

1. The arrow  $d : Y \rightarrow \overline{F}Y$  satisfies  $J!_{\overline{F}Y} \odot d = J!_Y$ .
2. Precomposing  $d : Y \rightarrow \overline{F}Y$  preserves the greatest fixed point of a decreasing sequence in  $\mathcal{Kl}(T)(\overline{F}Y, A)$ . Namely, for a decreasing sequence  $g_0 \sqsupseteq g_1 \sqsupseteq g_2 \dots : \overline{F}Y \rightarrow A$  of Kleisli arrows,  $\bigcap_{i \in \omega} (g_i \odot b) = (\bigcap_{i \in \omega} g_i) \odot b$  holds.
3. Precomposing  $d : Y \rightarrow \overline{F}Y$  preserves the largest mediating arrow. Namely, if  $l_{\max} : \overline{F}Y \rightarrow Z$  is the largest mediating arrow from a cone  $(\overline{F}Y, (\delta_i : \overline{F}Y \rightarrow \overline{F}^i 1))$  to a weak 2-limit  $(Z, (J\pi_i : Z \rightarrow \overline{F}^i 1))$ , then  $l_{\max} \odot d : Y \rightarrow Z$  is the largest mediating arrow from a cone  $(X, (\delta_i \odot b : X \rightarrow \overline{F}^i 1))$  to the weak 2-limit.