqrt{\frac{2 \ln N(v)}{N(v)}}$ 
```

Reward: an estimated winning rate

$v'$  : expanded child  
 $Q(v')$  : winning times  
 $N(v')$  : visiting times  
 $N(v)$  : visiting times to the parent

- Our definition:

$$\left(1 - \frac{R(v')}{\max_{w \in \mathcal{T}} R(w)}\right)$$

$R(v')$  : robustness

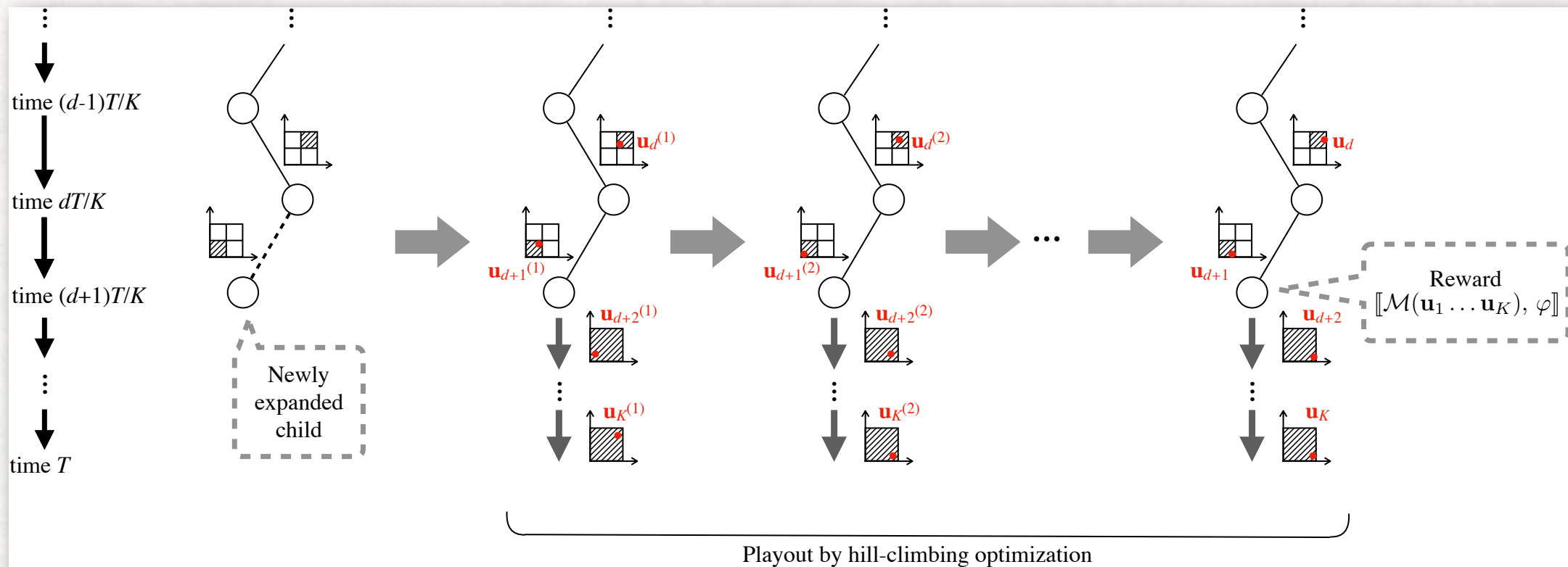
$\max_{w \in \mathcal{T}} R(w)$ : the max (worst) robustness over the whole tree

```
function BESTCHILD( $v, c$ )
  return arg max $v' \in \text{children of } v$   $\left( \left(1 - \frac{R(v')}{\max_{w \in \mathcal{T}} R(w)}\right) + c \sqrt{\frac{2 \ln N(v)}{N(v)}} \right)$ 
```

Reward: negatively correlated to robustness

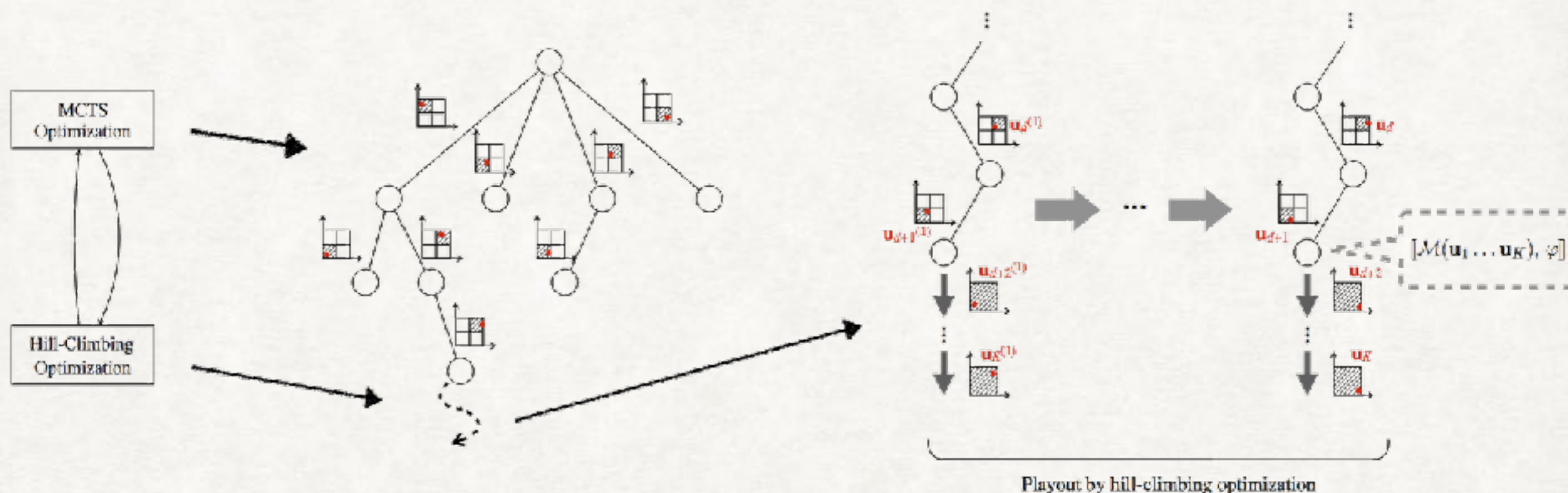


# Q3: playout



- Goal: evaluate the expanded child
- Steps:
  - Collect the sequence of sub-regions from the root to the expanded child
  - Include all the input region of the remaining stages
  - Run hill-climbing optimization within a timeout

# Basic Alg.: Two-layered optimization

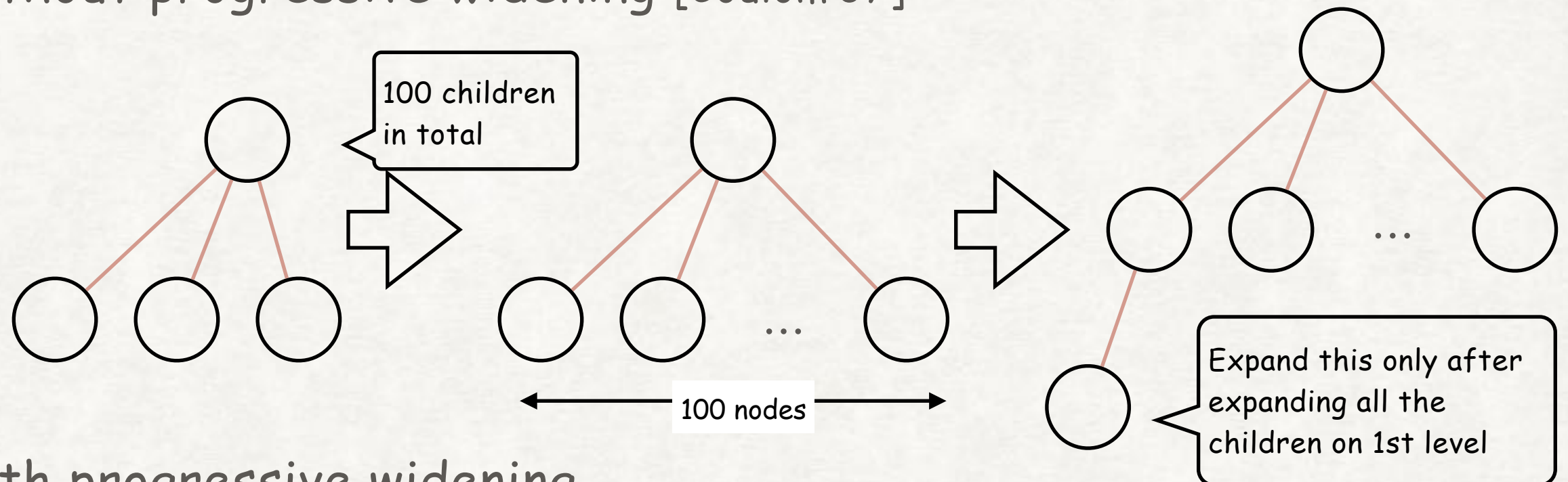


- Two-layered optimization framework:
  - MCTS: decide the directions of the search based on the reward given by hill-climbing
  - Hill-climbing: compute the concrete robustness values of the path assigned by MCTS

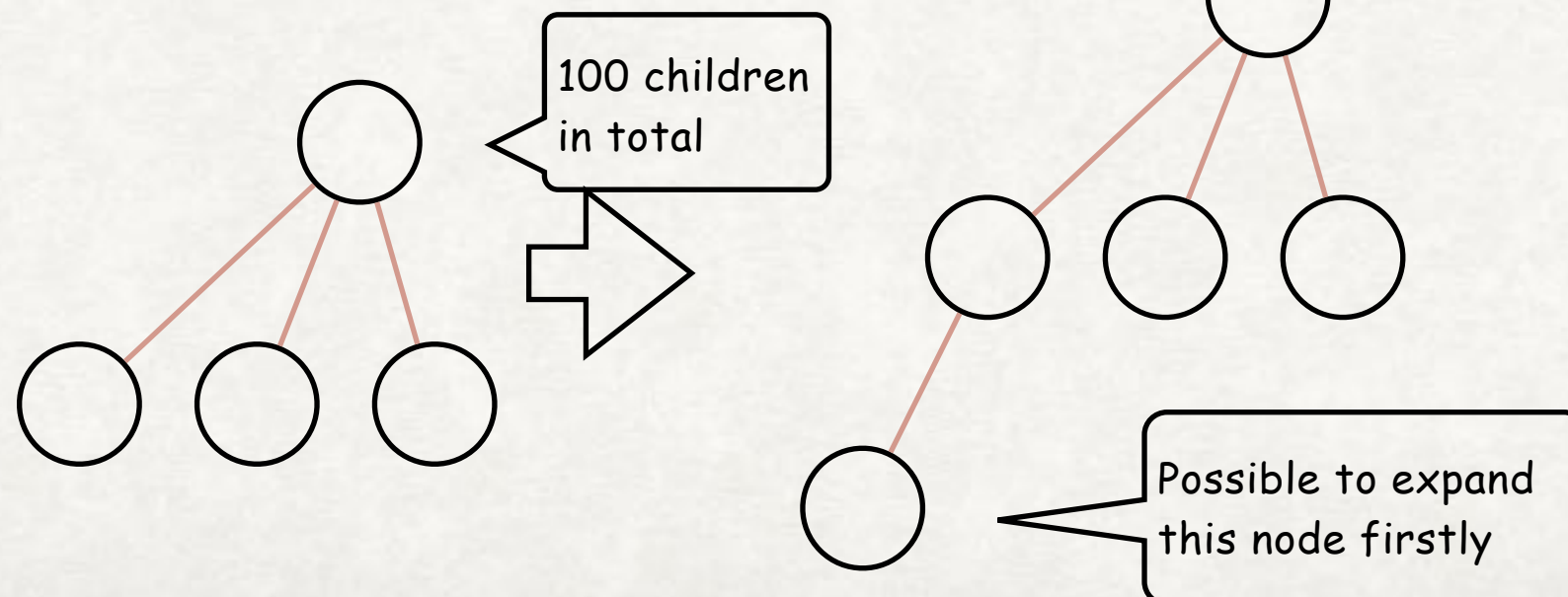


# Biased Alg.: Progressive widening

- Without progressive widening [Coulom'07]



- With progressive widening



$$C \cdot N(v)^\alpha$$

# Experimental evaluation

- Evaluated algorithms:
  - Breach (Hill-climbing)
  - Basic algorithm (MCTS + Hill-climbing)
  - Biased algorithm (MCTS + Hill-climbing + progressive widening)
- Benchmarks:
  - Automatic transmission
  - Abstract fuel control
  - Free floating robot



# Experimental evaluation

		AT model										AFC model				FFR model	
		S1		S2		S3		S4		S5		Sbasic		Sstable		Strap	
Algorithm		succ.	time	succ.	time	succ.	time	succ.	time	succ.	time	succ.	time	succ.	time	succ.	time
Random		10/10	108.9	10/10	289.1	1/10	301.1	0/10	-	0/10	-	6/10	278.7	10/10	242.6	4/10	409.3
CMA-ES	Breach	10/10	21.9	6/10	30.3	<b>10/10</b>	<b>193.9</b>	4/10	208.8	3/10	75.5	<b>10/10</b>	<b>111.7</b>	3/10	256.3	<b>10/10</b>	<b>119.8</b>
	Basic	10/10	15.8	10/10	108.5	10/10	697.1	7/10	786.8	9/10	384.4	10/10	182.0	7/10	336.9	10/10	338.0
	P.W.	<b>10/10</b>	<b>10.8</b>	<b>10/10</b>	<b>65.7</b>	10/10	728.6	7/10	<b>767.8</b>	<b>10/10</b>	<b>648.1</b>	10/10	177.1	8/10	<b>272.9</b>	10/10	473.9
GNM	Breach	<b>10/10</b>	<b>5.4</b>	<b>10/10</b>	<b>151.4</b>	0/10	-	0/10	-	0/10	-	<b>10/10</b>	<b>171.4</b>	0/10	-	0/10	-
	Basic	10/10	12.4	10/10	162.3	<b>10/10</b>	<b>185.6</b>	7/10	261.9	7/10	163.7	10/10	227.1	2/10	378.5	<b>10/10</b>	<b>162.2</b>
	P.W.	10/10	60.8	9/10	110.7	8/10	211.2	<b>8/10</b>	<b>313.0</b>	<b>10/10</b>	<b>178.7</b>	10/10	252.0	6/10	<b>153.2</b>	6/10	197.4
SA	Breach	<b>10/10</b>	<b>160.1</b>	0/10	-	3/10	383.7	0/10	-	3/10	80.4	0/10	-	6/10	307.0	3/10	92.8
	Basic	10/10	264.8	9/10	236.1	<b>8/10</b>	<b>385.6</b>	<b>8/10</b>	<b>505.3</b>	7/10	341.2	5/10	391.3	<b>8/10</b>	<b>273.8</b>	<b>10/10</b>	<b>273.2</b>
	P.W.	10/10	208.7	<b>10/10</b>	<b>377.6</b>	8/10	666.0	7/10	795.4	<b>10/10</b>	<b>624.2</b>	<b>8/10</b>	<b>665.7</b>	6/10	293.7	10/10	390.9

**S1**  $\square_{[0,30]}$  ( $speed < 120$ )

**S2**  $\square_{[0,30]}$  ( $gear = 3 \rightarrow speed \geq 20$ )

**S3**  $\diamond_{[10,30]}$  ( $speed \leq 53 \vee speed \geq 57$ )

**S4**  $\square_{[0,29]}$  ( $speed < 100$ )  $\vee$   $\square_{[29,30]}$  ( $speed > 65$ )

**S5**  $\square_{[0,30]}$  ( $rpm < 4770 \vee \square_{[0,1]}$  ( $rpm > 600$ ))

**Sbasic**  $\square_{[11,30]}$  ( $\neg(|AF - AF_{ref}| > 0.05 * 14.7)$ )

**Sstable**  $\neg(\diamond_{[6,26]} \square_{[0,4]} (AF - AF_{ref} > 0.01 * 14.7))$

**Strap**  $\neg \diamond_{[0,5]} (x, y \in [3.9, 4.1] \wedge \dot{x}, \dot{y} \in [-1, 1])$

Model:

- AT: Automatic Transmission
- AFC: Abstract Fuel Control
- FFR: Free Floating Robot

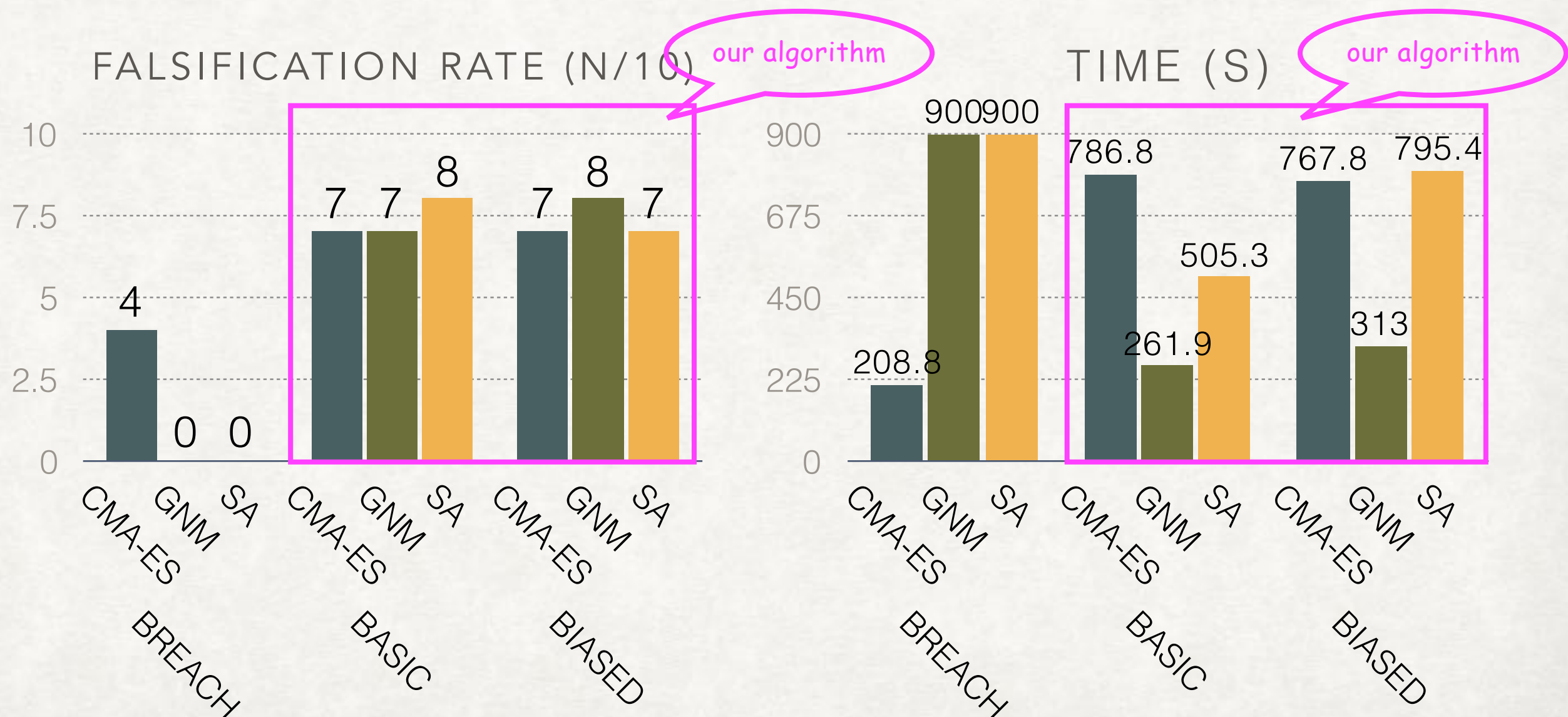
Algorithm:

- Breach: optimization
- Basic: MCTS + Hill-Climbing
- P.W.: MCTS + Hill-Climbing + progressive widening

# Experimental evaluation

Model: Automatic transmission:

Property:  $\square_{[0,29]}(\text{speed} < 100) \vee \square_{[29,30]}(\text{speed} > 65)$

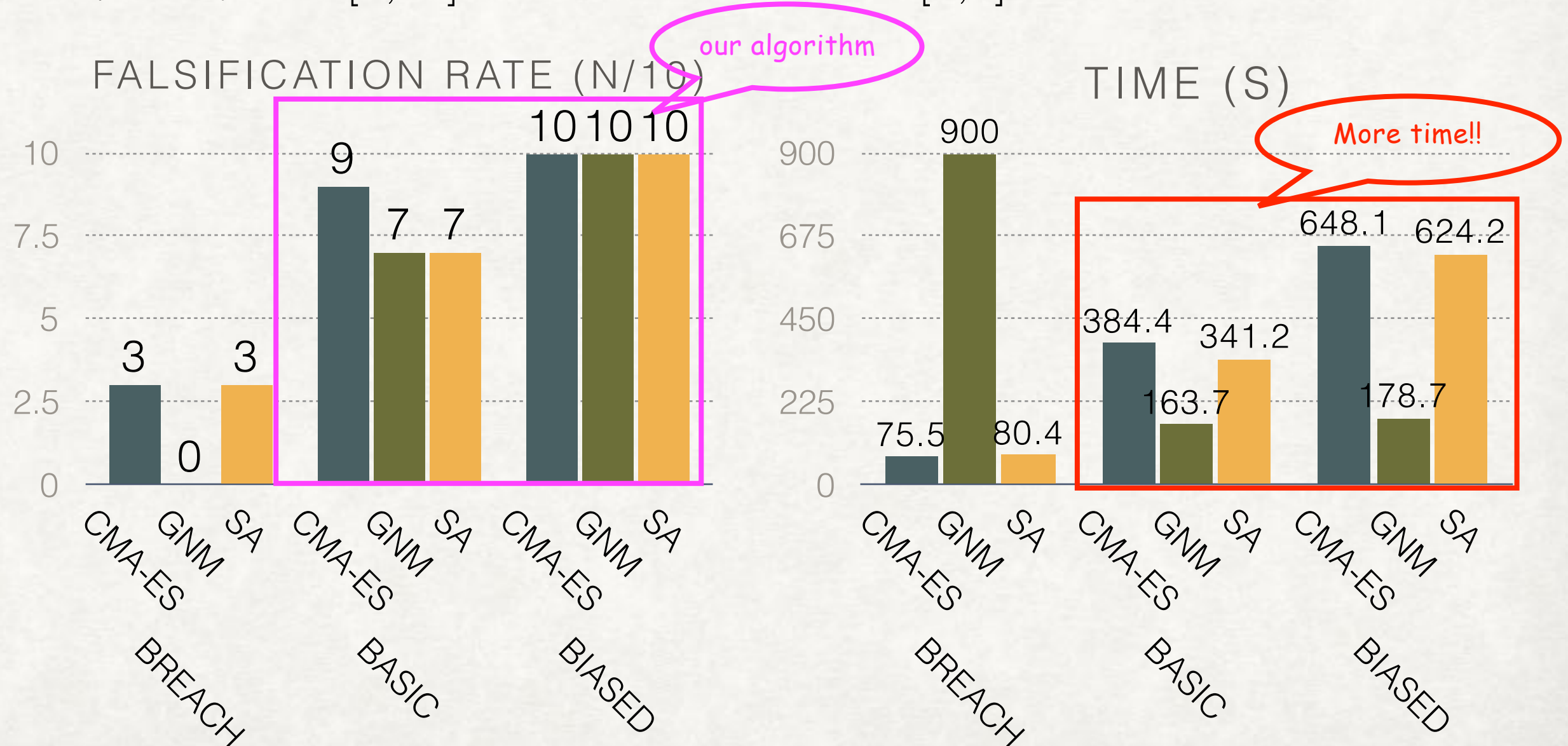




# Experimental evaluation

Model: Automatic transmission

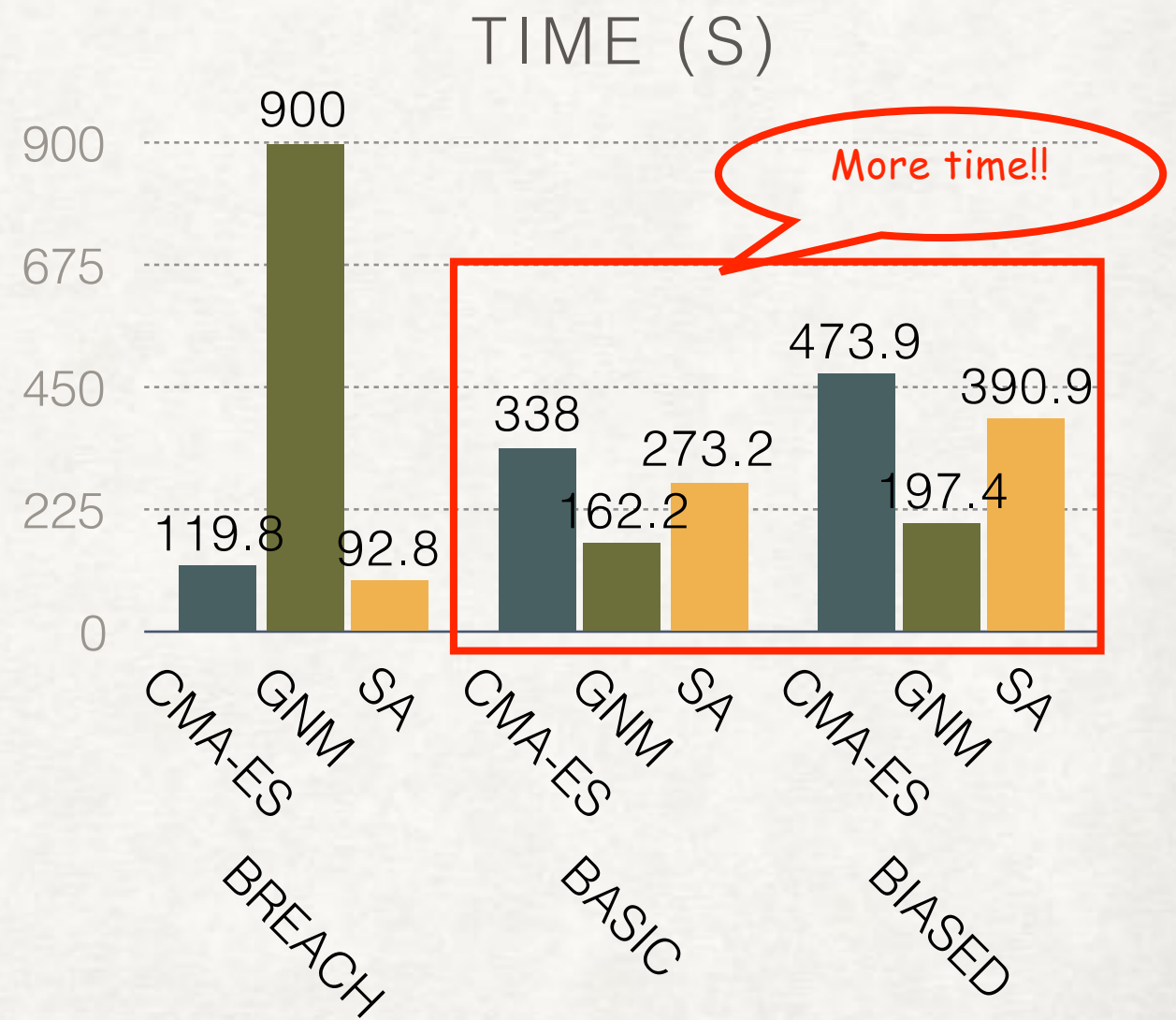
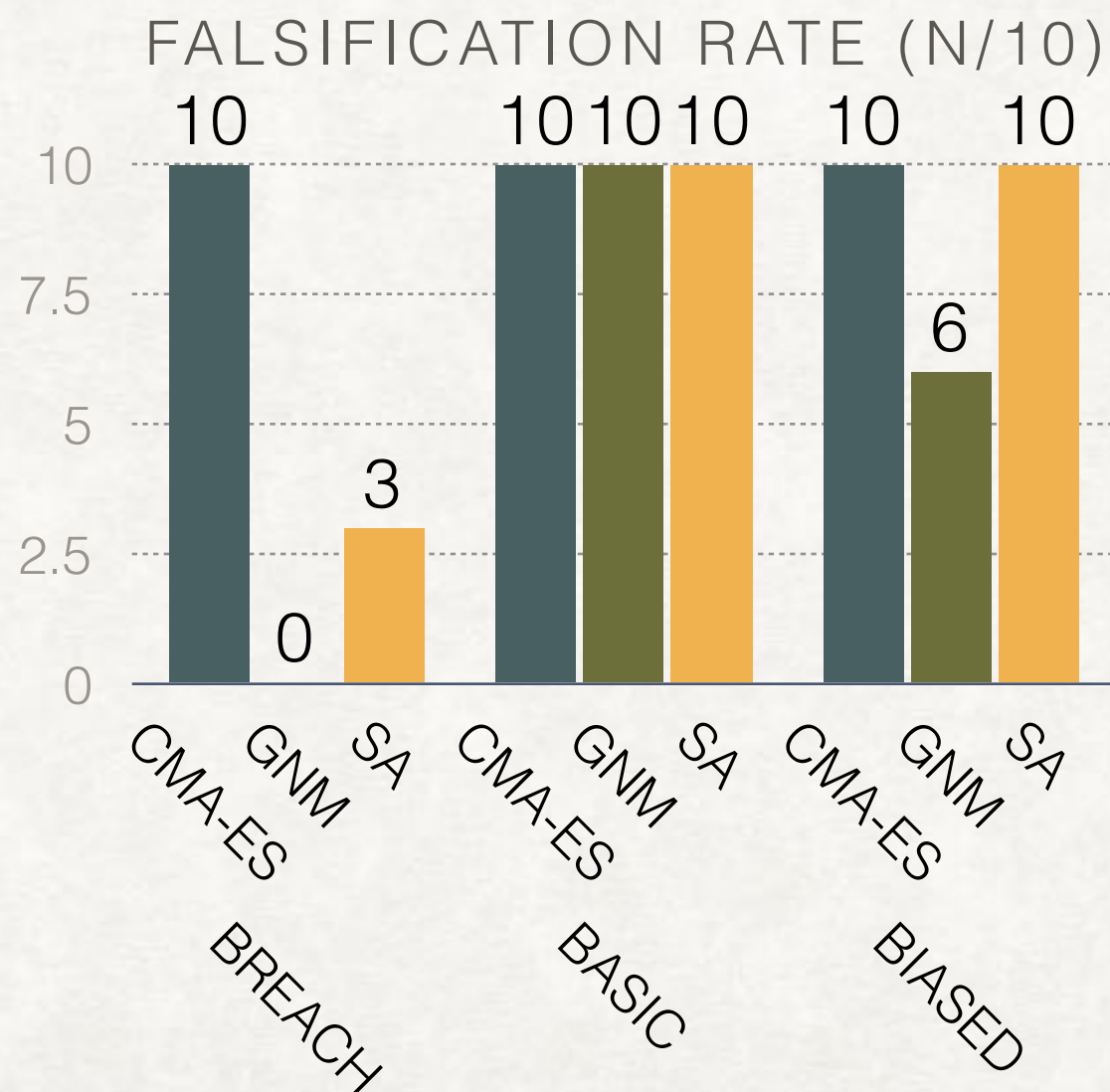
Property:  $\square_{[0,30]}(rpm < 4700 \vee \square_{[0,1]}(rpm > 600))$



# Experimental evaluation

Model: Free floating robot

Property:  $\neg \diamond_{[0,5]} (x, y \in [3.9, 4.1] \wedge \dot{x}, \dot{y} \in [-1, 1])$





# Experimental evaluation

- Our approach improves the falsification rate in most cases
- Sometimes our approach takes more time to find the solution
  - MCTS takes more time on exploration and it is acceptable.

# Conclusion and Future work

- This paper proposes a two-layered framework:
  - High level: Monte Carlo Tree Search to guide the search direction
  - Low level: Hill-climbing to do playout to give reward to each node
- Experimental evaluation shows that our approach can solve some hard problems within acceptable time.
- Future work:
  - Quantitative coverage metric



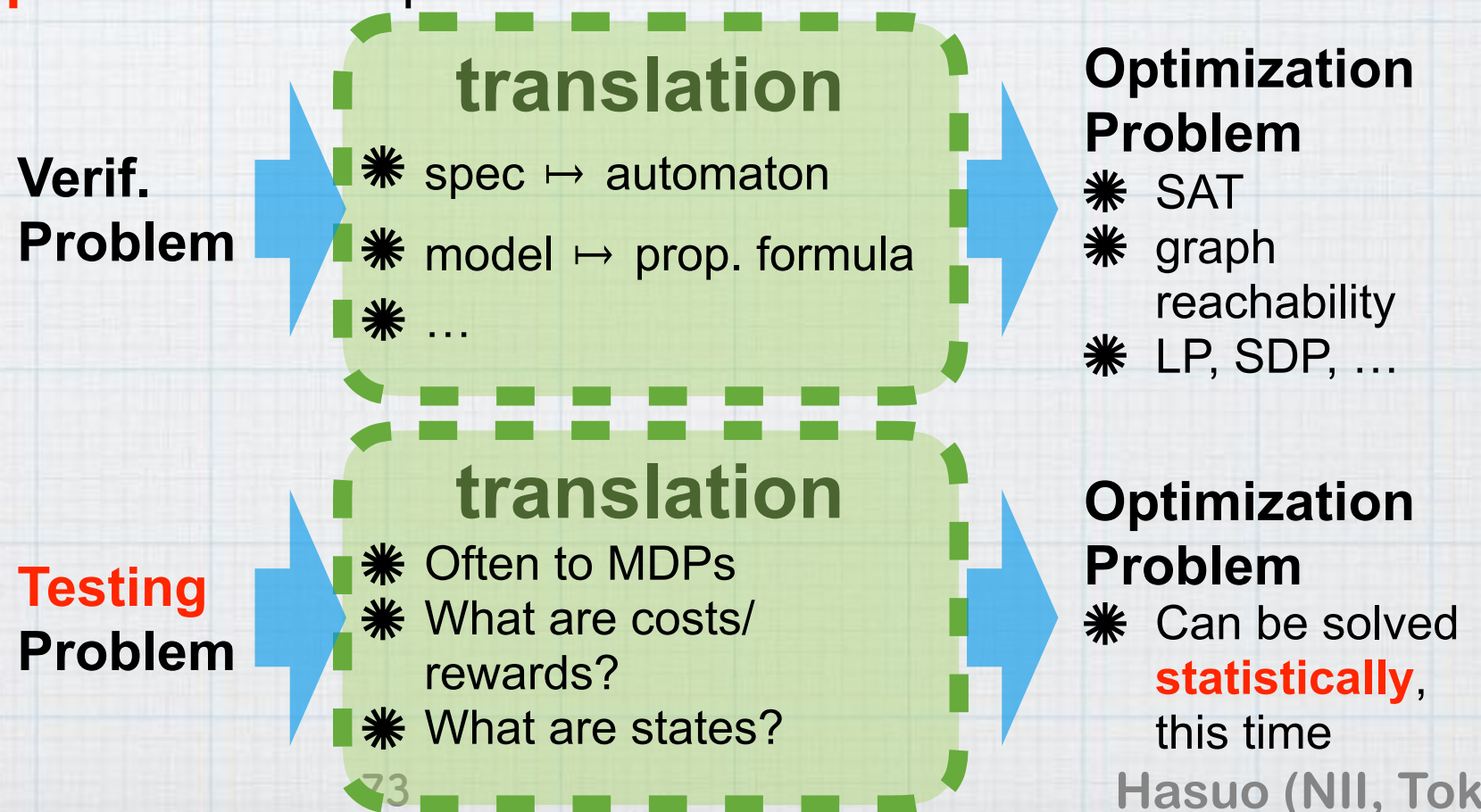
THANK YOU!



# Verification, Control, Testing, ... Reduction to Optimization

- \* Verification → **testing**
  - \* Fight **complexity**. Accommodate **black-box** systems/models
- \* Rigorous graph algorithms, convex optimization → **statistical machine learning**
  - \* Faster
  - \* Maybe imprecise. But do we need that much precision?
- \* **Formal methods techniques** are still important

- \* Formal verification:





# Outline

- \* Cyber-physical systems under uncertainties
- \* **Formal methods** and **testing** for CPS
- \* Hybrid system falsification
  - \* Logical connectives [CAV'19]
  - \* Causality in time [EMSOFT'18]
  - \* ... as demonstration of combining **logical** and **statistical**
- \* Other topics



# Formal Safety Architecture

- \* Example: simplex architecture (right)

- \* **AC** is complex, performance-oriented, black-box
- \* **BC** is simple, safety-oriented, (hopefully) white-box

- \* Idea: we can verify the whole system even if **AC is a black-box!**

- \* Enough to show: safety of BC, and correctness of DM
- \* We impose certain **contracts** on AC

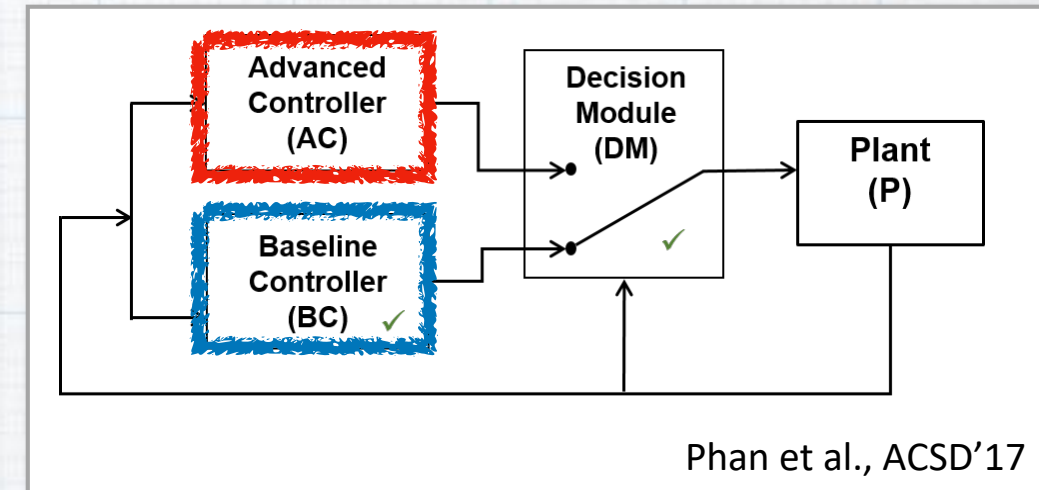
- \* Related

- \* FM4AI (ML/AI components as AC)
- \* Monitoring (checking contracts on AC)

- \* One promising way to

**make formal verification down-scalable**

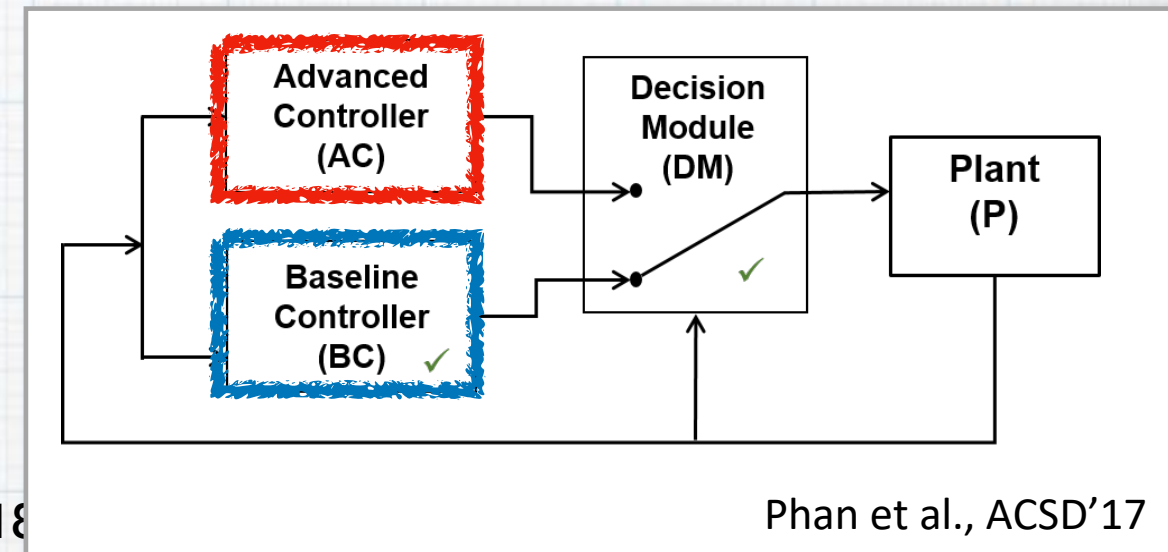
- \* Weaker contracts on AC  
→ weaker safety guarantee (but hopefully non-zero)





# Formal Safety Architecture

- \* At ERATO MMSD:  
we formalize, verify and refine safety architectures
- \* Event-B: a formal modeling language  
[Abrial, “The Event-B Book”, 2010 CUP] [Kobayashi+, ICFEM’18]  
Based on state transition systems.  
A tool Rodin supports:
  - \* Safety proofs
  - \* Incremental modeling by refinements
    - \* Flexibility in choosing model fidelity → down-scaling
    - \* From (our) general model to (industry partner’s) individual model





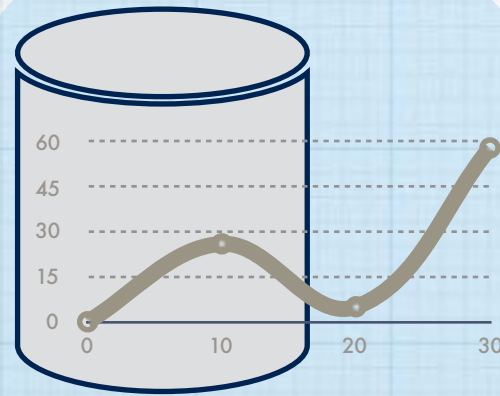
# Pattern Matching against Timed Automata, Monitoring

## Specification

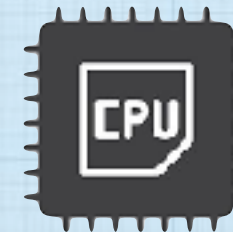
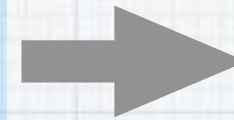
“Frequent gear changes within 3 sec after shifting up to 4th”



Running  
system



Log



Monitor



Monitoring  
result

“From 18.9 sec. to  
23.2 sec.”

- \* Runtime verification, monitoring
- \* Not straightforward, esp. when specs involve timing constraints
  - \* Speed requirements (GBs of log per second)
  - \* Computing resource (embedded)
  - \* ...
- \* Industry needs
- \* Technically: theory of **(parametrized) timed automata**





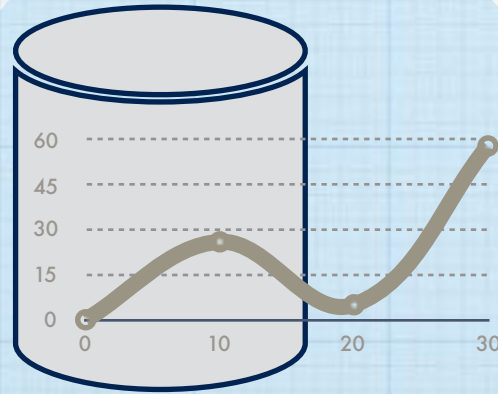
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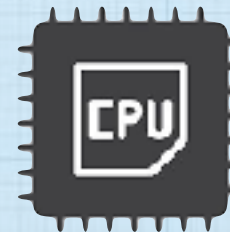
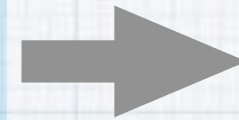
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Running  
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Log

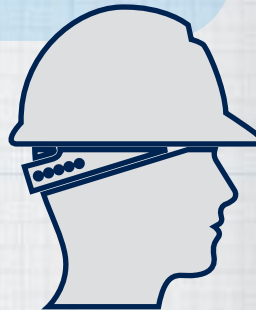


Monitor



Monitoring  
result

“From 18.9 sec. to  
23.2 sec.”



## \* Use cases

- \* “Here is 1 PB of log, and I want to extract its relevant parts”
- \* “Raise an alert if this specific type of anomaly occurs”

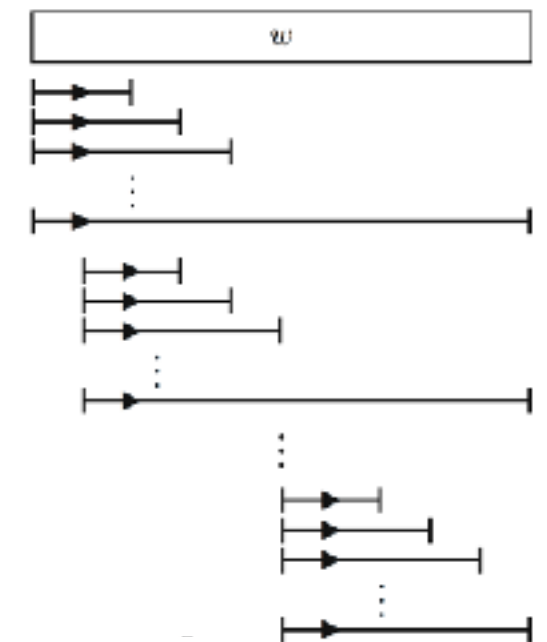


# Monitoring: Problem Formulations

- \* Given: a log, discrete time  $w = abaaacb\dots bbc$   
 a spec  $\varphi$  "no occurrence of c for 6 steps after b"  
 Answer: all subsequences of  $w$  that satisfy  $\varphi$

- \* Given: a log, **continuous** time  $w = (a, 0.12) (b, 1.28) \dots$   
 a spec  $\varphi$  "no occurrence of c for 6 **seconds** after b"  
 Answer: all subsequences of  $w$  that satisfy  $\varphi$   
 [Ulus, CAV'17] [Waga+, FORMATS'17]

Nontrivial due to temporal causality



Infinitely many such subsequences  
 (starting at  $t=1$ ?  $t = 1.01$ ?  $t = 1.001$ ? ...)  
 → Efficient representation & computation by **zones**

- \* Given: a log, **continuous** time  $w = (a, 0.12) (b, 1.28) \dots$   
 a **parametrized** spec  $\varphi(p)$   
 "no occurrence of c for **p** seconds after b" "b occurs with a period of **p** seconds"  
 Answer: all the pairs of  $(p, (\text{a subseq. of } w \text{ that satisfies } \varphi))$

[Andre+, ICECCS'18] [Waga+, NFM'19] [Waga+, CAV'19]

In industry, fixing a spec is a big challenge.  
 Parameters → **flexibility** in specs



# Monitoring: Our Achievements

- \* Given: a log, discrete time  $w = \text{abaaacb...bbc}$   
a spec  $\varphi$  "no occurrence of c for 6 steps after b"  
Answer: all subsequences of  $w$  that satisfy  $\varphi$

Efficient algorithm from theory of **timed automata**.  
Processes ~ 1M events/second (laptop).

- \* Given: a log, **continuous** time  $w = (a, 0.12) (b, 1.28) \dots$   
a spec  $\varphi$  "no occurrence of c for 6 **seconds** after b"  
Answer: all subsequences of  $w$  that satisfy  $\varphi$   
[Ulus, CAV'17] [Waga+, FORMATS'17]

[Waga+, FORMATS'17]  
<https://github.com/maswag/monaa>

Also implemented on  
Renesas RH850

Efficient algorithm using **parametrized timed automata**.  
Processes ~ 10K events/second (laptop). [Waga+, NFM'19]  
<https://github.com/maswag/symon>

- \* Given: a log, **continuous** time  $w = (a, 0.12) (b, 1.28) \dots$   
a **parametrized** spec  $\varphi(p)$   
"no occurrence of c for **p** seconds after b" "b occurs with a period of **p** seconds"  
Answer: all the pairs of  $(p, (\text{a subseq. of } w \text{ that satisfies } \varphi))$   
[Andre+, ICECCS'18] [Waga+, NFM'19] [Waga+, CAV'19] ...



# Outline

- \* Cyber-physical systems under uncertainties
- \* **Formal methods** and **testing** for CPS
- \* Hybrid system falsification
  - \* Logical connectives [CAV'19]
  - \* Causality in time [EMSOFT'18]
  - \* ... as demonstration of combining **logical** and **statistical**
- \* Other topics



# Conclusions

- \* Focused on **safety-critical CPS** with statistical ML components
- \* **Don't trust statistical AI.**  
Use them with precaution
  - \* System-level safety
- \* Formal methods are not applicable per se  
→ combine **logical** and **statistical** reasoning
  - \* Hierarchical optimization in falsification, as an example
- \* Quality assurance under uncertainties
  - \* A scientific and engineering problem,
  - \* that is challenging but rewarding!