

1. The arrow $d : Y \rightarrow \overline{F}Y$ satisfies $J!_{\overline{F}Y} \odot d = J!_Y$.
2. Precomposing $d : Y \rightarrow \overline{F}Y$ preserves the greatest fixed point of a decreasing sequence in $\mathcal{Kl}(T)(\overline{F}Y, A)$. Namely, for a decreasing sequence $g_0 \supseteq g_1 \supseteq g_2 \dots : \overline{F}Y \rightarrow A$ of Kleisli arrows, $\prod_{i \in \omega} (g_i \odot b) = (\prod_{i \in \omega} g_i) \odot b$ holds.
3. Precomposing $d : Y \rightarrow \overline{F}Y$ preserves the largest mediating arrow. Namely, if $l_{\max} : \overline{F}Y \rightarrow Z$ is the largest mediating arrow from a cone $(\overline{F}Y, (\delta_i : \overline{F}Y \rightarrow \overline{F}^i \mathbf{1}))$ to a weak 2-limit $(Z, (J\pi_i : Z \rightarrow \overline{F}^i \mathbf{1}))$, then $l_{\max} \odot d : Y \rightarrow Z$ is the largest mediating arrow from a cone $(X, (\delta_i \odot b : X \rightarrow \overline{F}^i \mathbf{1}))$ to the weak 2-limit.