

Token-passing semantics *with and without* rewriting

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Token-passing semantics *without* rewriting

Token-passing semantics *without* rewriting

execution models, provided by Girard's GoI,
of functional programming

- call-by-name λ -calculus [Danos&Regnier '99] [Mackie '95]
- call-by-value λ -calculus [Fernandez&Mackie '02]
- and more: PCF, effects, concurrency...

Token-passing semantics *without* rewriting

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of functional programming

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- call-by-value λ -calculus [Fernandez&Mackie '95]
- and more: PCF, effects, concurrency...

(MELL) proof net,
 λ -graph, ...

<i>program</i>	<i>diagram</i>
<i>evaluation</i>	<i>token passing</i>

Token-passing semantics *without* rewriting

<i>program</i>	<i>diagram</i>
<i>evaluation</i>	<i>token passing</i>
<i>result</i>	<i>token data/position</i>

live demo:

Jumping Abstract Machine for call-by-name λ -calculus [DR99]

<https://koko-m.github.io/GoI-Visualiser/>

Token-passing semantics *without* rewriting

<i>program</i>	<i>λ-graph + !-boxes</i>
<i>evaluation</i>	<i>token passing + jumping</i>
<i>result</i>	<i>token data/position</i>

live demo:

Jumping Abstract Machine for call-by-name λ -calculus [DR99]

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Token-passing semantics *without* rewriting

<i>program</i>	<i>diagram</i>
<i>evaluation</i>	<i>token passing</i>
<i>result</i>	<i>token data/position</i>

execution models of functional programming

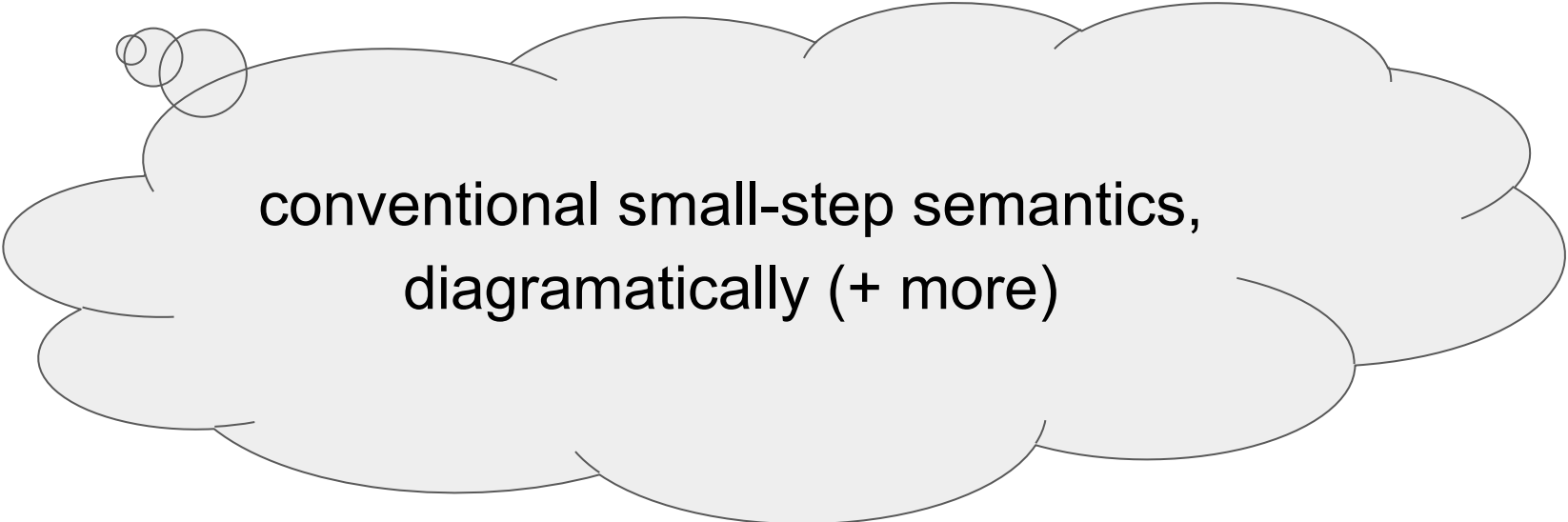
- compiler [Mackie '95]
- higher-order synthesis [Ghica '07]

Token-passing semantics *with* rewriting

Token-passing semantics *with* rewriting

execution models of functional programming

- call-by-name & call-by-value λ -calculus [Sinot '05]
- call-by-need & fully lazy λ -calculus [Sinot '06]
- call-by-need & call-by-value λ -calculus [–&Ghica '17]



conventional small-step semantics,
diagrammatically (+ more)

Token-passing semantics *with* rewriting

execution models of functional programming

- call-by-name & call-by-value λ -calculus [Sinot '05]
- call-by-need & fully lazy λ -calculus [Sinot '05]
- call-by-need & call-by-value λ -calculus [Sinot '05]

inspired by
virtual reduction
[Danos&Regnier '93]

<i>program</i>		<i>diagram</i>
<i>evaluation</i>	<i>redex search</i>	<i>token passing</i>
	<i>reduction</i>	<i>diagram rewriting</i>

Token-passing semantics *with* rewriting

<i>program</i>		<i>diagram</i>
<i>evaluation</i>	<i>redex search</i>	<i>token passing</i>
	<i>reduction</i>	<i>diagram rewriting</i>
<i>result</i>		<i>diagram</i>

live demo:

Dynamic GoI Machine for call-by-value λ -calculus [KG17]

<https://koko-m.github.io/GoI-Visualiser/>

Token-passing semantics *with* rewriting

<i>program</i>		λ-graph + !-boxes
<i>evaluation</i>	<i>redex search</i>	<i>token passing</i>
	<i>reduction</i>	<i>diagram rewriting</i>
<i>result</i>		λ-graph + !-boxes

live demo:

Dynamic GoI Machine for call-by-value λ -calculus [KG17]

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Token-passing semantics *with* rewriting

<i>program</i>		<i>diagram</i>
<i>evaluation</i>	<i>redex search</i>	<i>token passing</i>
	<i>reduction</i>	<i>diagram rewriting</i>
<i>result</i>		<i>diagram</i>

execution models of functional programming

- with robustness [S05] [S06]
- with time/space efficiency [MG17]

Token-passing semantics *with* rewriting

<i>program</i>		<i>diagram</i>
<i>evaluation</i>	<i>redex search</i>	<i>token passing</i>
	<i>reduction</i>	<i>diagram rewriting</i>
<i>result</i>		<i>diagram</i>

whenever possible

execution models of functional programs

- with robustness [S05] [S06]
- with time/space efficiency [MG17]

Token-passing semantics *with* rewriting

<i>program</i>		<i>diagram</i>
<i>evaluation</i>	<i>redex search</i>	<i>token passing</i>
	<i>reduction</i>	<i>diagram rewriting</i>
<i>result</i>		<i>diagram</i>

selective?

execution models of functional program

- with robustness [S05] [S06]
- with time/space efficiency [MG17]

Token-passing semantics *with and without* rewriting

token-passing semantics *without* rewriting

... space efficiency



token-passing semantics *with* rewriting

... time efficiency



selective rewriting

non-trivial space/time balancing?

token-passing semantics *without* rewriting

... space efficiency



token-passing semantics *with* rewriting

... time efficiency



selective rewriting

non-trivial space/time balancing?

A red starburst shape with multiple points, containing the text "another perspective".

**another
perspective**

token-passing semantics *without* rewriting

... result given by the token



token-passing semantics *with* rewriting

... result given by a diagram



selective rewriting

programming with dual result

... given by the token *and* a diagram?

token-passing semantics *without* rewriting

... result given by the token



token-passing semantics *with* rewriting

... result given by a diagram



selective rewriting

programming with “computation graphs”

... result being value with computation graph

Programming with “computation graphs”

result

*value
with computation graph*

- construction
- manipulation

Programming with “computation graphs”

TensorFlow, Google’s machine-learning library

```
W = tf.Variable(...)  
b = tf.Variable(...)  
y = W * x_data + b
```

```
x_data = ...  
y_data = ...  
sess = tf.Session()  
sess.run(init)  
sess.run(train)
```

```
x_data = ...  
sess = tf.Session()  
sess.run(init)  
y_initial_values =  
sess.run(y)
```

construction

machine-learning model
with parameters

manipulation

model training
(imperative parameter update)

value extraction

output prediction

Programming with “computation graphs”

TensorFlow, Google’s machine-learning library

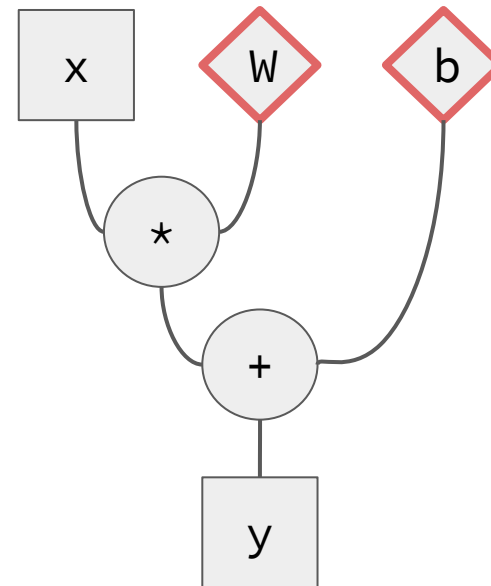
```
W = tf.Variable(...)  
b = tf.Variable(...)  
y = W * x_data + b
```

```
x_data = ...  
y_data = ...  
sess = tf.Session()  
sess.run(init)  
sess.run(train)
```

```
x_data = ...  
sess = tf.Session()  
sess.run(init)  
y_initial_values =  
sess.run(y)
```

construction

“variables”



Programming with “computation graphs”

TensorFlow, Google’s machine-learning library

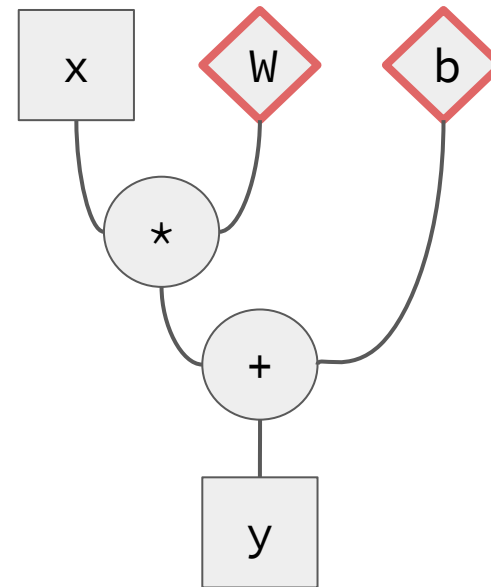
```
W = tf.Variable(...)  
b = tf.Variable(...)  
y = W * x_data + b
```

```
x_data = ...  
y_data = ...  
sess = tf.Session()  
sess.run(init)  
sess.run(train)
```

```
x_data = ...  
sess = tf.Session()  
sess.run(init)  
y_initial_values =  
sess.run(y)
```

construction

~~“variables”~~
“parameters”



Programming with “computation graphs”

TensorFlow, Google’s machine-learning library

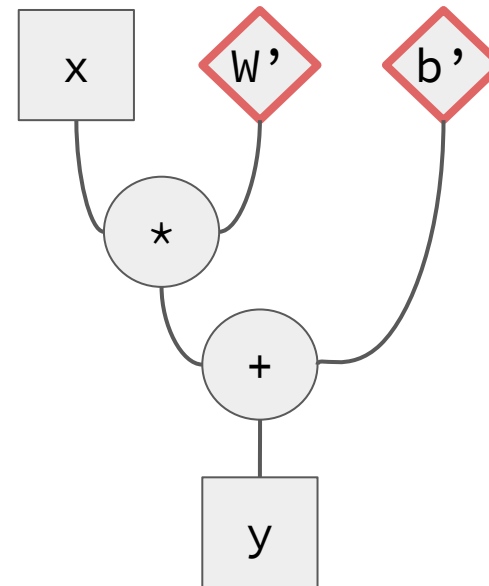
```
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b = tf.Variable(...)  
y = W * x_data + b
```

```
x_data = ...  
y_data = ...  
sess = tf.Session()  
sess.run(init)  
sess.run(train)
```

```
x_data = ...  
sess = tf.Session()  
sess.run(init)  
y_initial_values =  
sess.run(y)
```

manipulation

in-place (imperative)
parameter update



Programming with “computation graphs”

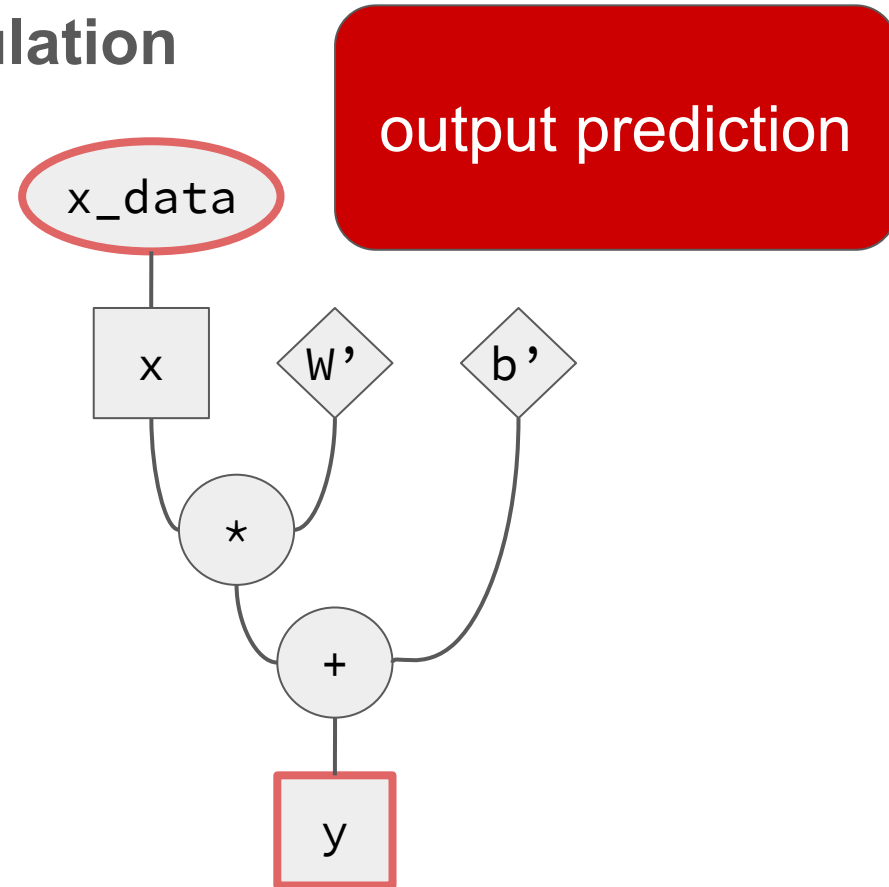
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y = W * x_data + b
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```

```
x_data = ...  
sess = tf.Session()  
sess.run(init)  
y_initial_values =  
sess.run(y)
```

manipulation



Programming with “computation graphs”

Self-Adjusting Computation [Acar '05]

“spreadsheet”

(Incremental, an OCaml library)

```
let x = Inc.Var.create 1 in
let y = Inc.map2
  (Inc.Var.watch x)
  (Inc.Var.watch x) ~f:( + ) in
let z = Inc.Var.create 2 in
let w = Inc.map2
  (Inc.Var.watch y)
  (Inc.Var.watch z) ~f:( + ) in
let w_obs = Inc.observe w in
Inc.Var.set x 3;

Inc.stabilize ();

print_int
  (Inc.Observer.value_exn w_obs)
```

construction

acyclic dependency graph
with “modifiabiles/cells”

manipulation

change propagation

value extraction

Programming with “computation graphs”

Self-Adjusting Computation [Acar '05]

“spreadsheet”

(Incremental, an OCaml library)

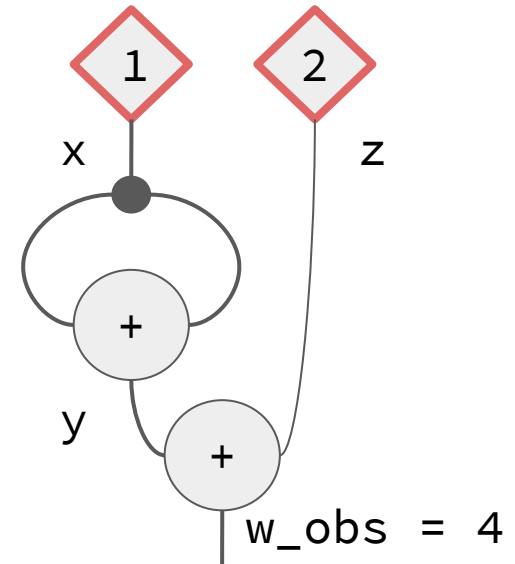
```
let x = Inc.Var.create 1 in
let y = Inc.map2
  (Inc.Var.watch x)
  (Inc.Var.watch x) ~f:( + ) in
let z = Inc.Var.create 2 in
let w = Inc.map2
  (Inc.Var.watch y)
  (Inc.Var.watch z) ~f:( + ) in
let w_obs = Inc.observe w in
Inc.Var.set x 3;

Inc.stabilize ();

print_int
  (Inc.Observer.value_exn w_obs)
```

construction

“modifiables”
“cells”



Programming with “computation graphs”

Self-Adjusting Computation [Acar '05]

“spreadsheet”

(Incremental, an OCaml library)

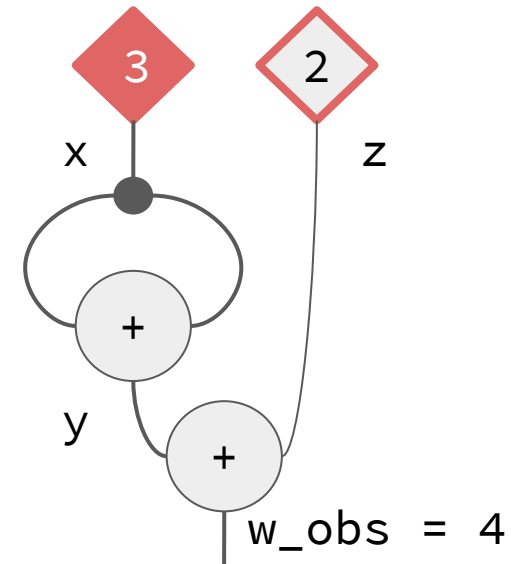
```
let x = Inc.Var.create 1 in
let y = Inc.map2
  (Inc.Var.watch x)
  (Inc.Var.watch x) ~f:( + ) in
let z = Inc.Var.create 2 in
let w = Inc.map2
  (Inc.Var.watch y)
  (Inc.Var.watch z) ~f:( + ) in
let w_obs = Inc.observe w in
Inc.Var.set x 3;

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print_int
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construction

change set



Programming with “computation graphs”

Self-Adjusting Computation [Acar '05]

“spreadsheet”

(Incremental, an OCaml library)

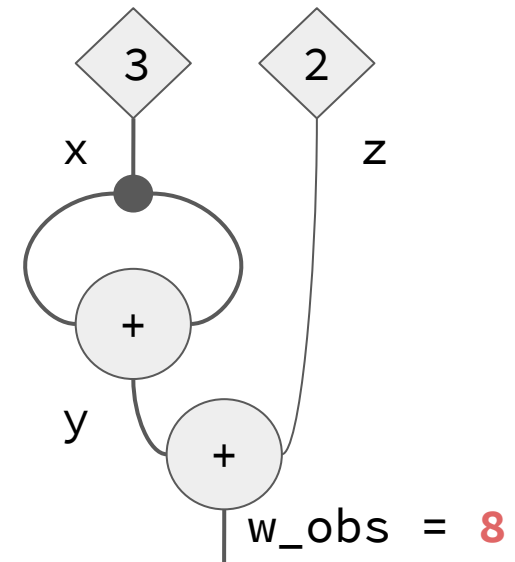
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  (Inc.Var.watch x) ~f:( + ) in
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let w = Inc.map2
  (Inc.Var.watch y)
  (Inc.Var.watch z) ~f:( + ) in
let w_obs = Inc.observe w in
Inc.Var.set x 3;

Inc.stabilize ();

print_int
  (Inc.Observer.value_exn w_obs)
```

manipulation

change propagation



Programming with “computation graphs”

Self-Adjusting Computation [Acar '05]

“spreadsheet”

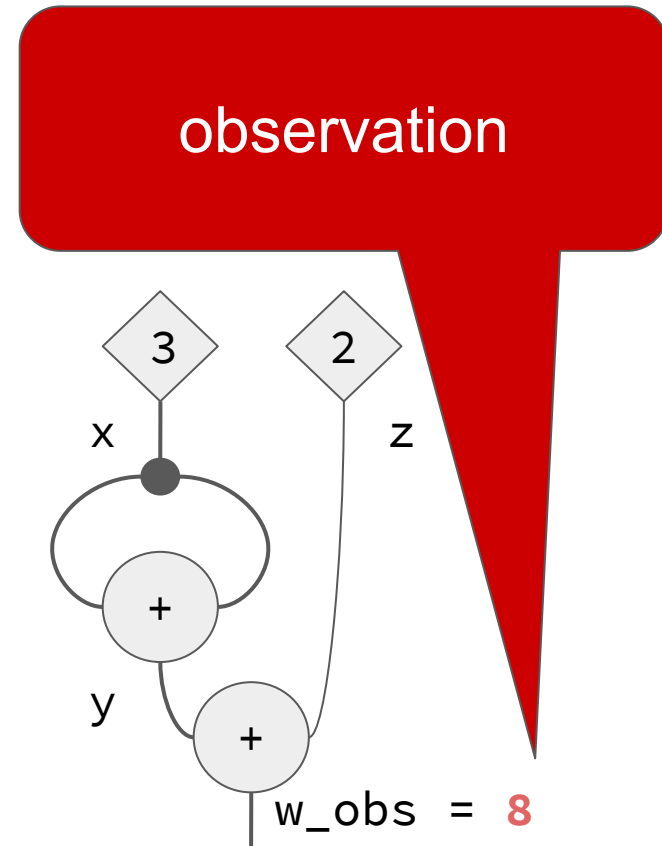
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let y = Inc.map2
  (Inc.Var.watch x)
  (Inc.Var.watch x) ~f:( + ) in
let z = Inc.Var.create 2 in
let w = Inc.map2
  (Inc.Var.watch y)
  (Inc.Var.watch z) ~f:( + ) in
let w_obs = Inc.observe w in
Inc.Var.set x 3;

Inc.stabilize ();

print_int
  (Inc.Observer.value_exn w_obs)
```

value extraction



Programming with “computation graphs”

Probabilistic Programming

[program]

construction

stochastic model + observations

[run-time system]

manipulation

stochastic inference

value extraction

posterior distribution

Programming with “computation graphs”



- construction
- manipulation

TensorFlow

imperative parameter update on machine-learning model

Self-Adjusting Computation

change propagation on acyclic dependency graph

Probabilistic Programming

inference on stochastic model

token-passing semantics *without* rewriting

... result given by the token



token-passing semantics *with* rewriting

... result given by a diagram



selective rewriting

programming with “computation graphs”

... result being value with computation graph

Token-passing semantics *with* & *without* rewriting

<i>program</i>		<i>diagram</i>
<i>evaluation</i>	<i>redex search</i>	<i>token passing</i>
	<i>reduction</i>	<i>diagram rewriting</i>
<i>computation graphs</i>	<i>construction</i>	selective <i>diagram rewriting</i>
	<i>manipulation</i>	<i>diagram rewriting</i>
	<i>value extraction</i>	<i>token data</i>

Programming with “computation graphs”



- construction
- manipulation

Idealised TensorFlow [–, Cheung&Ghica ‘18]

functional parameter update on machine-learning model

Synchronous Self-Adjusting Computation

change propagation on **cyclic** dependency graph

Synchronous Self-Adjusting Computation

live demo: <https://cwtsteven.github.io/GoI-SAC-Visualiser/>

```
x = {1}
y = x + x
z = {2}
w = y + z
link x to 3;

_ = step ()
_ = step ()
w;
```

construction

cyclic dependency graph
with “modifiables/cells”

manipulation

cell-wise change propagation

multiple
independent tokens
without rewriting

Synchronous Self-Adjusting Computation

live demo: <https://cwtsteven.github.io/GoI-SAC-Visualiser/>

```
(* alternating signal *)
```

```
x = {true}
```

```
link x to ~x;
```

```
_ = step ()
```

```
_ = step ()
```

construction

cyclic dependency graph
with “modifiabiles/cells”

manipulation

cell-wise change propagation

multiple
independent tokens
without rewriting

token-passing semantics *without* rewriting

... result given by the token



token-passing semantics *with* rewriting

... result given by a diagram



selective rewriting

programming with “computation graphs”

... result being value with computation graph

given by the token and a diagram with “cells”

Token-passing semantics *with* & *without* rewriting

<i>program</i>		<i>diagram</i>
<i>evaluation</i>	<i>redex search</i>	<i>token passing</i>
	<i>reduction</i>	<i>diagram rewriting</i>
<i>computation graphs</i>	<i>construction</i>	selective <i>diagram rewriting</i>
	<i>manipulation</i>	<i>diagram rewriting</i>
	<i>value extraction</i>	<i>token data</i>

Directions

- sit back and lay the foundation?
 - “cells”, special constants
 - shared but never duplicated
 - blocking rewrite

- more applications?
 - differentiating (higher-order) computation graphs
 - digesting meta-level stochastic inference